

Evidence for even parity unconventional superconductivity in Sr₂RuO₄

A. Chronister^{a,1,2}, A. Pustogow^{a,1,2}, N. Kikugawa^b, D. A. Sokolov^c, F. Jerzembeck^c, C. W. Hicks^c, A. P. Mackenzie^{c,d}, E. D. Bauer^e, and S. E. Brown^{a,2}

^aDepartment of Physics & Astronomy, UCLA, Los Angeles, CA 90095, USA; ^bNational Institute for Materials Science, Tsukuba 305-0003, Japan; ^cMax Planck Institute for Chemical Physics of Solids, Dresden 01187, Germany; ^dScottish Universities Physics Alliance, School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews KY16 9SS, UK; ^eLos Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

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Unambiguous identification of the superconducting order parameter symmetry in Sr₂RuO₄ has remained elusive for more than a quarter century. While a chiral *p*-wave ground state analogue to superfluid ³He-*A* was ruled out only very recently, other proposed triplet pairing scenarios are still viable. Establishing the condensate magnetic susceptibility reveals a sharp distinction between even parity (singlet) and odd parity (triplet) pairing, since the superconducting condensate is magnetically polarizable only in the latter case. Here, field-dependent ¹⁷O Knight shift measurements, being sensitive to the spin polarization, are compared to previously reported specific heat measurements for the purpose of distinguishing the condensate contribution from that due to quasiparticles. We conclude that the shift results can be accounted for entirely by the expected field-induced quasiparticle response. An upper bound for the condensate magnetic response of < 10% of the normal state susceptibility is sufficient to exclude all purely odd-parity candidates.

unconventional superconductivity | triplet pairing | Sr₂RuO₄ | nuclear magnetic resonance | Knight shift | order parameter | Keyword XY | ...

Unraveling the secrets of the superconducting state in Sr₂RuO₄ (1–3) has been a priority for unconventional superconductivity research since its discovery in 1994, by Maeno and coworkers (4). Among several reasons for broad interest in Sr₂RuO₄ was the particularly notable suggestion of a *p*-wave triplet pairing state (5). One of the symmetry-allowed triplet states is the chiral state $\mathbf{z}(p_x \pm ip_y)$, which breaks time reversal symmetry and therefore requires two components. Soon after, the combination of results from NMR Knight shift (6) and μ^+ SR (7) measurements lent support to the chiral *p*-wave description. Further evidence was inferred from the observed onset of a non-zero Kerr rotation at T_c (8). Unresolved issues remained, however. For example, thermal conductivity (9) and specific heat (10) experiments were both interpreted as evidence for a nodal gap structure (3). Furthermore, the field-driven first-order phase transition observed at low temperatures (11, 12) is a natural consequence of the Zeeman coupling to quasiparticles (1), but this mechanism is inoperative for any fully gapped state. In a step toward clarification, recent ¹⁷O NMR measurements exclude candidate *p*-wave states with *k*-independent *d*-vector aligned parallel to the *c*-axis (13, 14). Left open is the possibility for an odd-parity triplet-pairing state with an in-plane *d*, as explicitly discussed in recent theoretical works (15, 16).

With these developments in mind, we recall other distinctive properties of superconductivity in Sr₂RuO₄. Among unconventional superconductors, Sr₂RuO₄ is not just stoichiometric, but possibly also the cleanest (1). Unlike the cuprates (17) and Fe-based superconductors, the superconductivity emerges

from a well-understood Fermi-liquid normal state (18), and for which the fermiology is precisely characterized (19, 20). Thus, Sr₂RuO₄ constitutes an ideal platform for achieving a level of understanding for an unconventional superconductor rivaling what is routinely expected for conventional superconductors. In general, identifying the order parameter symmetry is an essential step toward that goal. Moreover, there is a broader motivation to make connections from a system so well characterized, to other unresolved questions in unconventional superconductivity. As described above, Sr₂RuO₄ was reasonably proposed as analogous to ³He, for which ferromagnetic (FM) fluctuations are key to the superfluid triplet pairing. Indeed, the presence of FM correlations were inferred early on (4, 5). In an alternative proposal, the system is a more weakly coupled analog of the cuprate and Fe-based superconductors, in which antiferromagnetic fluctuations most naturally mediate singlet pairing (21). Thus, associating the superconducting state with AF fluctuations would more directly relate the physics of Sr₂RuO₄ to the much broader class of unconventional superconductors.

The temperature and field dependences of the NMR Knight shifts $K_s(T < T_c, \mathbf{B})$ are recognized as a crucial probe of the order-parameter symmetry. In the normal state, $K_s \sim \chi_n$, with χ_n the susceptibility. In the superconducting phase, a

Significance Statement

Sr₂RuO₄ is distinctive among unconventional superconductors, in that, in addition to exhibiting evidence for strong correlations, it is stoichiometric and extremely clean. As a result, its electronic structure is unusually well-characterized, rendering it an ideal platform for developing a deep understanding of the mechanism behind the emergence of the superconducting state from a Fermi liquid. Toward that end, an unambiguous determination of the pairing symmetry is an essential step. For more than two decades, the preponderance of evidence pointed to a triplet spin pairing state, and only recently has this interpretation been challenged. By means of field-dependent NMR Knight shift measurements, we eliminate from further consideration all candidate purely odd-parity triplet pairing states.

