## SUPPLEMENATARY MATERIALS

## Next Generation QTAIM for the Design of Emitters Exhibiting Thermally-Activated Delayed Fluorescence (TADF)

Zi Li, Xing Nie, Alireza Azizi, Yong Yang, Tianlv Xu, Steven R. Kirk<sup>\*</sup> and Samantha Jenkins<sup>\*</sup>

Key Laboratory of Chemical Biology and Traditional Chinese Medicine Research and Key Laboratory of Resource National and Local Joint Engineering Laboratory for New Petro-chemical Materials and Fine Utilization of Resources, College of Chemistry and Chemical Engineering, Hunan Normal University, Changsha, Hunan 410081, China

email: steven.kirk@cantab.net email: samanthajsuman@gmail.com

**1.** Supplementary Materials S1. The QTAIM  $\{q,q'\}$  path-packets of the cyclazine molecular graph for the S<sub>1</sub> and T<sub>1</sub> states without and with an applied electric (**E**)-field.

**2.** Supplementary Materials S2. The QTAIM  $\{p,p'\}$  path-packets of the cyclazine molecular graph for the S<sub>1</sub> and T<sub>1</sub> states without and with an applied electric (**E**)-field.

**3.** Supplementary Materials S3. The values of the precession  $\mathbb{K}$  along the C3-C5 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states

## 1. Supplementary Materials S1.

For the precession of the  $\{q,q'\}$  path-packet, defined by the  $\underline{e}_2$  eigenvector, about the bond-path,  $\beta = (\pi/2 - \alpha)$ and  $\alpha$  is defined by equation (2) and the right panel of **Scheme 1** of the main text, we can write an expression  $\mathbb{K}'$  for the bond-path-flexibility:

$$\mathbb{K}' = 1 - \cos^2 \beta$$
, where  $\cos \beta = \underline{\mathbf{e}}_2 \cdot \underline{\mathbf{u}}$ ,  $\beta = (\pi/2 - \alpha)$  and  $0 \le \mathbb{K}' \le 1$  (2)

For  $\mathbb{K}' = 0$  we have a maximum degree of facile character and for  $\mathbb{K} = 1$  we have the minimum degree of facile character and values of  $\mathbb{K}' = 0$  and  $\mathbb{K}' = 1$  therefore indicate bond-paths with the lowest and highest tendencies towards bond-path-flexibility respectively.





**(b)** 



**(d)** 

**Figure S1(I).** The QTAIM  $\{q,q'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the unchirped pulse 30 fs, 40 fs, 50 fs and 75fs with a positive energy gap  $\Delta E(S_1-T_1) > 0$  are presented in each of sub-figures (**a-d**) respectively.













(b)



**Figure S1(II).** The QTAIM {*q,q'*} path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the unchirped pulse 5fs, 10fs, 60fs and 65fs with a negative energy gap  $\Delta E(S_1-T_1) < 0$  are presented in each of sub-figures (**a-d**) respectively.













(b)



**Figure S1(III).** The QTAIM  $\{q,q'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the chirped pulse 10 fs, 45 fs, 67 fs and 90 fs with a positive energy gap  $\Delta E(S_1-T_1) > 0$  are presented in each of sub-figures (**a-d**) respectively.















(b)



**Figure S1(IV).** The QTAIM  $\{q,q'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the chirped pulse 5fs, 30fs, 78fs and 100fs with a negative energy gap  $\Delta E(S_1-T_1) < 0$  are presented in each of sub-figures (**a-d**) respectively.



**(b)** 

**Figure S1(V).** The QTAIM  $\{q,q'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of an applied electric(**E**)-field =  $\pm 0.2$  a.u are presented in each of sub-figures (**a-b**) respectively.

2. Supplementary Materials S2.











(b)

(a)

(c)



**(d)** 

**Figure S2(I).** The QTAIM {*p*,*p*'} path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the unchirped pulse 30 fs, 40 fs, 50 fs and 75 fs with a positive energy gap  $\Delta E(S_1-T_1) > 0$  are presented in each of sub-figures (**a-d**) respectively.









(a)



(c)

(b)



**Figure S2(II).** The QTAIM {*p*,*p'*} path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the unchirped pulse 5fs, 10fs, 60fs and 65fs with a negative energy gap  $\Delta E(S_1-T_1) < 0$  are presented in each of sub-figures (**a-d**) respectively.













(b)



**Figure S2(III).** The QTAIM  $\{p,p'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the chirped pulse 10 fs, 45 fs, 67 fs and 90 fs with a positive energy gap  $\Delta E(S_1-T_1) > 0$  are presented in each of sub-figures (**a-d**) respectively.













