Photoionising feedback and the star formation rates in galaxies

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Received 10 July 2013 / Accepted 11 October 2014

ABSTRACT

Aims. We investigate the effects of ionising photons on accretion and stellar mass growth in a young star forming region, using a Monte Carlo radiation transfer code coupled to a smoothed particle hydrodynamics (SPH) simulation.

Methods. We introduce the framework with which we correct stellar cluster masses for the effects of photoionising (PI) feedback and compare to the results of a full photoionisation hydrodynamics code.

Results. We present results of our simulations of star formation in the spiral arm of a disk galaxy, including the effects of photoionising radiation from high mass stars. We find that PI feedback reduces the total mass accreted onto stellar clusters by ≈23% over the course of the simulation and reduces the number of high mass clusters, as well as the maximum mass attained by a stellar cluster. Mean star formation rates (SFRs) drop from \( \frac{\text{SFR}_{\text{unadjusted}}}{\text{SFR}_{\text{unadjusted}}} = 4.2 \times 10^{-2} \ M_\odot \text{yr}^{-1} \) to \( \frac{\text{SFR}_{\text{MCPI}}}{\text{SFR}_{\text{MCPI}}} = 3.2 \times 10^{-2} \ M_\odot \text{yr}^{-1} \) after the inclusion of PI feedback with a final instantaneous SFR reduction of 62%. The overall cluster mass distribution appears to be affected little by PI feedback.

Conclusions. We compare our results to the observed extra-galactic Schmidt-Kennicutt relation and the observed properties of local star forming regions in the Milky Way and find that internal photoionising (PI) feedback is unlikely to reduce SFRs by more than a factor of ≈2 and thus may play only a minor role in regulating star formation.

Key words. HII regions – radiative transfer – stars: massive

1. Introduction

Feedback from young massive stars can have a significant impact on their environment on scales of tens of au to several kpc (Hollenbach et al. 2000; Franco et al. 1994; Tenorio-Tagle 1979; Whitworth 1979), and is often invoked to regulate star formation rates (SFRs) in galaxies. The emission of high frequency photoionising photons into the surrounding neutral gas can act to unbind the gas and disrupt ongoing star formation. On small scales the action of PI photons from the central star is a principal mechanism for the dispersal of circumstellar disks around massive stars (Hollenbach et al. 2000; Bally et al. 1998). In dense cluster environments the photoevaporation by an external source can cause the destruction of circumstellar disks, even around low mass stars, if the cluster is large enough to host an O or B star.

It is thought that a large fraction of stars form in clusters embedded within molecular clouds rather than in isolation (Lada et al. 1991; Lada & Lada 2003) and so the action of massive stars can strongly affect the growth and evolution of other cluster members. In the case where ionised gas becomes unbound and escapes from the cluster, then it can lead to the complete disruption of the stellar cluster (Hills 1980; Baumgardt & Kroupa 2007; Goodwin & Bastian 2006).

In addition to limiting the ability of stars to accrete neutral gas, the influence of ionised gas can also promote the formation of new stars. This may be due to the “collect and collapse” mechanism in which neutral gas is swept up by the advancing ionisation front and forms unstable clumps that undergo collapse and form stars (Whitworth et al. 1994; Elmegreen & Lada 1977; Dale et al. 2007a). Alternatively additional star formation may be caused by the radiatively driven implosion of pre-existing stable gas clumps that exist in the structure of the undisturbed molecular cloud (Kessel-Deynet & Burkert 2003; Bisbas et al. 2011).

It has been shown by previous authors (Dale et al. 2005; Dale & Bonnell 2011; Krumholz et al. 2005) that the underlying structure of the neutral gas in which an ionising source is embedded will have a strong influence on the propagation of ionising photons. If the source is accreting from high density accretion flows, then these will strongly inhibit the flow of PI photons in certain directions and effectively shield portions of the surrounding medium from the direct effects of the source. The ionising photons will escape more easily into the low density cavities of the surrounding gas, and the accretion flows can remain mostly neutral.

Smoothed particle hydrodynamics (SPH) provides a useful method to follow the evolution of a molecular cloud where large contrasts in gas densities are present. The Lagrangian nature of SPH codes also helps in following the evolution of self-gravitating flows, but traditional methods for evaluating the transfer of radiation in such environments are often best suited to Eulerian schemes, where the optical depth can be more simply integrated along directions of photon travel. Several authors have implemented radiation transfer methods in SPH simulations to treat PI radiation (Dale et al. 2005, 2007b; Gritschneder et al. 2009; Kessel-Deynet & Burkert 2000). While methods exist to implement radiation transfer in SPH codes, many simulations still neglect such effects for the sake of computational speed and complexity.

