THE WELL-ALIGNED ORBIT OF WASP-84b: EVIDENCE FOR DISK MIGRATION OF A HOT JUPITER*

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ABSTRACT

We report the sky-projected orbital obliquity (spin–orbit angle) of WASP-84b, a 0.69MJup planet in an 8.52 day orbit around a G9V/K0V star, to be $\lambda = -0.3 \pm 1.7^\circ$. We obtain a true obliquity of $\psi = 17.3 \pm 7.7^\circ$ from a measurement of the inclination of the stellar spin axis with respect to the sky plane. Due to the young age and the weak tidal forcing of the system, we suggest that the orbit of WASP-84b is unlikely to have both realigned and circularized from the misaligned and/or eccentric orbit likely to have arisen from high-eccentricity migration. Therefore we conclude that the planet probably migrated via interaction with the protoplanetary disk. This would make it the first “hot Jupiter” ($P < 10$ d) to have been shown to have migrated via this pathway. Further, we argue that the distribution of obliquities for planets orbiting cool stars ($T_{\text{eff}} < 6250$ K) suggests that high-eccentricity migration is an important pathway for the formation of short-orbit, giant planets.

Key words: planets and satellites: dynamical evolution and stability – planet–disk interactions – planets and satellites: individual (WASP-84b) – planet–star interactions – stars: individual (WASP-84)

1. INTRODUCTION

The orbital obliquity (spin–orbit angle; $\psi$) distribution of short-orbit, giant planets, or “hot Jupiters”, may be indicative of the manner in which they arrived in their current orbits from farther out, where they presumably formed (e.g., Rafikov 2006). As a star and its planet-forming disk both inherit their angular momenta from their parent molecular cloud, stellar spin and planetary orbital axes are expected to be, at least initially, aligned ($\psi = 0$). Migration via interaction with the gas disk is expected to preserve this initial spin–orbit alignment (Lin et al. 1996; Marzari & Nelson 2009). Migration via high-eccentricity migration, in which a cold Jupiter is perturbed into an eccentric, misaligned orbit that is then circularized, shortened, and realigned by tidal dissipation, is expected to produce a broad range of obliquities (Rasio & Ford 1996; Fabrycky & Tremaine 2007; Nagasawa et al. 2008; Matsumura et al. 2010; Naoz et al. 2011).

A broad range of obliquities has been found for hot-star systems ($T_{\text{eff}} > 6250$ K), for which tidal realignment is expected to be inefficient due to the absence of a substantial convective envelope (Winn et al. 2010a; Schlafman 2010), whereas systems with massive stars that had no convective envelope on the main sequence, but that are old enough to have developed convective envelopes ($\geq 2.5\text{Gyr}$), are aligned (Triaud 2011). Conversely, cool-star systems experiencing strong tidal forcing—that is, those with short scaled orbital distances, $a/R_*$, and high planet-to-star mass ratios—tend to be aligned (see Albrecht et al. 2012 and references therein). The obliquities of nine planets orbiting cool stars ($T_{\text{eff}} < 6250$ K) suggests that high-eccentricity migration is an important pathway for the formation of short-orbit, giant planets.

Various groups are attempting to reproduce the observed obliquity distribution with models (e.g., Naoz et al. 2012; Rogers & Lin 2013; Xue et al. 2014; Dawson 2014; Valsecchi & Rasio 2014). We require a larger sample of measured obliquities, especially for weak-tide, cool-star systems, and more realistic models to be able to discern the relative contribution of the different migration pathways and to better understand the physical processes involved in tidal dissipation and orbital realignment. Here we present an obliquity measurement for the weak-tide, cool-star system WASP-84 from observations of its Rossiter–McLaughlin (RM) effect (e.g., Albrecht et al. 2012). Anderson et al. (2014a, hereafter A14) found the WASP-84 system to comprise a 0.69MJup planet in a circular ($e < 0.077$ at $2\sigma$), 8.52 day orbit around an active K0V star.
2. OBSERVATIONS

We obtained 17 spectra of WASP-84 with HARPS on the ESO 3.6 m telescope (Pepe et al. 2002) through the transit of 2013 February 4–5 and a further 13 spectra around the orbit. The transit spectra, with exposure times of 1200 s, were taken over an airmass range of 1.39–1.17–1.92 and have signal-to-noise ratio (S/N) of 19–40 per pixel at 5500 Å. The seeing deteriorated to >2′ going into the transit, which reduced the flux entering the fiber. We chose to switch the read-out mode from fast to slow for the final six spectra, aiming for a higher precision at the expense of time resolution. The Moon, 31% illuminated and 115° from WASP-84, rose at the time of mid-transit. The spectra around the orbit had exposure times of 600 s, except for the final spectrum, for which the exposure time was 900 s.