(b)



**Figure S2(IV).** The QTAIM  $\{p,p'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of the chirped pulse 5fs, 30fs, 78fs and 100fs with a negative energy gap  $\Delta E(S_1-T_1) < 0$  are presented in each of sub-figures (**a-d**) respectively.



**Figure S2(V).** The QTAIM  $\{p,p'\}$  path-packets of the cyclazine molecular graph corresponding to the S<sub>1</sub> (left panel) and T<sub>1</sub> (right panel) states of an applied electric(**E**)-field =  $\pm 0.2$  a.u are presented in each of sub-figures (**a-b**) respectively.



**Figure S3(I).** The values of the precession  $\mathbb{K}$  along the C7-N9 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states of the unchirped pulse with a positive energy gap  $\Delta E(S_1-T_1) > 0$  (top-left) of sub-figure, the unchirped pulse with a negative energy gap  $\Delta E(S_1-T_1) < 0$  (top-right) of sub-figure. The chirped pulse with  $\Delta E(S_1-T_1) > 0$  (bottom-left) of sub-figure and the chirped pulses with  $\Delta E(S_1-T_1) < 0$  (bottom-right) of sub-figure.



**Figure S3(II).** The values of the precession  $\mathbb{K}$  along the C13-N9 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states of the unchirped pulse with a positive energy gap  $\Delta E(S_1-T_1) > 0$  (top-left) of sub-figure, the unchirped pulse with a negative energy gap  $\Delta E(S_1-T_1) < 0$  (top-right) of sub-figure. The chirped pulse with  $\Delta E(S_1-T_1) > 0$  (bottom-left) of sub-figure and the chirped pulses with  $\Delta E(S_1-T_1) < 0$  (bottom-right) of sub-figure.

The profiles of the K for the C10-C2 *BCP* with the unchirped laser pulse corresponding to a S<sub>1</sub> state at a given time with  $\Delta E(S_1-T_1) > 0$  responding less than the corresponding T<sub>1</sub> state the same time, see the top-left panel of **Figure S3(III**). The corresponding K for the C10-C2 *BCP* with  $\Delta E(S_1-T_1) < 0$  and unchirped pulse result in a mixing of the K profiles of the S<sub>1</sub> and T<sub>1</sub> states, see the top-right panel of **Figure S3(III**). The effect of the chirped laser pulse on the K profiles with a positive energy gap  $\Delta E(S_1-T_1) > 0$  is to spread out the K profiles of the S<sub>1</sub> and T<sub>1</sub> states, see the bottom-left panel of **Figure S3(III**). Conversely, the effect of the chirped pulse on negative energy gap  $\Delta E(S_1-T_1) < 0$  is to contract the K profiles corresponding to the S<sub>1</sub> and T<sub>1</sub> states to closer together, see the bottom-right panel of **Figure S3(III**).



**Figure S3(III).** The values of the precession  $\mathbb{K}$  along the C10-C2 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states of the unchirped pulse with a positive energy gap  $\Delta E(S_1-T_1) > 0$  (top-left) of sub-figure, the unchirped pulse with a negative energy gap  $\Delta E(S_1-T_1) < 0$  (top-right) of sub-figure. The chirped pulse with  $\Delta E(S_1-T_1) > 0$  (bottom-left) of sub-figure and the chirped pulse s with  $\Delta E(S_1-T_1) < 0$  (bottom-right) of sub-figure.



**Figure S3(IV).** The values of the precession  $\mathbb{K}$  along the C3-C5 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states of the unchirped pulse with a positive energy gap  $\Delta E(S_1-T_1) > 0$  (top-left) of sub-figure, the unchirped pulse with a negative energy gap  $\Delta E(S_1-T_1) < 0$  (top-right) of sub-figure. The chirped pulse with  $\Delta E(S_1-T_1) > 0$  (bottom-left) of sub-figure and the chirped pulse s with  $\Delta E(S_1-T_1) < 0$  (bottom-right) of sub-figure.



**Figure S3(V).** The values of the precession  $\mathbb{K}$  along the C13-C16 *BCP* bond-paths for the S<sub>1</sub> and T<sub>1</sub> states of the unchirped pulse with a positive energy gap  $\Delta E(S_1-T_1) > 0$  (top-left) of sub-figure, the unchirped pulse with a negative energy gap  $\Delta E(S_1-T_1) < 0$  (top-right) of sub-figure. The chirped pulse with  $\Delta E(S_1-T_1) > 0$  (bottom-left) of sub-figure and the chirped pulse s with  $\Delta E(S_1-T_1) < 0$  (bottom-right) of sub-figure.