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Characterisation of Structural Disorder in γ-Ga$_2$O$_3$

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Abstract Solvothermal oxidation of metallic gallium in monoethanolamine for 72 hours at 240 °C yields a crystalline sample of γ-Ga$_2$O$_3$ (~30 nm crystallites). While Rietveld refinement (cubic spinel structure, $Fdar{3}m$, $a = 8.23760(9)$ Å) reveals that Ga occupies two pairs of octahedral and tetrahedral sites (ideal spinel and non-spinel), it provides no information about their local distribution, which cannot be statistical owing to the short Ga-Ga contacts produced if neighbouring ideal spinel and non-spinel sites are simultaneously occupied. To create an atomistic model to reconcile this situation, a $6 \times 6 \times 6$ supercell of the crystal structure is constructed and refined against neutron total scattering data using a reverse Monte Carlo (RMC) approach. This accounts well for the local as well as long-range structure, and reveals significant local distortion in the octahedral sites that resembles the structure of thermodynamically stable β-Ga$_2$O$_3$. $^{71}$Ga solid-state NMR reveals a ratio of octahedral:tetrahedral Ga that is consistent with the model obtained from RMC. Nanocrystalline samples of γ-Ga$_2$O$_3$ are produced by either a short solvothermal reaction (240 °C for 11 hours in diethanolamine; ~15 nm crystallites) or by precipitation from an ethanolic solution of gallium nitrate (~5 nm crystallites). For these samples, the Bragg scattering profile is broadened by their smaller crystallite size, consistent with transmission electron microscopy, and analysis of the relative Bragg peak intensities provides evidence that a greater proportion of tetrahedral vs octahedral sites are filled. In contrast, neutron total scattering shows the same average Ga-O distance with decreasing particle size, consistent with $^{71}$Ga solid-state NMR that indicates that all samples contain the same overall proportion of octahedral:tetrahedral Ga. It is postulated that increased occupation of tetrahedral sites within the smaller crystallites is balanced by an increased proportion of octahedral surface Ga sites, owing to termination by bound solvent or hydroxide.

Keywords: Spinel; Neutron scattering; Reverse Monte Carlo; Solid-State NMR
Introduction

The structure of $\gamma$-Ga$_2$O$_3$ is recognised as being similar to $\gamma$-Al$_2$O$_3$, a cubic, cation-deficient spinel with partial occupancy of both tetrahedral and octahedral sites. The relative proportion of occupied sites and their distribution, however, gives rise to inherent structural disorder that makes this analogy more complex. The catalytic chemistry of $\gamma$-Al$_2$O$_3$ has been widely investigated and indeed its use as a catalyst support is commonplace. The solid solution $\gamma$-Ga$_2$O$_3$-$\gamma$-Al$_2$O$_3$ has also been investigated for specific catalysis applications, and it is believed that preferential occupation of the tetrahedral sites by gallium leads to unique properties for the surface aluminium, such as in methane-selective catalytic reduction of NO, and in the dehydrogenation of propene. $\gamma$-Ga$_2$O$_3$ has itself been studied for various applications in catalysis and compared with other Ga$_2$O$_3$ polymorphs; for example, in the steam reforming of methanol and the photocatalytic degradation of volatile organics. Recently Lueangchaichaweng et al. have reported the use of gallium oxide nanorods, largely the $\gamma$ polymorph, as high effective catalysts for epoxidation reactions of alkenes. Interesting optical properties have also been a focus of recent attention for $\gamma$-Ga$_2$O$_3$: Chen et al. described the formation of quantum dots with blue-green photoluminescence, which Wang et al. showed was particle-size controllable and could be enhanced by inducing defects under reductive conditions. The formation of mesoporous $\gamma$-Ga$_2$O$_3$ has been reported, and recently the growth of thin films of $\gamma$-Ga$_2$O$_3$ has been explored. It also relevant to note that that various transition-metal-containing gallium oxides with spinel structures have recently been investigated and studied for their magnetic, optical and photocatalytic properties.