We have used a Monte Carlo photoionisation (MCPI) code to calculate the ionisation structure for a series of static, independent snapshots of the SPH simulation. We do not re-run the SPH simulation but instead use the MCPI code to estimate which of the SPH particles become photoionised by young stars and remove their contribution to future star formation. There is no
additional computational overhead during the SPH simulation as all photoionisation calculations are performed once the simulation is completed. In this way we are able to characterise the reduction in SFRs and efficiency caused directly by PI feedback. The aim of this work is to provide an estimate of the first order effects of feedback from PI radiation. We first test our method against a full ionisation hydrodynamic simulation before applying it to star formation in a galactic spiral arm.

2. SPH simulations

We begin our investigation with the star formation simulations of Bonnell et al. (2013). These are designed to track the small scale star formation processes as well as the large scale evolution of the interstellar medium on galactic scales. Three simulations were carried out by Bonnell et al. (2013). Firstly a global disk simulation of a $5-10$ kpc annulus of material within a galactic disk was evolved for $370$ Myr. Cooling in the spiral shocks produced a complex, multiphase interstellar medium in which dense clouds reminiscent of the molecular clouds seen within our own galaxy formed. To follow the star formation process within such dense clouds a second high resolution run was then carried out, the Cloud simulation. This followed the formation of one dense cloud at higher resolution than the initial global simulation. Finally, the Gravity simulation added the effects of self-gravity and allowed the dense cloud to form stars from the realistic initial conditions provided by the Cloud simulation. The Gravity simulation contains $1.29 \times 10^7$ SPH particles with each particle having a mass of $0.15$ $M_\odot$. The formation of stars was treated with the use of sink particles (Bate et al. 1995). Due to the prescription of the formation of a sink particle which requires a minimum of 70 particles we are only able to resolve the gravitational collapse to a mass of $11 M_\odot$. This is too high to represent low mass star formation and each sink should instead be thought of as a stellar cluster. The results from Bonnell et al. (2013) based on the Gravity simulation suggest that the observed Schmidt-Kennicutt (Schmidt 1963; Kennicutt 1998) power law relation between star formation rate and gas surface density can be explained by the combination of spiral shocks and gas cooling rates. However, the star formation rates produced by the simulation are higher than those observed.

We start our investigation with the Gravity simulation. The dense cloud it represents is approximately 250 pc in size and contains $\approx 1.7 \times 10^6 M_\odot$ of gas. We assume that no prior star formation has occurred in the cloud or its surroundings during its previous evolution. The star formation and evolution of the cloud is traced for $\approx 5$ Myr. Beyond this point it is likely that supernovae within the cloud will quickly act to disperse it, ending most star formation. We assume that all gas forming or accreting onto a sink particle is retained by the sink and that none is recycled back into the simulation by feedback on the scale of the small clusters represented by the sinks. Star formation efficiencies are unlikely to be this high and evidence suggests that they are in the region $25-50\%$ (Ostriker & Tremaine 2002) which would lead to our star formation rates being upper limits by a factor 2–4.

During the time evolution of the Gravity simulation the properties of each SPH particle (position, velocity etc.) are printed out to file at several points. It is on these outputs that we base our analysis regarding the effects of photoionisation on the star formation process.

3. Monte Carlo photoionisation code

In order to calculate the photoionisation of the gas throughout the star forming region during its evolution we use a MCPI code described in Wood & Loeb (2000) and extended by Wood et al. (2010). The routines can be used to calculate the hydrogen-only photoionisation and have been modified to allow the use of SPH data as initial input. The Monte Carlo treatment of the radiation transfer is fully 3D and can easily treat the complex geometries encountered within the gas distribution.

All ionising photons encounter an average opacity which is given by $n_H \bar{\sigma} + n_{dust} \sigma_{dust}$, where $n_H$ is the number density of neutral hydrogen, $\bar{\sigma}$ is the flux averaged cross section and $\sigma_{dust}$ gives the dust cross section per hydrogen atom (i.e. cm$^{-2}$ H$^{-1}$). Two different flux averaged cross sections are considered depending on whether a photon has been emitted directly by an ionising source (direct photon) or is the product of absorption and subsequent reemission (diffuse photon). The cross section for direct photons is averaged over the flux

$$\bar{\sigma} = \frac{\int_0^\nu F \sigma_\nu \, d\nu}{\int F \, d\nu},$$

where $F$ is the source ionising spectrum, $\nu_0$ is the frequency of the Lyman edge and $\sigma$ is the absorption cross-section for Hydrogen. In the case of the diffuse ionising spectrum the photon energies are strongly peaked at just above 13.6 eV and so we set the cross section for the diffuse photons to the hydrogen cross-section just above 13.6 eV, $\bar{\sigma} = 6.2 \times 10^{-18}$ cm$^{-2}$. This simplification means that essentially only two frequencies are considered and greatly speeds the computation of the ionisation fractions throughout the grid.

