

# Appendix C

## Supplementary movie captions

### C.1 Movies of quasi-geostrophic shallow-water simply-connected equilibria

Supplementary movies are available on the compact disc attached to this thesis in the folder SC.

**MOVIE SC1.** Examples of simply-connected vortex equilibria for  $\gamma=0.5, 3,$  and  $8$ . For each case we begin at the aspect ratio  $\lambda = 1$ , and end at the smallest aspect ratio attained,  $\lambda = \lambda_f$ . Here,  $|x|, |y| \leq 2.3$ . In this and subsequent movies we are in a frame of reference rotating with the equilibria.

**MOVIE SC2.** An example of type 2 instability, filamentation. We show the case  $\gamma = 0.5$  and  $\lambda_c = 0.296$ , for times between  $18.12T_p$  and  $45.31T_p$ . Note that  $|x|, |y| \leq 3.3$  in this and subsequent movies.

**MOVIE SC3.** An example of type 3i instability, asymmetric split. We show the case  $\gamma = 2$  and  $\lambda_c = 0.091$ , for times between  $74.78T_p$  and  $100.04T_p$ .

**MOVIE SC4.** An example of type 3ii instability, symmetric split. We show the case  $\gamma = 10$  and  $\lambda = 0.024$ , for times between  $43.50T_p$  and  $50.00T_p$ .

**MOVIE SC5.** An example of type 1 instability, vacillation. We show the case  $\gamma = 5$  and  $\lambda = 0.024$ , for times between 0 and  $40.02T_p$ .

## C.2 Movies of quasi-geostrophic shallow-water doubly-connected equilibria

Supplementary movies are available on the compact disc attached to this thesis in the folder DC. They are also available online, hosted on the *Journal of Fluid Mechanics* website at <http://dx.doi.org/10.1017/jfm.2013.104>.

**MOVIE DC1.** Examples of doubly-connected vortex equilibria for  $\gamma=0.02$ , 3, and 10 at  $\alpha = 0.2$ . For each case we begin at the distance  $\delta_{min} = 0.8$ , and end at the smallest distance attained,  $\delta_{min} = \delta_f(\gamma)$ , at which a sharp corner develops on the boundary of one of the vortices. The smallest distance decreases with  $\gamma$ . In this and subsequent movies we are in a frame of reference rotating with the equilibria, and  $|x|, |y| \leq 3$ .

**MOVIE DC2.** An example of the evolution of a state undergoing partial straining out  $PSO_b$ . We show the case  $\gamma = 1$ ,  $\alpha = 0.4$ , and  $\delta_{min} = 0.339$ , for times between  $88.47T_p$  and  $132.71T_p$ .

**MOVIE DC3.** An example of the evolution of a state undergoing partial merger PM. We show the case  $\gamma = 2$ ,  $\alpha = 0.6$ , and  $\delta_{min} = 0.270$ , for times between  $150.28T_p$  and  $254.31T_p$ .

**MOVIE DC4.** An example of the evolution of a state having large  $\gamma$  which undergoes complete merger CM. We show the case  $\gamma = 10$ ,  $\alpha = 0.2$ , and  $\delta_{min} = 0.268$ , for times between  $121.70T_p$  and  $135.22T_p$ .

**MOVIE DC5.** An example of the evolution of a state having small  $\gamma$  which undergoes complete merger CM. We show the case  $\gamma = 0.02$ ,  $\alpha = 1.0$ , and

$\delta_{min} = 0.266$ , for times between  $33.50T_p$  and  $100.49T_p$ .

**MOVIE DC6.** An example of the evolution of a state undergoing vacillations. We show the case  $\gamma = 10$ ,  $\alpha = 0.4$ , and  $\delta_{min} = 0.200$ , for times between 0 and  $115.68T_p$ . Note, the boundary of stability occurs at  $\delta_{min} = \delta_c = 0.265$ .

### C.3 Movies of shallow-water simply-connected quasi-equilibria

Supplementary movies are available on the compact disc attached to this thesis in the folder SW. They will also be available in a forthcoming paper.

**MOVIE SW1.** The curvature  $\kappa$  as a function of  $\theta$  for the state  $(\gamma, \mathcal{R}) = (1, 0.1)$  at  $\lambda = 0.400$ , for times between 0 and  $11T_{ip}$  (recall, the ramp period has length  $\Delta_\tau = 10T_{ip}$ ). Here,  $\theta = 2\pi\xi(s)/\xi(P)$ , where  $P$  is the arc length of the PV contour,  $s$  is the distance along the PV contour and  $\xi(s) = \int_0^s |\kappa| ds'$ . When  $\kappa > 0$ ,  $\theta$  is the tangent angle. The shift along the  $x$ -axis arises from differences in what the numerical method specifies as the “first” point on each PV contour. Note that here the contour is discretised by 1200 points on a grid having a resolution of  $1024^2$ .