Unlike the structures of alumina polymorphs, the structures of several of the gallia polymorphs have resisted characterisation until our recent work that highlighted how structural disorder is common in the various forms of Ga$_2$O$_3$. All samples of $\gamma$-Ga$_2$O$_3$
described in the literature have been produced by solution methods, since thermal treatment readily leads to collapse to the thermodynamically stable $\beta$-Ga$_2$O$_3$.\textsuperscript{32,33,34,35,36} These synthesis routes tend to produce small particles, which then introduces further complications in structural investigation, since Bragg diffraction peaks are broadened and surface structure may become significant. Indeed until our recent work, in which we performed Rietveld refinement of the structure against powder neutron diffraction data,\textsuperscript{31} only the cubic unit cell parameter of $\gamma$-Ga$_2$O$_3$ had been reported.\textsuperscript{1} Our Rietveld analysis of this material revealed a defective spinel structure ($Fd\overline{3}m$, $a = 8.23760(9)$ Å) with gallium distributed over four sites: the expected tetrahedral 8a and octahedral 16d sites and additional tetrahedral 48f and octahedral 16c sites,\textsuperscript{31} similar to found in $\gamma$-Al$_2$O$_3$, found from single-crystal X-ray diffraction.\textsuperscript{37} The refined octahedral:tetrahedral ratio is 1.35:1 for this crystalline $\gamma$-Ga$_2$O$_3$, compared to 1.70:1 for $\gamma$-Al$_2$O$_3$. The refined average structure does not, however, describe the distribution of gallium atoms, since this cannot be completely random as physically implausible Ga---Ga distances ($< 2.4$ Å) would result from the occupation of the 48f and 16c sites adjacent to the ideal spinel 8a and 16d sites. Furthermore, the local environment of gallium within the octahedral sites is likely to be asymmetrical, if the structures of $\alpha$-Ga$_2$O$_3$\textsuperscript{38} and $\beta$-Ga$_2$O$_3$\textsuperscript{39} are considered, both of which have been refined from single crystal diffraction. These discrepancies between average and local structure were not resolved in our previous work, where we used pair distribution function (PDF) analysis to refine the crystal structure; it proved impossible to fit the local structure of $\gamma$-Ga$_2$O$_3$ with the average model, though the medium-to-long range structure was very well described. In this paper we consider the structure of $\gamma$-Ga$_2$O$_3$ in detail; first by using a reverse Monte Carlo (RMC) refinement technique to obtain an atomistic model consistent with both local and average structure of a moderately crystalline sample, and then by examining two samples with smaller crystallite sizes, where we use neutron total scattering and solid-state NMR spectroscopy in conjunction
with traditional diffraction analysis to develop a consistent picture of the structure of the material.

**Experimental**

Three samples of $\gamma$-Ga$_2$O$_3$ were prepared. The first (‘crystalline’) was formed by the solvothermal oxidation of metallic gallium, based on the method of Kim *et al.*, but optimised to give the most crystalline product at lower temperatures. 0.3 g of Ga (Aldrich 99.99%) and 5 ml of monoethanolamine (Aldrich ≥99.0%) were placed in a Teflon-lined stainless steel autoclave which was sealed and transferred to a pre-heated fan oven at 240 °C for 72 hours. The solid product was dispersed into 10 ml of hot methanol, recovered by suction filtration, washed with further methanol and dried at 70 °C overnight. The second sample (‘nanocrystalline’) was prepared using a shorter time: 0.3 g of Ga (Aldrich 99.99%) and approximately 5 ml of diethanolamine (Aldrich ≥ 98.5%) were placed in a Teflon-lined stainless steel autoclave which was sealed and transferred to a pre-heated fan oven at 240 °C for 11 hours. The reaction product, a fine white powder suspended in a viscous solvent, was dispersed into 15 ml of methanol, passed through a coarse filter to separate any pieces of unreacted gallium and then isolated and washed with methanol via centrifugation, before being dried at 70 °C overnight. The third sample was prepared using an aqueous route, similar to that of Areán *et al.* Gallium nitrate hydrate (3 g, Aldrich 99.9% metals basis) was dissolved in ethanol (50 ml) and concentrated aqueous ammonia, diluted 50% v/v with ethanol, was added to achieve a pH of 9.0. The resulting precipitate was immediately filtered, washed with ethanol and dried at 70 °C for 12 hours before being calcined at 500 °C in air for 1 hour.

For comparison, samples of $\alpha$-Ga$_2$O$_3$ and $\beta$-Ga$_2$O$_3$ were also prepared. $\alpha$-Ga$_2$O$_3$ was synthesised in two stages, using a procedure similar to those reported by Lavalley *et al.* and Hou *et al.* Gallium nitrate hydrate (3.0 g, Aldrich, 99.9% metals basis) was dissolved in
distilled water (50 ml), and concentrated aqueous ammonia, diluted 50% v/v with distilled water, was added until no further precipitation was observed. The solution was left to stand overnight, then a fine white precipitate was collected by vacuum filtration, washed with water and acetone and dried at 70 °C overnight. This GaO(OH) product was heated at 500 °C for 4 hours to yield phase-pure α-Ga₂O₃. A reference sample of β-Ga₂O₃ was obtained by heating gallium nitrate hydrate at 220 °C in air for 18 hours, followed by re-grinding and heating the product at 800 °C in air for 22 hours.

Preliminary sample assessment was made using powder X-ray diffraction: patterns were recorded using a Siemens D5000 X-ray diffractometer operating with CuKα radiation. Infra-red spectra were recorded from the solid samples using a Perkin-Elmer Spectrum100 diamond ATR-FTIR spectrometer. Thermogravimetric analysis was performed using a Mettler Toledo TGA/DSC1 instrument. Approximately 10 mg of powder were loaded into an alumina crucible; the sample was heated in air to 1000°C at a rate of 10°C min⁻¹. Transmission electron microscopy (TEM) measurements were made using a JEOL 2100 LaB₆ instrument, operating at 200 kV on specimens that were dispersed by ultrasound in ethanol and dropped onto 3 mm lacey carbon grids supplied by Agar.