As an output of the photoionisation code we have a grid containing the neutral fraction ($f_n$) which gives the fraction of the mass in each grid cell which is neutral, with the remainder being ionised. In order to apply our MCPI routines to the SPH data it is necessary to discretise the SPH density estimate across a cartesian grid. In this case each SPH simulation dump is discretised onto a 200$^3$ grid of cells. For the Gravity simulation we centre the grid on the centre of mass of the system and have the grid extend to $\pm 0.1$ kpc in all three axes, to fully encompass the central region of the cloud with sufficient resolution. This results in
a 1 pc resolution for the MCPI simulations. We found that an increased resolution (a 2^3 increase in grid cells) has little impact on the results (of order a 1 per cent change in the ionised gas mass) of the MCPI code, but adds significantly to the time required for each simulation.

3.1. Ionising photon numbers

To estimate the positions and locations of ionising sources within the molecular cloud we create a list of all stellar sink particles in the simulation along with their locations. Due to the limited mass resolution of the simulations each sink particle represents a stellar cluster in this case. The number of photons able to ionise hydrogen produced each second by each stellar cluster is represented by the $Q_H$ value. Following the method of Dale & Bonnell (2011) we assign a $Q_H$ to clusters that exceed 600 $M_\odot$ by calculating the total mass in stars $M > 30 M_\odot$ and dividing this mass by 30 $M_\odot$. This gives an approximate measure of the number of 30 $M_\odot$ stars, $N_{30}$. To estimate $Q_H$ for a 30 $M_\odot$ O-star we fit the data of Conti et al. (2008; Table 3.1) and Diaz-Miller et al. (1998; Table 1) to find a relation between the stellar mass and number of ionising photons. From this we estimate that the number of ionising photons produced by a 30 $M_\odot$ star will be $Q_H = 2.8 \times 10^{48}$ s\(^{-1}\).

We assume a Salpeter IMF with upper and lower mass limits of 100 $M_\odot$ and 0.1 $M_\odot$. The use of a Salpeter IMF slope down to 0.1 $M_\odot$ is an overestimate of the total mass in low mass stars as the true IMF should turn over near 0.5 $M_\odot$ (Kroupa et al. 1993). This will lead to lower estimates for the mass in stars $>30 M_\odot$, but is likely offset by our assumption of 100 per cent star formation efficiency. We performed a test simulation using a two-part Kroupa IMF (Kroupa 2001) and included mean values of $Q_H$ from stochastic sampling. The ionising fluxes in this case was typically a factor of 2 higher than given by our regular estimate, but this increase is less than that due to our assumed 100 per cent star formation efficiency, which likely overestimates the total stellar mass by a factor 2–4. Dale et al. (2012a) find that uncertainties in the ionising fluxes of factors of a few have little impact in the ionised gas mass. We can reasonably conclude that these simulations are likely to encompass the maximum impact of photoionising feedback. It is possible that the stochastic sampling of the IMF could result in significantly larger fluxes at low cluster masses in rare cases with a high-mass star in isolation or in a low-mass cluster. We do not consider such cases here.

4. Coupling the MCPI to SPH simulations

As the time evolution of the SPH simulation we are investigating has previously been completed and did not include the effects of photoionisation, it is necessary to approximate the feedback effects as well as possible without rerunning the simulation itself. By linking our MCPI codes to the individual time dumps of the SPH code we hope to investigate the effects that photoionisation by young stars can have on the mass accretion rates during the course of the simulation. To accomplish this we have included a series of checks on each SPH gas particle, that are carried out at each SPH time dump in the simulation.

We initially begin at the point in the simulation where at least one stellar sink has a mass $\geq$600 $M_\odot$, as this will provide the first source of ionising photons as described in Sect. 3. We then run our MCPI code using as inputs the SPH density discretised into a cartesian grid and the positions and $Q_H$ values for the stellar clusters. The output of the the MCPI code is a grid containing the hydrogen ionisation fraction throughout the star forming region at the time-step of interest.

Once the MCPI code has computed the ionisation fraction within the grid we identify the SPH particles that are located within ionised cells. If a gas phase SPH particle is located in a cell with an neutral fraction ($f_n$) $< 0.5$ then it is classified as an ionised particle. We have found that in general the results we obtain are relatively insensitive to the exact value of $f_n$ at which particles are classified as ionised, as the mass of ionised particles is dominated by SPH particles that are almost fully ionised ($f_n < 0.1$).

We adjust the accretion rates by removing any mass accreted from an “ionised” SPH particle as such gas should no longer be gravitationally bound to the accreting sink. The stellar cluster masses are recalculated by removing an amount of mass from the sink equal to the mass of the ionised particle multiplied by (1 $-$ $f_n$). In this way if an accreted ionised particle was found in a cell with $f_n = 0.4$ then 60% of its mass would be prevented from accreting onto the stellar sink. Ionised gas is assumed to escape the simulation and be no longer available for star formation. This means that the ionisation fraction cannot decrease. In testing this approach, we found that few particles ever returned to a neutral status as once they are exposed to the ionising radiation, they did not re-enter a shadowed region in these simulations. We also test for the ionisation of the SPH particles that are used to initially form stellar sinks. If, when a sink particle is formed, more that 50% of the gas particles that took part in its formation were classified as ionised, then the sink will be removed from further calculations and assumed not to form.