We observed 38 spectra of WASP-84 with HARPS-North on the 3.6 m Telescopio Nazionale Galileo (Cosentino et al. 2012) through the transit of 2014 January 11–12. There was light cloud throughout the night, though it cleared during the latter portion of the sequence. At the time of mid-transit the Moon was 85% illuminated at a distance of 66° from WASP-84. We discarded the final five spectra as they were taken when the target was significantly beyond an airmass of 2 and the final spectrum was aborted. The remaining 33 spectra, each with an exposure time of 600 s, covered an airmass range of 1.27–1.12–2.06 and have S/N of 25–42 per pixel at 5500 Å.

We used the HARPS pipeline to process the HARPS and HARPS-North spectra and to compute radial velocities (RVs) by weighted cross-correlation with a numerical K5-spectral template (Pepe et al. 2005).

We observed WASP-84 during the same transit and from the same site as HARPS-North with the RISE photometer mounted on the 2 m Liverpool Telescope (Steele et al. 2008). RISE has a single fixed V + R filter, a field of view of 9/2 × 9/2 and zero read-out overhead. We defocussed the instrument and used autoguiding to minimize the effect of flat-fielding errors. We used an exposure time of 4 s to acquire 4236 images. Over the sequence the airmass of the target ranged over 1.12–1.80. We performed differential aperture photometry on the images using five comparison stars.

We plot the HARPS and HARPS-North RVs and the RISE photometry obtained through the transit in Figure 1 and all the RVs around the orbit in Figure 2. Time-correlated noise is evident in the early portion of the transit in both the HARPS and the HARPS-North RV sequences. Though this may have an astrophysical source, we suggest it results from a meteorological coincidence: the seeing deteriorated at the start of the transit observed by HARPS, which resulted in a drop in S/N, and the scatter in the HARPS-North RVs correlates well with the cloud visible in the Liverpool Telescope’s sky cameras.

3. STELLAR PARAMETERS FROM THE HARPS SPECTRA

We co-added the individual HARPS spectra to produce a single spectrum with an average S/N of 100:1. We performed the spectral analysis using the methods detailed in Doyle et al. (2013). The excitation balance of the Fe i lines was used to determine the effective temperature \( T_{\text{eff}} \). The surface gravity (log \( g_s \)) was determined from the ionization balance of Fe i and Fe ii and using the Na i D lines. The iron abundance was obtained from equivalent width measurements of 47 unblended Fe i and Fe ii lines. The quoted error estimates include that given by the uncertainties in \( T_{\text{eff}} \) and log \( g_s \), as well as the scatter due to measurement and atomic data uncertainties. The projected stellar rotation velocity \( v_{\text{rot}} \) was determined by fitting the profiles of several unblended Fe i lines in the wavelength range 6000–6200 Å. A value for macroturbulent velocity \( v_{\text{macroturb}} \) was assumed from the asteoseismic-based calibration of Doyle et al. (2014). Using those spectra with S/N > 20 and assuming \( B - V = 0.82 \), we determined the log \( R_{\text{HK}} \) activity index from the emission in the cores of the Ca ii H + K lines (e.g., Boisse et al. 2009). The results of the spectral analysis are given in Table 1.

4. OBLIQUITY AND SYSTEM PARAMETERS FROM THE HARPS RADIAL VELOCITIES AND THE RISE LIGHTCURVES

We determined the sky-projected obliquity and the system parameters from a simultaneous fit to the transit lightcurves and the radial velocities. The fit was performed using the current version of the Markov-chain Monte Carlo (MCMC) code described by Collier Cameron et al. (2007) and Anderson et al. (2014b). The RM effect was modeled using the formulation of Hinano et al. (2011b).