Neutron total scattering experiments were performed using the instrument GEM at ISIS, the UK spallation neutron source. Each of the three samples of γ-Ga₂O₃ (~ 2 g) was separately loaded into vanadium cans with inner diameter 7.62 mm. Data were accumulated for approximately 5 hours to ensure they were of good statistical quality. Data were also collected from an empty vanadium can, the empty instrument and a vanadium rod for normalisation purposes. Three banks of Bragg scattering data from GEM were analysed simultaneously using the GSAS suite of software, visualised with EXPGUI. Total neutron scattering data analysis was performed by normalisation of four banks of GEM data and merging them to produce the distinct scattering, \( i(Q) (Q_{\text{max}} = 32 \text{ Å}^{-1}) \) using the GudrunN and
ATLAS\textsuperscript{46} softwares. Fourier transformation of \(i(Q)\), using a Lorch modification function, \(M(Q)\),\textsuperscript{47} to reduce the effect of termination ripples, yielded the differential correlation function \(D(r)\), Equation (1).

\[
D(r) = \frac{2}{\pi} \int_0^{Q_{\text{max}}} Qi(Q) M(Q) \sin rQ \, dQ
\]  

Equation (1)

The function \(D(r)\) is hereafter referred to as the pair distribution function (PDF). The program RMCPProfile was used for reverse Monte Carlo modelling.\textsuperscript{48} Datasets used for RMC refinements were the \(i(Q)\) as mentioned above, and the total correlation function \(T(r)\) (Equation 3). Fitting was carried out to the \(T(r)\) as the \(r\) weighting allows the medium range data to be fitted more accurately, whereas \(G(r)\) is used for post-refinement visualisation of the low-\(r\) region. For RMC the Fourier transform was carried out without the use of the Lorch function. The region of the correlation functions below \(r = 1.7\) Å, which contained only nonphysical noise, was excluded from the RMC fit.

\[
G(r) = \frac{D(r)}{4\pi r \rho_0}
\]  

Equation (2)

\[
T(r) = 4\pi r \rho_0 \left[ G(r) + \left( \sum_{i=1}^{n} c_i \bar{b}_i \right)^2 \right]
\]  

Equation (3)

In these equations, \(\rho_0\) is the number density and \(c_i\) and \(b_i\) are the concentration and the neutron scattering length of the \(i\)th atom, respectively.

\(\text{\(^{71}\)}\text{Ga}\) solid-state NMR spectra were acquired at a magnetic field strength of 20.0 T. Samples were packed into 1.3 mm rotors and rotated at a MAS rate of 60 kHz. A spin echo was used to ensure undistorted lineshapes were acquired, with an echo duration, \(\tau\), of two rotor periods (33.33 \(\mu\)s) for \(\alpha\)- and \(\beta\)-Ga\(_2\)O\(_3\) and one rotor period (16.67 \(\mu\)s) for \(\gamma\)-Ga\(_2\)O\(_3\). Owing to the width of the lineshapes, high-power pulses (\(~125\) kHz radiofrequency nutation rate), of 1 and 2 \(\mu\)s for the first and second pulses, respectively, rather than central-transition selective pulses, were employed. For \(\gamma\)-Ga\(_2\)O\(_3\), the spectra were recorded with high-power
pulses (~200 kHz radiofrequency nutation rate) of 0.6 and 1.3 µs for the first and second pulses, respectively. While typically the first pulse must have a short flip angle in order to achieve (approximately) quantitative NMR spectra of quadrupolar nuclei, no significant variation in the relative intensity ratios of the tetrahedral, Ga(IV), and octahedral, Ga(VI), resonances was observed with increasing pulse length, whereas the overall signal was most intense with the pulse lengths used. Signal averaging was carried out for 2240 (α-Ga₂O₃), 7760 (β-Ga₂O₃) or 2048 (γ-Ga₂O₃) transients with a recycle interval of 3 s (α and β-Ga₂O₃) or 1 s (γ-Ga₂O₃).