This method allows us to investigate the effects of ionisation feedback on the accretion onto stellar clusters as the simulation progresses and compare the results with the initial distributions that do not include any effects of photoionisation by massive stars.

It is important to note that no dynamical effects of the photoionisation are included. Thus the pressure from the hot gas onto the surrounding environment is ignored as is the reduction of gravitational acceleration from the reduced sink masses in the simulation. The gravitational and pressure forces which were used to determine the dynamics are entirely due to the non-ionising runs with higher sink masses and fully neutral gas. This is an unfortunate but unavoidable effect of our approach and therefore we have first compared this approach to the full dynamical ionisation simulations from Dale et al. (2012). The fact that we are able to largely replicate the Dale results (see below) has allowed us to proceed with this approach with a high level of confidence in the results.

5. Validity of the method

In order to assess how well the methodology we have adopted is able to estimate the effects of ionisation feedback on the growth of stellar mass in our simulations we have performed tests against the simulations of Dale et al. (2012; hereafter referred to as D12). We have used the results from the run A and run I simulations from D12 in order to test the effectiveness of our treatment under differing conditions and their properties are summarised in Table 1. Run A has the largest radius of the simulations to form any stars in D12 and shows diffuse structure. It contains a few tens of clusters, with a number that are massive enough to become sources of ionising photons. Run I is physically much smaller and more compact than run A and possesses the lowest escape velocity of any of the simulations investigated.
The MCPI tends to overestimate the effective change in the stellar mass. Where the SFR in D12 increases significantly with a corresponding simulation, with the exception of the final few timesteps the data agree between the two methods at most times and formed over the course of the run A and run I simulations in the course of the simulation. By the end of the run the data method.

Table 1. Properties of the simulations from D12 used to test the MCPI method.

<table>
<thead>
<tr>
<th>Run</th>
<th>Mass ($M_\odot$)</th>
<th>Radius (pc)</th>
<th>$\delta_{\text{LSC}}$ (kms$^{-1}$)</th>
<th>$\langle n(H_2) \rangle$ (cm$^{-3}$)</th>
<th>$t_{\text{f}}$ (Myr)</th>
<th>$T$ (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>$10^6$</td>
<td>180</td>
<td>5.0</td>
<td>2.9</td>
<td>19.6</td>
<td>143</td>
</tr>
<tr>
<td>I</td>
<td>$10^4$</td>
<td>10</td>
<td>2.1</td>
<td>136</td>
<td>2.56</td>
<td>53</td>
</tr>
</tbody>
</table>

In run I the mass resolution is sufficient to consider the sink particles that form as individual stars and so we can directly estimate number of ionising photons produced from the stellar mass. We adopt the same method as D12 to calculate the $Q_{\text{H}}$ values in run I and assign any sink that exceeds 20 $M_\odot$ a number of ionising photons according to the relation:

$$\log(Q_{\text{H}}) = 48.1 + 0.02(M_\star - 20 M_\odot),$$  \hspace{2cm} (2)

where $M_\star$ is the stellar mass. In run A we adopt the standard relation between cluster mass and number of ionising photons from Sect. 3.1.

For both run A and I we have access to the control simulations, which included no ionisation effects (hereby referred to as the control runs), and also the simulations including the effects of ionisation. We apply our methods to the control runs and compare the results to the simulations which explicitly included ionisation. In this way, we can assess how important the dynamics of the ionised gas are, which we cannot follow in our MCPI method.

For run A we have an excellent agreement between our calculations and D12 over most of the time covered by the simulation. The integrated SFR, calculated from the total stellar mass formed during the simulation is $SFR_{\text{control}} = 3.6 \times 10^{-3} M_\odot$ yr$^{-1}$ in the control and drops to $SFR_{\text{Dale}} = 2.8 \times 10^{-3} M_\odot$ yr$^{-1}$ and $SFR_{\text{MCPI}} = 2.5 \times 10^{-3} M_\odot$ yr$^{-1}$ in the D12 and MCPI simulation respectively.

For run I the integrated SFR for the control is $SFR_{\text{control}} = 1.1 \times 10^{-4} M_\odot$ yr$^{-1}$ and drops to $SFR_{\text{Dale}} = 7.1 \times 10^{-5} M_\odot$ yr$^{-1}$ for the D12 simulation and $SFR_{\text{MCPI}} = 5.7 \times 10^{-5} M_\odot$ yr$^{-1}$ in the MCPI run.

5.1. Cumulative stellar mass

In Figs. 2 and 3 we present the cumulative stellar sink mass formed over the course of the run A and run I simulations in the control, D12 and MCPI implementations. In run A we have a good agreement between the two methods at most times and the difference in the stellar mass is less than 5% for the majority of the simulation, with the exception of the final few timesteps where the SFR in D12 increases significantly with a corresponding change in the stellar mass.