The available time-series photometries of WASP-84 are: the WASP lightcurves spanning 2009 January–2011 April (A14); a partial-transit lightcurve from TRAPPIST (A14); two full-transit lightcurves from RISE (A14); and a third RISE lightcurve (this paper). The available RV data are: 20 CORALIE RVs around the orbit, pre-whitened for stellar activity using a simple harmonic series (A14); and 13 HARPS spectra around the orbit, 17 HARPS spectra through a transit, and 38 HARPS-North spectra through a transit (this paper). Unlike with the CORALIE RVs, we found no reason to pre-whiten the HARPS orbital RVs: the Pearson correlation coefficient between residual RV and bisector span is \( r = -0.23 \) for the 13 RVs; this becomes \( r = 0.04 \) when excluding the latest RV, which was taken after the other 12 measurements. This compares with \( r = -0.71 \) for the 20 CORALIE RVs (A14). The star may have been quiescent during the HARPS observations around the orbit or it may have had an axisymmetric distribution of starspots, resulting in a weak activity signature.

In our final analysis we opted to determine the shape of the transit and the related physical properties using only the high-quality RISE transit lightcurves. We combined these with all the RVs, which were partitioned as listed above to allow for instrumental and astrophysical offsets. The excluded WASP photometries were imperfectly detrended for rotational modulation and instrumental noise and the excluded TRAPPIST photometry covers only the first half of the transit and was obtained at high airmass (1.47 at ingress to 2.40 at the end of the observation). However, as the WASP and TRAPPIST lightcurves significantly extend the baseline (from one year to five years), we wanted to use the timing information they contain to better constrain the orbital period. We did this by placing a normal prior on the time of mid-transit \( T_0 = 2456439.52878 \pm 0.00015 \) days, which was the \( T_0 \) from an initial analysis including all the listed data, but with an
The stellar density reported in A14 \((r^* = 2.02 \pm 0.07 \, \text{\sigma})\) seemed high for a star of the reported mass \(0.84 \pm 0.04 \, \text{\sigma}\). As a consistency check, we opted to determine stellar mass from a comparison with stellar models. We determined \(r^* = 1.851 \pm 0.049 \, \text{\sigma}\) from an initial analysis that omitted the WASP and TRAPPIST data. We input that value of \(r^*\) and the values of \(T_{\text{eff}}\) and \([\text{Fe/H}]\) from the spectral analysis into the BAGEMASS stellar evolution MCMC code of Maxted et al. (2014), from which we obtained a stellar mass of \(M^* = 0.855 \pm 0.028 \, \text{\sigma}\) and a stellar age of \(2.0 \pm 1.6 \, \text{Gyr}\).

In our final analysis, we adopted a circular orbit, which Anderson et al. (2012) advocate is the prudent choice for hot Jupiters in the absence of evidence to the contrary. In an initial analysis, in which we fit for eccentricity, \(e\), we found \(e = 0.018 \pm 0.011\) and \(<e<0.045\) at the 2\(\sigma\) level. The median values and the 1\(\sigma\) limits of our MCMC parameters’ posterior distributions are given in Table 1. The best fits to the radial velocities and the photometry are plotted in Figures 1 and 2. The presented solution supersedes that of the discovery paper owing to the additional RISE lightcurve and HARPS RVs, and the omission of the lower-quality WASP and TRAPPIST lightcurves.

We obtained \(\lambda = -0.3 \pm 1.7^\circ\) and \(v_a \sin I_a = 2.558 \pm 0.083 \, \text{km} \, \text{s}^{-1}\) when fitting the RM effect to both the HARPS-North and HARPS RVs. Unsurprisingly, the HARPS-North RVs, with both a cadence and a typical precision twice that of the HARPS RVs, do most to constrain the RM effect: we obtained \(\lambda = -1.2 \pm 1.7^\circ\) and \(v_a \sin I_a = 2.617 \pm 0.085 \, \text{km} \, \text{s}^{-1}\) when using only the HARPS-North RVs, and we obtained \(\lambda = 11.0 \pm 7.3^\circ\) and \(v_a \sin I_a = 1.96 \pm 0.31 \, \text{km} \, \text{s}^{-1}\) when using only the HARPS RVs. Primarily due to the omission of the WASP photometry, we obtained a lower stellar density as a result.
Table 1
System Parameters from the Spectral and the MCMC Analyses