Results

First we consider in detail the structure of the sample of ‘crystalline’ γ-Ga₂O₃ prepared by the extended solvothermal oxidation of gallium metal. To obtain a model consistent with the distinct features of the average structure as well as the local scale disorder, we have used a reverse Monte Carlo (RMC) approach. Initially, a 5 × 5 × 5 supercell of the crystal structure obtained from Rietveld refinement was created, and then, with each crystallographically distinct Ga site being treated separately, the correct proportion of “occupied” and “vacant” sites were created at random. This random distribution of atoms inevitably produces some unphysically short Ga-Ga correlations, and so the RMCPProfile software was used to swap pairs of atoms and vacancies to reduce the number that violated a “minimum distance” constraint. During this process, no translational moves were allowed and no data were being fitted. Unfortunately, a point of stagnation, where no further swaps could be made, was always reached prior to all the unphysical correlations being removed. Therefore, an alternative strategy to build a starting configuration was sought. First, gallium atoms and vacancies were manually arranged in a 2 × 2 × 2 supercell of the crystal structure such that there were no unphysical Ga-Ga distances. This configuration was then tripled to produce a
6 × 6 × 6 supercell containing ~25,000 atoms for input into RMCProfile. The configuration thus produced contained artificial superstructure which caused extra peaks in the Bragg diffraction profile (Supporting Information); an atom-swapping procedure, driven by fitting to the Bragg profile, was therefore used to re-randomise the atomic arrangement. Since no translational moves were permitted, only swaps that reduced the intensity of the spurious superstructure peaks improved the fit. In this manner, 20 different starting configurations were produced. For the full RMC refinements, each was duplicated 10 times, resulting in a total of 200 refined configurations per set. All refinements involved fitting to both the \(i(Q)\) and the \(T(r)\), with one set also including the Bragg profile as an additional dataset. During refinement, the four crystallographic Ga sites were not segregated so as to avoid overly biasing the result toward the crystal structure. Instead a bond valence sum constraint was used to keep the coordination environment of each Ga physically reasonable. A distance window constraint requiring atom pairs to remain within a window specified by an appropriate minimum and maximum distance, was also used. Representative fits obtained after a run time of 72 hours (after which time equilibrium was reached) can be seen in Figure 1. It should be noted that including or excluding the Bragg data had no visible effect on the quality of the fits to \(T(r)\) and \(i(Q)\) (Supporting Information). As can be seen in Figure 1, the fits to the total scattering data in both real and reciprocal space are excellent. Of particular note is the good agreement in the low-\(r\) region of the \(T(r)\), as this region is poorly described by the average structural model. To illustrate directly the relationship between the refined atomic configuration and the average starting structure, the supercell was folded back onto the original unit cell, Figure 2. The “clouds” of atoms in these illustrations represent the distribution of atoms around the average positions, and indeed for \(\gamma\)-Ga\(_2\)O\(_3\) their centroids map directly back onto the coordinates of the crystallographic sites. Including the Bragg data in the refinements reduced the spread of the atom clouds, and indeed a comparison of
calculated Bragg profiles (Supporting Information) shows that the model obtained is more appropriate for the average structure while, as we have already seen, being no less accurate for the local. All subsequent discussion therefore refers to the refinements that included Bragg data.

The Ga-O partial correlation functions for each different crystallographic site are shown in Figure 3. The pronounced asymmetry of the Ga_{16d}-O partial function shows that the [GaO6] octahedra are, on a local scale, distorted from cubic symmetry. Despite its small overall contribution to the total, the Ga_{16c}-O function is physically reasonable in shape and breadth (see Supporting Information), largely due to the application of the bond valence constraint. The summed Ga-Ga partial function, compared with that calculated from the average structure is shown in Figure 4. There are no unphysically short correlations and the peaks at 2.9 and 3.5 Å are slightly shifted and better defined in the RMC model with non-statistical distribution of site occupation. Partial pair distribution functions for all possible combinations of pairs of unique Ga sites confirm that the main discrepancy when the Ga sites are statistically occupied is indeed in the unphysical short distance region, but also that some other discrepancies concerned with Ga-Ga distances are removed by allowing the local symmetry to relax (Supporting Information).

The mean Ga-O bond lengths for each site were calculated for each refined configuration, and compared with the Rietveld averages (Table 1). The values are very similar and vary little from one refinement to the next. However, within each configuration the standard deviation in bond lengths is significantly larger for the octahedral sites than for the tetrahedral, indicating a greater degree of disorder in the 6-coordinate sites. Distributions of O-Ga-O bond angles were calculated from 100 refined configurations and summed (Figure 5). For the ideal spinel sites, the distributions are symmetrical and centred upon the Rietveld
values, but for the 48f tetrahedral site (which is rather distorted in the average structure) the
distribution has relaxed towards the ideal tetrahedral angle of 109.5°.

The polyhedral units in the refined configurations were further analysed and
categorised in terms of number of bonds longer or shorter than average. Surprisingly, some
trends in polyhedra ‘type’ were observed. For the tetrahedral sites, the majority (~52%) were
of the 2+2 type (i.e., having two shorter and two longer bonds). For the octahedral sites, the
majority had all 6 bonds shorter than average (54%), which is not surprising considering the
skewness of the bond length distribution. The next most common type was found to be 3+3
type (38%), which is a significant observation given that the crystal structures of both α-
Ga₂O₃ and β-Ga₂O₃ contain [GaO₆] sites of this type exclusively. RMC analysis therefore
provides direct evidence for the similarity in local structure between metastable cubic γ-Ga₂O₃
and the thermodynamically stable monoclinic β-Ga₂O₃.