The results from run I are also in reasonable agreement. The MCPI tends to overestimate the effects of feedback at all times with a steady divergence of the stellar sink masses over the course of the simulation. By the end of the run the difference is around 20%. Again the difficulties of the MCPI method in correctly treating sink runs are not unexpected due to the strong dynamical influence of the ionised gas.

The fact that the MCPI results are in reasonable agreement with the more sophisticated D12 treatment gives us encouragement that we are able to treat the ionisation feedback on stellar growth in a satisfactory way. It should also be noted that mostly the MCPI method predicts a SFR that is equal to or lower than D12. The MCPI treatment can then be interpreted as providing an upper limit to the effects of ionising feedback by only allowing it to reduce the SFRs and not accounting for the possible triggering of star formation.

6. Results

In Fig. 4 we plot the time evolution of the ionised gas mass and ionising luminosity as calculated by the MCPI simulation at each timestep from our SPH simulation. The total ionising luminosity grows steadily throughout the simulation from $0.29 - 6.6 \times 10^{49}$ s$^{-1}$ as the sink particles accrete more mass. Each step in the ionising luminosity represents a new sink particle (or particles) exceeding the minimum mass required to become an ionising source. The decrease in ionising luminosity at ~354.3 Myr is due to an ionising source exiting the region of interest. In our work the ionised gas mass is representative of the total number of SPH gas particles, present in each timestep, which have been ionised and therefore excluded from any subsequent star formation. The ionised gas mass shows an initial fast growth as the first ionising sources appear, followed by a modest, steady growth as the simulation progresses. As each MCPI simulation is independent, the ionised gas mass can decrease in time due to the exact distribution of sources and neutral gas in each case. It can also decrease if any ionised gas is subsequently an upper limit to the effects of ionising feedback by only allowing it to reduce the SFRs and not accounting for the possible triggering of star formation.
Figure 4 shows the distribution of the ionised gas particles at the first time step containing an ionising source (left panel) and sources is low density, di-
gas which has been ionised at large distances from the ionising
sections of the plot (\( y > 0 \)). It can be seen that
the shielding from the high density gas in the central region of
the cloud, preventing the propagation of ionising photons in this
direction. This has the effect that the low-level of star formation
in the upper region \( (y > 0) \) is largely unaffected by the PI photons.
Figure 5 shows the neutral
gas surface density at the corresponding times. It can be seen that
even in the early stages of PI feedback the ionising photons are
able to affect a large region of the cloud. However, much of the
gas which has been ionised at large distances from the ionising
sources is low density, diffuse gas, that is not currently actively
star forming. The cloud is the Gravity simulation \( \rho \) is a large region of the cloud, with highly ionised
regions within the dense inner core of the cloud close to the most
massive ionising sources. The region of the cloud in the upper
section of the plot \((y > 0)\) is largely unaffected by the PI photons.
This is due to a reduced star formation rate in this region and in
the shielding from the high density gas in the central region of
the cloud, preventing the propagation of ionising photons in this
direction. This has the effect that the low-level of star formation
in the upper region \((y > 0)\) is largely unaffected by PI feedback
from the massive clusters near the cloud centre.

In Fig. 7 we show the cumulative mass which has been
accreted onto the stellar sink particles as a function of time from
the point at which the first ionising source forms until the end of
the simulation. It can be seen that there is a steady divergence
of the standard and photoionised cases due to the ionisation of
gas particles, any accretion of which is discounted in our pho-
toionisation models. We stress that this is simply a reduction in
the estimate of the mass in sinks and the corresponding star for-
mation rates. The actual dynamics are unaffected as they were
calculated in our control, non-ionising SPH simulation. We find
that, in total, after our inclusion of photoionisation effects the fi-
nal mass accreted by all sinks falls from \( M_{\text{control}} = 2.2 \times 10^5 M_\odot \)
to \( M_{\text{MCPI}} \approx 1.7 \times 10^5 M_\odot \) which is a reduction in the stellar mass
of \( \approx 23\% \).

We estimate the mean SFR over the course of the simulation
for both runs by taking the total mass formed by the end of the
simulation and dividing by the total time for the Gravity simu-
lation. In the control run we achieve \( SFR_{\text{control}} = 0.042 M_\odot \text{ yr}^{-1} \),
while in the case including photoionisation the rate drops to
\( SFR_{\text{MCPI}} \approx 0.032 M_\odot \text{ yr}^{-1} \). This change is due to feedback from
ionising sources which have previously formed, ionising gas be-
fore it can be accreted onto stellar sinks or from new sinks.

The effect of the PI feedback on the SFR appears to increase as
the simulation progresses. The upper panel in Fig. 8 shows
the calculated SFR for the control and MCPI simulations and
the lower panel shows the fractional difference between the two.
Initially, before the formation of any ionising sources, both have
identical SFRs. There is an immediate drop in the MCPI SFR
compared to the control run as soon as the first massive clusters
form followed by a period where the reduction in SFR due to
PI feedback is around 5%. The last \( \approx 2 \) Myr show a steady and
generally gradual increase in the effects of PI feedback on the
SFR. By the end of the simulation the SFR in the MCPI run is
62% of that in the control run.