<table>
<thead>
<tr>
<th>Parameter, Symbol / Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stellar effective temperature, $T_{\text{eff}}$ / K</td>
<td>5280 ± 80</td>
</tr>
<tr>
<td>Stellar surface gravity, log $g_*$ / (cgs)</td>
<td>4.65 ± 0.17</td>
</tr>
<tr>
<td>Stellar metallicity, [Fe/H]</td>
<td>0.09 ± 0.12</td>
</tr>
<tr>
<td>Microturbulence, $\xi_*$ / km s$^{-1}$</td>
<td>0.7 ± 0.3</td>
</tr>
<tr>
<td>Macro turbulence, $v_{\text{mac}}$ / km s$^{-1}$</td>
<td>2.13 ± 0.73</td>
</tr>
<tr>
<td>Proj. stellar rot. vel., $v_p\sin I_*$ / km s$^{-1}$</td>
<td>2.9 ± 0.8</td>
</tr>
<tr>
<td>Lithium abundance, log (A(Li))</td>
<td>&lt;0.7</td>
</tr>
<tr>
<td>Ca r H+K activity index, log $R'_{\text{HK}}$</td>
<td>−4.44</td>
</tr>
</tbody>
</table>

MCMC Proposal Parameters:

- Period, $P$ / d: 8.5234962 ± 0.0000037
- Mid-transit$^b$, $T_0$ / d: 6448.052286 ± 0.000069
- Transit duration, $T_{14}$ / d: 0.11537 ± 0.00038
- Transit depth, $\Delta F = R_2/R_1^2$: 0.01705 ± 0.00011
- Impact parameter, $b$: 0.6540 ± 0.0083
- Reflex velocity, $K_1$ / m s$^{-1}$: 75.9 ± 1.2
- Systemic velocity, $\gamma$ / m s$^{-1}$: −11.577 ± 1.5
- HARPS-North offset, $\gamma_{\text{off},\text{N,trans}}$ / m s$^{-1}$: −21.90 ± 0.37
- HARPS transit offset, $\gamma_{\text{off},\text{S,trans}}$ / m s$^{-1}$: 28.06 ± 0.21
- HARPS orbital offset, $\gamma_{\text{off},\text{S,orb}}$ / m s$^{-1}$: 13.729 ± 0.031
- $\sqrt{\chi^2} / \sin I_*$: 1.599 ± 0.026
- $\sqrt{\chi^2} / \sin I_* \sin \lambda$: −0.001 ± 0.048
- Eccentricity, $e$: 0 (adopted; <0.045 at 2 $\sigma$)

MCMC derived parameters:

- Projected orbital obliquity, $\lambda$ / $^\circ$: 0.3 ± 1.7
- Orbit obliquity$^c$, $\psi$ / $^\circ$: 17.3 ± 7.7
- Proj. stellar rot. vel., $v_p\sin I_*$ / km s$^{-1}$: 2.558 ± 0.083
- Stellar rotation velocity$^c$, $v_*$ / km s$^{-1}$: 2.70 ± 0.09
- Stellar spin inclination$^c$, $I_*$ / $^\circ$: 71.1 (67.6 ± 1 $\sigma$)
- Orbital inclination, $i_p$ / $^\circ$: 88.272 ± 0.037
- Scaled orbital separation, $a/R_*$: 21.69 ± 0.19
- Ingress/egress duration, $T_{12} (= T_{34})$ / d: 0.02185 ± 0.00048
- Stellar mass, $M_*$ / $M_\odot$: 0.853 ± 0.058
- Stellar radius, $R_*$ / $R_\odot$: 0.768 ± 0.019
- Stellar surface gravity, log $g_*$ / (cgs): 4.598 ± 0.012
- Stellar density, $\rho_*$ / $\rho_\odot$: 1.882 ± 0.049
- Planetary mass, $M_p$ / $M_{\text{ Jupiter}}$: 0.687 ± 0.033
- Planetary radius, $R_p$ / $R_{\text{ Jupiter}}$: 0.976 ± 0.025
- Planetary surface gravity, log $g_p$ / (cgs): 3.218 ± 0.012
- Planetary density, $\rho_p$ / $\rho_{\text{ Jupiter}}$: 0.741 ± 0.034
- Orbital major semi-axis, $a$ / au: 0.0775 ± 0.0017
- Orbital equatorial temperat., $T_{\text{ eq}}$ / K: 833 ± 13

$^a$ $v_{\text{mac}}$ value obtained using the calibration of Doyle et al. (2014).
$^b$ $T_0$ is in HJD (UTC) and 2,450,000 has been subtracted.
$^c$ See Section 5 for the calculation of $\psi$, $v_p$, and $I_*$.

compared to the discovery paper (1.88 ± 0.05 $\rho_\odot$ cf. 2.02 ± 0.07 $\rho_\odot$; A14).