Having obtained a detailed structural model for the crystalline γ-Ga₂O₃ sample, we
now consider the two materials prepared as smaller crystallites. Figure 6 shows TEM images
of three samples. The most crystalline sample, Figure 6b, has a morphology that resembles
that reported by Kim et al. who used the same synthesis method¹⁸ and high magnification
images, Figure 6c, show individual particles to be made of agglomerates of plate-like primary
crystallites, of typically ~ 30 nm in maximum dimension. The ‘nanocrystalline’ sample,
prepared using a short solvothermal reaction, also is formed from the same plate-like
crystallites, Figure 6f, but the agglomerates are smaller (10 – 15 nm in dimension) and less
rough compared the more crystalline sample, Figure 6e. The ‘disordered’ sample, prepared
from ethanolic solution shows smaller particles, Figure 6h, and apparently also formed from
primary, plate-like crystallites, as the other two samples, Figure 6i, despite the different
synthesis method. Electron diffraction measured from the particles shows polycrystalline
rings, which can be indexed using the expected face-centred cubic unit cell, Figures 6a, 6d
and 6g. Figure 7 shows neutron Bragg scattering of the three samples. Shorter solvothermal oxidation reactions yield a sample with a broadened diffraction profile, Figure 7b, consistent with the smaller crystallite size seen by TEM, but all Bragg peaks can clearly still be resolved. In contrast, the sample prepared by the aqueous precipitation method shows a considerably more broadened profile, Figure 7c, with the effect of small crystallite size much more apparent. Scherrer analysis of the diffraction profiles gave average crystallite sizes of 30 nm, 15 nm and 5 nm for the ‘crystalline’, ‘nanocrystalline’, and ‘disordered’ samples, respectively. A closer inspection of the Bragg scattering shows systematic changes in relative peak intensities in addition to the broadening of the profile, Figure 7d. Rietveld analysis of the nanocrystalline sample, Figures 7e and 7f, using the model for the crystalline sample as a starting point shows reveals that the lattice parameter is slightly smaller ($a = 8.2240(2)$ Å $\text{cf. } a = 8.23760(9)$ Å for the crystalline sample) and, more obviously, that the site occupancies are different, Table 2: the total ratio of octahedral to tetrahedral gallium is 1.14:1 for this material ($\text{cf. } 1.35:1$ for the more crystalline sample), showing a greater number of tetrahedral sites are occupied, and, furthermore that the number of non-standard spinel sites has increased: the ratio of spinel to non-spinel sites is 1.94:1, compared to 5:1 in crystalline $\gamma$-Ga$_2$O$_3$. Any attempt made to fit the diffraction profile without changing the site occupancies from the original crystal structure, and instead adding additional parameters like anisotropic thermal displacements, was unsuccessful.

The diffraction profile from the disordered sample made via precipitation proved impossible to fit meaningfully using Rietveld analysis, and the high background of the data may be due to incoherent scattering from a hydrogeneous contaminant material, such as surface-bound solvent. Furthermore the apparent shift in the position of the (222) Bragg peak cannot be accounted for by the $\gamma$-Ga$_2$O$_3$ phase, and may be caused by overlap with a broadened peak from a poorly crystalline impurity. Nevertheless, using the idea of an increase
in tetrahedral relative to octahedral site occupancy with decreasing crystallite size (as seen for the previous sample) the Bragg peak intensities of the neutron diffraction pattern can be well matched using a modified spinel structure with an octahedral:tetrahedral ratio of 0.82 : 1 and a spinel:non spinel ratio of 0.51:1 which suggests that the trend seen going from crystalline to nanocrystalline solvothermal $\gamma$-Ga$_2$O$_3$ (i.e. an increase in the amount of tetrahedral gallium and increased occupancy of non-spinel sites) continues as the particle size further decreases in the precipitated sample; this model is summarised in Table 3 and shown in Figure 8 where the simulated scattering function is compared with the observed.

The pair distribution functions of the nanocrystalline and disordered samples of $\gamma$-Ga$_2$O$_3$ show clear evidence of decreasing particle size, with an obvious dampening with increasing radial distance, Figure 9a. In the case of the nanocrystalline, solvothermal sample, the low $r$ region exhibits a strong peak at $\sim$1.5 Å that can be assigned to C-C or C=N bonds from residual solvent molecules (expected at 1.51 and 1.47 Å, respectively), Figure 9b; this is confirmed by IR spectroscopy and thermogravimetric analysis (Supporting Information), and we suggest that this is surface-bound solvent. The sample from ethanolic precipitation shows a hydrogenous background in the neutron scattering, as noted above, and a larger proportion of surface water and/or hydroxide seen by TGA. The presence of secondary phases, which may in fact simply be surface-bound species, in both of these materials precludes the use of RMC analysis to analyse fully their structures. Nevertheless, an important observation from the comparison of the PDFs from all three samples is that the average Ga-O distance is invariant (Figure 9b). It should be noted that the peak at $\sim$2 Å in the PDF is a combination of all close Ga-O distances and the shorter tetrahedral and longer octahedral distances cannot be resolved. The observation that the average Ga-O coordination is unchanged on reducing particle size is apparently inconsistent with the analysis of the Bragg scattering, but in fact highlights the different views of the sample obtained from the different techniques. If the
entirety of a sample volume is crystalline, then both Bragg diffraction and total scattering analyses should obtain the same fundamental structural parameters, such as average coordination number. If, however, a significant region of the sample is not crystalline, such as for small particles for which the surface becomes more significant, this is no longer the case. The Ga-O coordination observed in the PDF includes all Ga-O pairs in the sample, including those in disordered regions, such as the crystallite surfaces.