Figure 9 shows a cumulative histogram of the final stellar
sink masses for both the standard and photoionised simulations.
It shows the total numbers of sinks formed by the end of each
simulation as a function of their mass. It can be seen that fewer
sinks have formed in the photoionised case compared to the stan-
dard case but both follow a similar distribution. The most obvi-
ous change in the sink mass distribution takes place at the high
mass end where there are a lower number of sinks due to the
action of PI feedback. The effects of photoionisation are to re-
duce the accretion rates and also the maximum mass attained by
a sink during the evolution of the system. In the standard case
sinks are allowed to grow freely, accreting gas without the effect
of feedback in this case we end up with several sinks with
masses \( > 1000 M_\odot \) and the highest sink mass of 1968 \( M_\odot \). In
the photoionised simulation the highest mass sink is 1154 \( M_\odot \)
and fewer of the sinks grow in excess of 600 \( M_\odot \). Here the effects of
feedback have prevented the sinks accreting gas as it becomes
ionised before its accretion and effectively reduces the source of
gas available to the high mass clusters.

6.1. Additional simulations
In addition to the case outlined above we have also investigated
the effects of PI feedback on two analogous simulations but with
mean surface densities ten times larger \( (40 M_\odot \text{ pc}^{-2}) \) and ten
times smaller \( (0.4 M_\odot \text{ pc}^{-2}) \) than the standard case. These sim-
ulations were produced by adapting the SPH particle masses
and the highest sink mass of 1968 \( M_\odot \). In
the photoionised simulation the highest mass sink is 1154 \( M_\odot \)
and fewer of the sinks grow in excess of 600 \( M_\odot \). Here the effects of
feedback have prevented the sinks accreting gas as it becomes
ionised before its accretion and effectively reduces the source of
gas available to the high mass clusters.

In these simulations we have no sources of PI photons as defined
(see Bonnell et al. 2013 for more details). In the ab-
ence of photoionising feedback, the three simulations combine
to reproduce a Schmidt-Kennicutt star formation relation but at a
higher level than is observed. The low surface density simulation
suffers from a lack of star formation due to a more limited reser-
voir of gas available for accretion and a lack of dense clumps
where the gas can cool efficiently (Bonnell et al. 2013). This
results in a much reduced star formation rate and a lack of high
mass sinks within the SPH simulation. With no sinks greater in
mass than \( \approx 75 M_\odot \) we have no sources of PI photons as defined
in Sect. 3 and so are unable to follow the possible effects upon
the star formation process.

The high surface density SPH simulation ran for a shortened
period of time due to the high densities producing prohibitively
short time-steps within the SPH code. However, a large number of sink particles were able to form and grow in mass until they became sources of PI photons. A total stellar mass of $2.54 \times 10^6 \, M_\odot$ forms in the control run within the $\approx 1.3$ Myr which the simulation was evolved for and this is reduced to $1.33 \times 10^6 \, M_\odot$ in the MCPI simulation. Even in this short timescale the PI photons are able to strongly affect the star formation in the region. Figure 10 shows the cumulative stellar mass in this case for the standard and photoionised cases. The mean star formation rate over the simulation falls from $SFR_{\text{control}} = 1.94 \, M_\odot \, \text{yr}^{-1}$ to $SFR_{\text{MCPI}} = 1.01 \, M_\odot \, \text{yr}^{-1}$. The sharp decrease in the star formation rate at a time of $\approx 351.6$ Myr appear to be caused by the coalescence of the ionised regions around several sources within the centre of the cloud to form one large ionised complex. This effectively ionises the majority of the gas near the sinks and removes the reservoir of star forming gas.

6.2. SFRs vs. surface density

In trying to understand the effects of PI feedback on the accretion processes it is useful to compare our results with the observed properties of star forming regions. It has been shown that there is a strong observed link between star formation and the local cold gas density (Schmidt 1963; Kennicutt 1998; Kennicutt & Evans 2012). In the case of disk averaged properties of local galaxies this can be fitted by a power-law relation of the form

$$\Sigma_{\text{SFR}} = A \Sigma_g^N,$$

where $\Sigma_{\text{SFR}}$ is the star formation surface density, $\Sigma_g$ the total cold gas mass density and the power-law slope $N$ has a value of $\approx 1.4$ (Kennicutt 1998). Observations of molecular clouds within our local environment in the Milky Way have suggested that the star formation surface density is a factor 10–20 higher than
Fig. 7. Total stellar mass is plotted as a function of time for the standard (red-solid) and photoionised (blue-dashed) simulation. The difference represents the mass of gas that is removed from the star formation process due to being photoionised.