5. RESULTS AND DISCUSSION

We find the sky-projected spin-orbit angle, or projected obliquity, of WASP-84b to be $\lambda = -0.3 \pm 1.7^\circ$. With a measurement of the angle between the stellar spin axis and the line of sight, $I_*$, we can calculate the true obliquity, $\psi$, using Equation (9) of Fabrycky & Winn (2009). Using the stellar rotation period of $P_{\text{rot}} = 14.36 \pm 0.35$ days, derived by A14 from observed photometric modulation, and our MCMC posterior distributions of $R_*$, $v_p\sin I_*$ and $\lambda$, we calculate $v_p = 2.70 \pm 0.09$ km s$^{-1}$, $I_0 = 71.1^\circ$ ($I_0 > 67.6^\circ$ at the 1$\sigma$ level), and $\psi = 17.3 \pm 7.7^\circ$; these are our adopted values. This is consistent with a well-aligned orbit and certainly excludes polar or retrograde orbits as observed for some other hot-Jupiter systems. We obtained consistent results from analyses using: only the HARPS-North RVs ($I_0 = 74.8^\circ$, $I_0 > 70.9^\circ$ at 1 $\sigma$; $\psi = 13.6 \pm 7.7^\circ$); only the HARPS RVs ($I_0 = 46.6^\circ$, $I_0 > 42.1^\circ$ at 1 $\sigma$; $\psi = 43 \pm 10^\circ$); all the RVs and the spectral $v_p\sin I_*$ ($I_0 = 90.0^\circ$, $I_0 > 68.7^\circ$ at 1 $\sigma$; $\psi = 3 \pm 18^\circ$). Using the relation between $P_{\text{rot}}$ and log $R'_{\text{HK}}$ of Mamajek & Hillenbrand (2008), we obtained $P_{\text{rot}} = 11.4 \pm 1.7$ days, which is consistent with the $P_{\text{rot}}$ from photometric modulation.

We found the orbital eccentricity of WASP-84-b to be low and consistent with a circular orbit: $e = 0.009^{+0.0017}_{-0.001}$ and $e < 0.045$ at the 2$\sigma$ level. Using the log $R'_{\text{HK}}$ age–activity relation of Mamajek & Hillenbrand (2008) we obtained an age of 0.70 ± 0.18 Gyr. This compares with our evolutionary analysis age of 2.1 ± 1.6 Gyr (Section 4) and the gyrochronological ages of 0.8 ± 0.1 and ~1.4 Gyr from A14. Using Equation (2) of Albrecht et al. (2012) we calculated the relative timescale for alignment via tidal dissipation to be $4.2 \times 10^{14}$ yr.

Considering the young age and the weak tidal forcing of the WASP-84 system, we suggest that it is improbable that the orbit of WASP-84b could have circularized and re-aligned from the eccentric, misaligned orbit likely to have arisen from migration via a high-eccentricity pathway. By requiring a circularization timescale of 1 Gyr, we used Equation 3 of Adams & Laughlin (2006) to calculate the maximal value of the planetary tidal quality factor, $Q_p$, of $4 \times 10^4$. This is far smaller than the value we obtained ($Q_p = 3 \times 10^7$) using equation (12) of Hansen (2010), which stems from an empirically calibrated model. Also, such a low $Q_p$ would imply a circularization timescale of only a few megayears for planets in short, eccentric orbits such as WASP-14b whose stellar age of a few hundred megayears suggests $Q_p > 10$ (Joshi et al. 2009). Therefore, we suggest that WASP-84b probably migrated to its current 8.52 day orbit via interaction with the protoplanetary disk. This would make it the first hot Jupiter to have been shown to have done so. Caution is warranted as tides are poorly understood (see Ogilvie 2014 for a review) and the larger radius of the planet during early times might have resulted in stronger tides, though a larger orbital distance would have acted oppositely. Alternatively, Petrovich (2014) argues that “coplanar high-eccentricity migration” could produce a planet in an aligned, circular orbit with the orbital separation of WASP-84b.