The $^{71}$Ga NMR spectra of the three samples of $\gamma$-Ga$_2$O$_3$, shown in Figure 10, provide clear evidence of the disordered nature of the material, as all resonances observed display significant additional broadening (rather than the characteristic second-order quadrupolar lineshapes observed for the more ordered $\alpha$- and $\beta$- polymorphs of Ga$_2$O$_3$, shown in Figures 8d and e), with asymmetric upfield “tails” indicative of a distribution of quadrupolar and chemical shift parameters. Indeed, even with the high B$_0$ field strength (20.0 T) and rapid MAS (60 kHz) used for this work, the isotropic tetrahedral and octahedral resonances remain slightly overlapped, although they are well separated from the first spinning sidebands. It is interesting to note that, although O’Dell et al. observed an increase in the disorder-related line broadening with decreasing particle size (down to ~20 nm) for $\beta$-Ga$_2$O$_3$, no such trend was observed here, most likely owing to the smaller particle size regime investigated and the inherently more disordered nature of $\gamma$-Ga$_2$O$_3$. The extent of the overlap of the resonances means that it was not possible to observe the distinct types of tetrahedral and octahedral Ga directly in the MAS spectra. However, from spectra recorded using short flip angles, ensuring that (approximate) quantification of the overall tetrahedral:octahedral ratio was possible, values of 1:1.8, 1:1.8 and 1:2.1 were obtained for the crystalline, nanocrystalline and disordered samples of $\gamma$-Ga$_2$O$_3$, respectively. This result is consistent with the PDF analysis, which showed that the average Ga coordination environment does not change significantly between the three different particle sizes.
Discussion

Our RMC analysis of $\gamma$-$\text{Ga}_2\text{O}_3$ reveals structural complexity in an apparently simple material, including pronounced local-scale deviation from the cubic average structure, and provides detailed information about the distribution of bond lengths and angles: information which is lacking from a crystallographic analysis alone. The structural model obtained using RMC is consistent with results from $^{71}\text{Ga}$ NMR which show heavily broadened resonances that can be assigned to mixtures of more than one type of both octahedral and tetrahedral Ga sites of non-ideal local symmetry. The effect of decreasing particle size apparently reduces the proportion of octahedral Ga sites compared to tetrahedral within the crystalline volume of the particles, as evidenced by Bragg scattering, but this must be compensated for by an increase in octahedral gallium since both the pair distribution functions and solid-state NMR show a invariant octahedral:tetrahedral gallium ratio. A likely explanation is that an increased number of surface Ga sites is present for the sample of smaller particle size, and these have different environment than the bulk. The surface chemistry of $\gamma$-$\text{Ga}_2\text{O}_3$ has received some consideration previously, owing to its relevance in catalysis applications, but our work is the first to examine structure directly using diffraction methods. In a series of papers by Areán and co-workers a similarity between the surface chemistry of $\gamma$-$\text{Ga}_2\text{O}_3$ and $\alpha$-$\text{Ga}_2\text{O}_3$ was noted, and by using IR spectroscopy with probe molecules such as CO and pyridine showed the presence of strong Lewis acid sites. Similar effects were seen for $\gamma$-$\text{Ga}_2\text{O}_3$-$\gamma$-$\text{Al}_2\text{O}_3$ solid. The consensus was reached from these IR studies that coordinatively unsaturated, tetrahedral gallium sites at the surface were responsible for the strong binding of Lewis bases, including for $\alpha$-$\text{Ga}_2\text{O}_3$ whose bulk crystal structure contains only octahedral gallium. It is important to note that in these IR experiments the samples were heated for several hours under dynamic vacuum (typically 673 K, $10^{-4}$ Torr), thus any pre-existing, surface-bound
solvent or hydroxide will undoubtedly have been removed to ‘activate’ the surface. For our materials, studied in an ‘as made’ state, from solution synthesis, the surface will have associated solvent, water or hydroxide and so is most likely to be terminated as octahedral gallium, consistent with the picture we see by considering the results of all techniques applied.