Fig. 8. Star formation rates of the control and MCPI simulations as a function of time.

that predicted by the extragalactic relation (Evans et al. 2009; Heiderman et al. 2010).

Bonnell et al. (2013) found that in the original SPH simulations there was a relation between $\Sigma_{\text{SFR}}$ and $\Sigma_{\text{g}}$ with a power law index $N = 1.55 \pm 0.06$ (when the low ($0.4 M_\odot \text{ pc}^{-2}$) and high ($40 M_\odot \text{ pc}^{-2}$) surface density data is also included). The authors argue that the relation is a natural consequence of the shock formation of the dense, cold gas when cooling in the interstellar medium is included. In Fig. 11 we show the final instantaneous SFR and neutral gas mass surface density in our photoionisation simulation, as viewed along the three axes of our simulation grid. The contour lines and points show the effects of calculating the relationship within differing sized cells, from 5 pc to an average over the entire region. The values were calculated using grids of neutral gas density and SFR. Each grid was a $200^3$ cube of cells which we re-gridded to the required cell size before calculating the observed surface densities, as viewed along the three axes of the grid. In this way the entire cloud is covered at each resolution. The red contours show the data averaged over 5 pc cells with each contour enclosing a certain fraction of the data points, from 0.1 to 0.95. Only cells which contain a non-zero SFR have been plotted. We also show the observations of Heiderman et al. (2010) of local molecular clouds and YSO derived star formation rates, as well as the extra-galactic relation of Kennicutt (1998).

Firstly it can be seen by comparing the three figures that the orientation of the cloud can influence its observed properties. The center and lower panels show a similar distribution of properties when observed at small scales (red contours) due to the fact they are both observed from within the mid-plane. The upper panel shows an offset to lower neutral gas surface densities and this is due its being observed from above the galactic plane where perspective effects reduce the surface density observed for different regions. As we increase the cell size over which the properties are averaged we see that, in general, all three figure move into better agreement. We see many regions in our cloud which

Fig. 9. Final cumulative stellar mass distributions for the standard (red) and photoionised (blue) runs.

Fig. 10. Cumulative stellar mass as a function of time for the standard (red-solid) and photoionised (blue-dashed) simulation for the SPH simulation with a mean surface density of $40 M_\odot \text{ pc}^{-2}$.
Fig. 11. Surface densities of the star formation rates are plotted as a function of the surface densities of the neutral gas. The three panels represent the simulation as viewed along the three principle axes of the simulation grids. Crosses are observed data from Table 1 of Heiderman et al. (2010) with the extent of the cross indicating the confidence interval of the data. Coloured points (see key in top left) show the effects of increasing the cell size up to the size of the entire region (200 pc). The dashed line shows the observed extragalactic power-law relation from (Kennicutt 1998) and the blue line the power law fit achieved by Bonnell et al. (2013) to the Gravity simulation without PI feedback.

overlap with the observed data of Heiderman et al. (2010) as well as many which seem to lie at lower gas surface densities.

7. Discussion

From the results shown in Fig. 7 it is clear that the total mass accreted onto sinks throughout the simulation is overestimated by standard SPH methods when PI feedback is ignored. The final total stellar sink mass in the standard surface density simulation including photoionisation is reduced by around 23% and the instantaneous SFR is reduced to 62% of its original value at the end of the simulation. This is a significant change and suggests that it is likely very important to include photoionisation effects to accurately model the SFRs and efficiency within SPH simulations.

7.1. Limitations

The techniques outlined here provide a way to provide a first order approximation to the feedback provided by high mass stars. We neglect the dynamical effects of ionised gas that may provide additional forms of feedback due to the restrictions of our simulation.

7.1.1. Triggering of additional star formation

It has been suggested that the feedback from massive stars may act to trigger additional star formation under certain conditions. The expansion of the ionised HII region into surrounding neutral gas can sweep up a dense shell of material which can become self-gravitating (Whitworth et al. 1994; Elmegreen & Lada 1977; Dale et al. 2007a). Observationally it has proved difficult to definitively find evidence for triggered star formation surrounding massive stars but several authors have presented compelling arguments based on multiwavelength datasets (Deharveng et al. 2005; Dirienzo et al. 2007a). The extent to which these triggered star formation processes may counteract the reduction in star formation caused by the heating and ionisation of neutral gas is also unclear but
simulations suggest they are likely second order effects (Dale et al. 2012, 2013).

There are also additional mechanisms in which the dynamical effects of ionised gas can allow the PI feedback to have a greater effect than we estimate here. The penetration of the ionising photons into dense regions of gas can be increased due to the streaming of hot ionised gas out of the cloud. Whitworth (1979) and Gendelev & Krumholz (2011) explored this scenario and found that the removal of ionised gas allows the ionisation front to penetrate deeper into dense gas and may increase the effects of ionising photons beyond those discussed here.