Another candidate hot Jupiter for disk migration is HAT-P-17b, which has a slightly larger scaled orbital distance ($a/R_*$ = 22.6 cf. 21.7) and a slightly smaller mass ratio ($M_p/M_\odot = 0.00059$ cf. 0.00077) than WASP-84b. Though HAT-P-17b may be aligned ($\lambda = 19 \pm 15^\circ$), Fulton et al. (2013) find that the data weakly favor a misaligned orbit. Further, the orbit is eccentric ($e = 0.342 \pm 0.006$) and the system is old (7.8 ± 3.3 Gyr; Howard et al. 2012). Thus the evidence for disk migration is less compelling.
Disk migration probably occurred in the Kepler-30 system (Sanchis-Ojeda et al. 2012), which is comprised of three planets in coplanar orbits that are aligned with the sky-projection of their star’s spin axis: Kepler-30b ($R_p = 3.9 \ R_\oplus; P = 29.3 \text{ days}$), Kepler-30c ($R_p = 12.3 \ R_\oplus; P = 60.3 \text{ days}$), and Kepler-30d ($R_p = 8.8 \ R_\oplus; P = 143.3 \text{ days}$). The 1:2 mean-motion resonance of Kepler-30b and the Uranus-mass planet, Kepler-30c, is suggestive of disk migration, though Kepler-30 is not a hot-Jupiter system.

6. THE DEPENDENCE OF ALIGNMENT ON ORBITAL DISTANCE

A broad range of obliquities has been found for hot-star systems ($T_{eff} > 6250 \text{ K}$), whereas cool-star systems tend to be aligned. This has been interpreted as evidence for realignment by tidal dissipation, which is suggested to be efficient for cool stars, which have deep convection layers, and inefficient for hot stars, which lack substantial convective envelopes (Winn et al. 2010a; Schlafman 2010). For viscous dissipation in a convective layer, the timescale for spin–orbit alignment is proportional to both the sixth power of the scaled orbital separation, ($a/R_\star$)$^6$, and the square of the star-to-planet mass ratio, ($M_*/M_p$)$^2$ (Zahn 1977). Thus, if hot Jupiters migrate via high-eccentricity pathways and realign via tidal dissipation, then, for cool stars, there should be a trend from spin–orbit alignment for close-in planets to a broad range of obliquities for those in more distant orbits.

We selected those cool-star systems with $T_{eff} \lesssim 6150 \text{ K}$ (to account for uncertainties) and with a mean uncertainty on $\lambda$ less than 20$^\circ$. Their spin–orbit angles are plotted in Figure 3, as a function of orbital distance in units of stellar radii $a/R_\star$, which is determined directly from the depth and width of the transit lightcurve (Seager & Mallén-Ornelas 2003). We see that $\lambda$ is confined to within $\sim 20^\circ$ of aligned orbit separations of $\lesssim 15 \text{ stellar radii}$ and that the distribution is broad at greater separations. No such pattern is observed for hot stars, which exhibit a broad distribution of $\lambda$ at $a/R_\star < 15$. This suggests that a high fraction of hot Jupiters orbiting cool stars used to be misaligned and that tides changed the initial distribution either by realigning the orbits or by destroying misaligned planets.

6.1. Giant-planet migration

As tides become ineffective with sufficient distance from the star, the population that we are beginning to see at $a/R_\star > 15$ may be close to the initial distribution in spin–orbit angle. We note that orbits shorter than $a/R_\star < 15$ are circular, whereas longer orbits are often eccentric (Figure 3). The misaligned and/or eccentric systems are suggestive of high-eccentricity migration and the aligned, circular system of WASP-84 is suggestive of disk-driven migration. Thus, both pathways appear to factor in the inward migration of giant planets; by measuring more systems in the weak-tide regime we can determine their relative contributions.

Figure 3. Projected obliquity, $\lambda$, of planetary orbital planes as a function of scaled orbital distance, $a/R_\star$, for those systems with $T_{eff} \lesssim 6150 \text{ K}$ and $\lambda < 20^\circ$. The filled symbols depict near-circular orbits ($e < 0.1$ or $e$ consistent with zero) and the open symbols depict eccentric orbits. WASP-84 b is depicted by a blue triangle. The planet at $a/R_\star \sim 23.7$ is HD 17156b, which has $e = 0.68$, and the planet at $a/R_\star \sim 22.6$ is HAT-P-17 b, which has $e = 0.342$ (Narita et al. 2009; Fulton et al. 2013). The planet at an $a/R_\star$ of $\sim 40$, Kepler-30 b, is not a hot Jupiter (Section 5).

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