**Conclusions**

Structural investigation of an apparently simple binary oxide has been made possible using several advanced structural probes, both diffraction-based and spectroscopic, which in combination provide a model for the non-statistical occupation of partially filled metal sites, and the balance of bulk vs surface metal sites. While Rietveld refinement shows that in $\gamma$-Ga$_2$O$_3$ the Ga occupies two pairs of octahedral and tetrahedral sites (ideal spinel and non-spinel), it provides no information about their local distribution, which cannot be statistical owing to the short Ga--Ga contacts produced if simultaneous occupation of neighbouring ideal spinel and non-spinel sites occurs. Thus refinement against neutron total scattering data using a reverse Monte Carlo (RMC) approach was used to produce a model that accounts for the local and long-range structure, but this also reveals significant local distortion in the octahedral sites that resembles the structure of thermodynamically stable polymorph of the same composition, $\beta$-Ga$_2$O$_3$. For nanocrystalline samples of the same material analysis of the relative Bragg peak intensities reveals evidence for a greater proportion of tetrahedral vs octahedral sites. In contrast, neutron total scattering shows an invariant average Ga-O distance with particle size, itself consistent with $^{71}$Ga solid-state NMR that indicates that all samples contain the same overall proportion of octahedral:tetrahedral Ga. It is therefore proposed that increased occupation of tetrahedral sites within the smaller crystallites is matched by an increased proportion of octahedral surface Ga sites, most likely due to termination by bound
solvent or hydroxide. This new insight into the inherent disorder of the structure and how it is
affected by crystallite size provides new information to further understand the $\text{Ga}_2\text{O}_3$ system,
of importance given the recent interest in the catalytic and electronic properties of gallium
oxides.

Supporting Information
Further details of Reverse Monte Carlo analysis of crystalline $\gamma$-$\text{Ga}_2\text{O}_3$ and general
classification data from all samples (TGA-DSC, IR and TEM). This material is available
free of charge via the Internet at http://pubs.acs.org.

Acknowledgements
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equipment used in materials characterisation at the University of Warwick was obtained
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Generation Advanced Materials" with support from Advantage West Midlands (AWM) and
part funded by the European Regional Development Fund (ERDF). The UK 850 MHz solid-
state NMR Facility used in this research was funded by EPSRC and BBSRC, as well as the
University of Warwick. Computing resources were provided by STFC's e-Science facility.
Table 1: Comparison of mean bond lengths obtained from RMC refinements with those from Rietveld analysis for crystalline γ-Ga$_2$O$_3$.

<table>
<thead>
<tr>
<th></th>
<th>RMC bond length / Å</th>
<th>Rietveld bond length / Å</th>
<th>Difference / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ga 8a</td>
<td>1.8705(3)</td>
<td>1.8578</td>
<td>0.69</td>
</tr>
<tr>
<td>Ga 16d</td>
<td>2.0064(2)</td>
<td>2.0174</td>
<td>-0.55</td>
</tr>
<tr>
<td>Ga 48f</td>
<td>1.8553(3)</td>
<td>1.7874</td>
<td>3.80</td>
</tr>
<tr>
<td>Ga 16c</td>
<td>2.015(1)</td>
<td>2.1032</td>
<td>-4.18</td>
</tr>
</tbody>
</table>

Table 2: Crystal parameters from nanocrystalline, solvothermal γ-Ga$_2$O$_3$. Space group $Fd\overline{3}m$, $a = 8.2240(2)$ Å. Rp = 0.66%, wRp = 0.92%. The italic values in square brackets are those for the crystalline, solvothermal material.

<table>
<thead>
<tr>
<th>Atom</th>
<th>Wyckoff site</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>$U_{iso}$ / Å$^2$</th>
<th>Occupancy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ga1</td>
<td>8a</td>
<td>0.125</td>
<td>0.125</td>
<td>0.125</td>
<td>0.0129(2)</td>
<td>0.54(2) [0.741(8)]</td>
</tr>
<tr>
<td>Ga2</td>
<td>16d</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
<td>0.0129(2)</td>
<td>0.610(7) [0.741(3)]</td>
</tr>
<tr>
<td>Ga3</td>
<td>48f</td>
<td>0.348(1)</td>
<td>0.125</td>
<td>0.125</td>
<td>0.0129(2)</td>
<td>0.118(3) [0.066(1)]</td>
</tr>
<tr>
<td>Ga4</td>
<td>16c</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.0129(2)</td>
<td>0.100(6) [0.024(1)]</td>
</tr>
<tr>
<td>O</td>
<td>32e</td>
<td>0.251(3)</td>
<td>0.251(3)</td>
<td>0.251(3)</td>
<td>0.0135(1)</td>
<td>1</td>
</tr>
</tbody>
</table>

Table 3: The modified spinel model used to describe disordered γ-Ga$_2$O$_3$ made by the ethanolic precipitation method.