In addition to assuming a 100% efficient star formation process the SPH simulation we have studied also neglect several physical processes which are likely to affect the overall star formation process. There is no treatment of magnetic fields which may cause a reduction in the star formation rate (Price & Bate 2008; Arthur et al. 2011; McKee 1999) by providing an additional support mechanism to overcome self-gravity and prevent the collapse of less massive clouds to form stars. Self gravity is also not included in the initial disk simulation from which our dense star forming region originates. This will lead to a reduced kinetic energy which, again, will influence star formation rates. The reduction in the star formation rates caused by the inclusion of such effects may provide a mechanism to move our simulated values into better agreement with observed relations.

We include no source of ionising photons outwith the bounds of our star forming cloud. In reality there will be a non zero background of ionising flux produced by previous bouts of star formation in the galactic disk. The effects of background far-ultraviolet heating are included in the SPH code (Vazquez Semadeni et al. 2006) but without account for the ionisation of the gas. Reynolds (1990) found that the diffuse ionised gas (DIG) in our local environment requires a diffuse ionising flux of \(4 \times 10^{-5}\) erg s\(^{-1}\) cm\(^{-2}\) to maintain it. This additional source of PI photons may be able to affect the outer regions of the cloud, but is unlikely to penetrate into the dense cloud centre. While this is unlikely to affect the star formation in the cloud interior it may impact the initial stages of cloud formation during compression within the spiral shock.

7.2. Localisation of stellar signatures

We find that the clumpy gas distribution produced by the SPH calculation produces a highly structured complex of HII regions which, due to low density paths, provides an illustration of a possible source of ionising photons required to maintain the DIG seen in the Milky Way and external galaxies. At the final step of the simulation our photoionisation code suggests that \(\approx 15\%\) of ionising photons escape into the ISM from this star forming complex. This escape fraction may also be important for observations of \(\text{H}_\alpha\) as a localised star formation indicator. If a significant fraction of the ionising photons are able to escape the star forming cloud then it also suggests there would be a corresponding drop in the \(\text{H}_\alpha\) luminosity. This effect will lead to \(\text{H}_\alpha\) emission that is non-coincident with the star formation. In turn this may cause deviations from the observed power law relation between star formation and gas surface densities at small scales (Relaño et al. 2012). Indeed Schruba et al. (2010) and Onodera et al. (2010) have found observational evidence of such deviations in high spatial resolution studies of the star formation in the nearby spiral galaxy M 33. Based on analysis of CO emission maps and \(\text{H}_\alpha\) imaging Schruba et al. (2010) estimate that the star formation law observed at large scales breaks down at scales below \(\sim 300\) pc. It is not possible to verify this effect here due to the size of the region studied.

In this work we have utilized a simple hydrogen only MCPI code but the method we propose can easily be extended to use radiation transfer codes which provide a more realistic treatment of the photoionisation physics (Wood et al. 2004; Ercolano et al. 2008). Our simplified treatment likely only provides a first order correction as it focuses on the ionisation of hydrogen and the impact of Lyman continuum photons only, neglecting the effects of Helium as a source of opacity. There is, however, no reason that more complex radiation transfer codes which includes these effects could not be added to provide more accurate gas physics at the cost of computation time. The possibility to also self-consistently include calculations of star formation indicators, such as \(\text{H}_\alpha\) and 24 \(\mu\)m dust emission would allow the direct comparison with observational data.

8. Summary

We have carried out an investigation into the effects of PI feedback from massive stars on the growth of stellar clusters in SPH simulations of a dense star forming region within a disk galaxy by utilizing post-completion MCPI calculations. In order to quantify the effects of PI photons we track SPH particles which are likely to be ionised during the course of the simulation and remove them from stellar sink particles where they have been accreted during the future evolution of the system.

Results indicate that the total stellar mass in sink particles may be reduced by up to \(23\%\) due to the action of PI photons emitted form the most massive stars. The final instantaneous SFR is reduced to 62\% of its original value. The overall distribution of sink particle masses does not seem to be greatly affected with the most noticeable changes occurring at the high mass end. The maximum sink mass attained is reduced and fewer massive stellar clusters form. As we cannot include the possible dynamical feedback effects of the hot ionised gas to trigger additional star formation our results provide an estimate of the maximum impact of PI feedback.

A comparison of our region-averaged properties to observed extra-galactic relations and observations of local molecular clouds suggests that our simulations over-predict the star formation rate by a factor 2–10. While the inclusion of PI feedback from massive stars is able to reduce the discrepancy between the simulation and observations it cannot fully account for it. We also find that a significant fraction of the PI photons emitted by massive stars in the simulation are able to traverse low density paths and escape the star formation region entirely. This provides a mechanism to produce a fraction of the DIG observed in many galaxies.

Acknowledgements. I.A.B. acknowledges funding from the European Research Council for the FP7 ERC advanced grant project ECOGAL. This research was also supported by the DFG cluster of excellence “Origin and Structure of the Universe” (JRG). This research has made use of NASA’s Astrophysics Data System Service.

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