<table>
<thead>
<tr>
<th>Atom</th>
<th>$Fd\overline{3}m$ site</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>Occupancy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ga1</td>
<td>8a</td>
<td>1/8</td>
<td>1/8</td>
<td>1/8</td>
<td>0.3</td>
</tr>
<tr>
<td>Ga2</td>
<td>8b</td>
<td>3/8</td>
<td>3/8</td>
<td>3/8</td>
<td>0.3</td>
</tr>
<tr>
<td>Ga3</td>
<td>16d</td>
<td>1/2</td>
<td>1/2</td>
<td>1/2</td>
<td>0.3</td>
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<tr>
<td>Ga4</td>
<td>16c</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.3</td>
</tr>
<tr>
<td>Ga5</td>
<td>48f</td>
<td>0.3679</td>
<td>1/8</td>
<td>1/8</td>
<td>0.1445</td>
</tr>
<tr>
<td>O</td>
<td>32e</td>
<td>0.2552</td>
<td>0.2552</td>
<td>0.2552</td>
<td>1</td>
</tr>
</tbody>
</table>
Figure Captions

Figure 1: Representative final fits to neutron total scattering data from crystalline, solvothermal $\gamma$-Ga$_2$O$_3$ using RMC analysis: (a) fit to $F(Q)$, (b) fit to $T(r)$ and (c) expanded view of fit to $T(r)$ showing satisfactory resolution of local structure, compared with the $T(r)$ calculated from the ideal cubic structure.

Figure 2: A group of 10 RMC refined configurations collapsed back onto the original unit cell, for the refinements without Bragg data (a) and with Bragg data (b). A projection of the crystal structure is shown in (c) for comparison. Red spheres are Ga atoms on octahedral sites, blue are Ga on tetrahedral sites.

Figure 3: Partial PDFs of crystalline, solvothermal $\gamma$-Ga$_2$O$_3$; measured data are points and the lines are those simulated from a set of 10 refined RMC configurations. The Ga-O correlations for each crystallographic site are shown in (a) while, for clarity, the sum of these is shown in (b).

Figure 4: Comparison of Ga-Ga partials from Rietveld and RMC structural models. The unphysically short correlations in the average structure are clearly visible at $r < 2.0$ Å.

Figure 5: Comparison of O-Ga-O bond angles in the average structural model with the distributions of bond angles in the RMC configurations. $B(\theta)$ is the bond angle distribution function and the division by $\sin \theta$ accounts for the geometric factor when calculating bond angles. Distributions were calculated from 100 refined configurations and summed. Plots are for (a) 8a, (b) 16d, (c) 48f and (d) 16c sites, respectively.

Figure 5: TEM of $\gamma$-Ga$_2$O$_3$ samples: top row is electron diffraction indexed using the F-cubic unit cell seen by neutron diffraction and middle and bottom rows are images at two magnifications from (a)-(c) crystalline $\gamma$-Ga$_2$O$_3$, (d)-(f) nanocrystalline $\gamma$-Ga$_2$O$_3$ and (g)-(i) disordered $\gamma$-Ga$_2$O$_3$.

Figure 6: Neutron Bragg scattering from for the three samples of $\gamma$-Ga$_2$O$_3$ (a) crystalline solvothermal sample (b) nanocrystalline solvothermal sample and (c) poorly crystalline precipitated sample. (d) Shows an expanded region highlighting changes in relative Bragg peak intensity, while (e) and (f) show a Rietveld fit of the profile for the nanocrystalline solvothermal sample for two banks of GEM data.

Figure 7: A comparison of the neutron $\langle Q \rangle$ from (a) disordered $\gamma$-Ga$_2$O$_3$ with (b) the $\langle Q \rangle$ simulated for the modified spinel model, adjusted for small particle size using a Mason factor.

Figure 8: PDFs of the three $\gamma$-Ga$_2$O$_3$ materials (a) showing the effect of decreasing particle size on the damping of the function, (b) the low-r region showing the contaminant C-C / C-N peak at ~1.5 Å in the ~15 nm solvothermal sample and the invariant Ga-O interatomic distance.

Figure 9: 1D 71Ga (20.0 T, 60 kHZ MAS) NMR spectra of (a) crystalline $\gamma$-Ga$_2$O$_3$, (b) nanocrystalline $\gamma$-Ga$_2$O$_3$, (c) disordered $\gamma$-Ga$_2$O$_3$, (d) a-Ga$_2$O$_3$, and (e) b-Ga$_2$O$_3$. Asterisks denote spinning sidebands and, in part (d), † denotes a Ga tetrahedral resonance assigned to surface reconstruction, and Ga(IV) and Ga(VI) denote tetrahedral and octahedral gallium, respectively.

References


(24) Yuan, Y. P.; Du, W. M.; Qian, X. F. Zn$_x$Ga$_{2-3x}$O$_3$ (0 $\leq$ x $\leq$ 1) Solid Solution Nanocrystals: Tunable Composition and Optical Properties \textit{J. Mater. Chem.} \textbf{2012}, \textit{22}, 653-659.


82x175mm (300 x 300 DPI)
Ga(VI)  
Ga(IV)  

400  200  0  -200  -400  
δ (ppm)