A.C., A.P., A.P.M. and S.E.B. conceived and designed the experiments. N.K., D.A.S., F.J., C.W.H. and A.P.M. prepared the crystal. E.D.B. characterized the sample and performed the spin labelling. A.C. and A.P. performed the NMR measurements. A.C., A.P., A.P.M. and S.E.B. discussed the data, interpreted the results and wrote the paper with input from all authors.

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¹A.C. and A.P. contributed equally to this work.

²To whom correspondence should be addressed. E-mail: aaronchronister@physics.ucla.edu, pustogow@ifp.tuwien.ac.at, brown@physics.ucla.edu

54 nonzero susceptibility χ_{sc} associated with condensate polar-
 55 ization is expected generally for triplet-paired, p -wave states.
 56 The response ranges from vanishingly small to that of the normal
 57 state, χ_n , with the limiting cases corresponding to $\mathbf{d} \parallel \mathbf{B}$,
 58 $\mathbf{d} \perp \mathbf{B}$, respectively. Hence, the observed reduction of the
 59 Knight shift for an applied in-plane field excludes the chiral
 60 state (13), for which $\mathbf{d} \parallel \mathbf{c}$. Crucially, states characterized
 61 by $\mathbf{d} \perp \mathbf{c}$ are not eliminated by the prior work. Among such
 62 states allowed by the crystal symmetry is the so-called 'helical'
 63 state, $\mathbf{d} = p_x \mathbf{x} + p_y \mathbf{y}$, for which $\chi_{sc}/\chi_n = 1/2$ (in the absence
 64 of Fermi-liquid corrections (13, 14)).

65 The most direct way to test for symmetry-allowed states
 66 with $\mathbf{d} \perp \mathbf{c}$ is to perform measurements with $\mathbf{B} \parallel \mathbf{c}$, since for
 67 this orientation the response of the helical state is $\chi_{sc} = \chi_n$.
 68 However, the relevant upper critical field $B_{c2,[001]} < 100$ mT is
 69 very small* making such experiments particularly challenging
 70 because signal strength and spectral resolution are reduced for
 71 very weak applied fields. Here, we take another approach, dis-
 72 cussed previously in Refs. (14, 23): the field orientation is fixed
 73 in-plane, and the ^{17}O shifts K_s are evaluated at low tempera-
 74 ture (25 mK) while varying B as much as experimentally fea-
 75 sible. Quasiparticle creation is controlled by the field strength,
 76 and also contributes to the magnetic response. At issue is
 77 the fractional magnetic response arising from quasiparticles,
 78 which must be separated from the condensate contribution.
 79 The relative contributions are determined by way of compar-
 80 ing to previously reported specific heat results $C_e(B)/T$ (24),
 81 which is sensitive to field-induced quasiparticles only. We
 82 estimate that the upper bound for the condensate portion is
 83 $\chi_{sc}/\chi_n < 10\%$ (25), a value that contradicts the expectation
 84 for any of the proposed purely odd-parity order parameters
 85 relevant to Sr_2RuO_4 .

86 Results

87 **Pulse-Heating Control by Low-Power NMR Experiments.** The
 88 recent studies (13, 14) identified RF heating by the NMR
 89 pulses as a possible impediment to accurate measurements
 90 in the superconducting state. The issue is illustrated in the
 91 results of Fig. 1. So as to enhance sensitivity to this potential
 92 artifact, we examined the transients with the field set to 1.38
 93 T, a value very close to, but smaller than B_{c2} . Clear evidence
 94 for warming by the RF pulsing is inferred from a transient
 95 response corresponding to that of the normal-state (instead of
 96 the sought-after superconducting state). Shown in Fig. 1(b,c)
 97 are ^{17}O spectra corresponding to central transitions for the
 98 three oxygen sites, $\text{O}(1_{\parallel,2,1\perp})$, at applied magnetic fields
 99 slightly above and below B_{c2} . With $B = 1.5$ T $> B_{c2}$, the
 100 line shape remains unaffected by changing the pulse energy,
 101 and a normal state spectrum is also produced for $B = 1.38$ T
 102 $< B_{c2}$ when using a pulse energy $E_p = 130$ nJ. Decreasing
 103 E_p to 40 nJ leads to a response where a new spectral line
 104 appears for each site, indicating the coexistence of normal
 105 and superconducting phases. This data set is particularly
 106 useful, since the macroscopic phase segregation provides a
 107 quantitative measure of the magnetization jump ΔM at the
 108 discontinuous (first-order) transition (11, 12). Note that these
 109 data are recorded following a single-pulse excitation. That is,
 110 the transient NMR response corresponds to a free induction
 111 decay (FID). All shift results of the present work were obtained

* a -axis stress increases B_{c2} significantly by this measure, see Ref. (22)

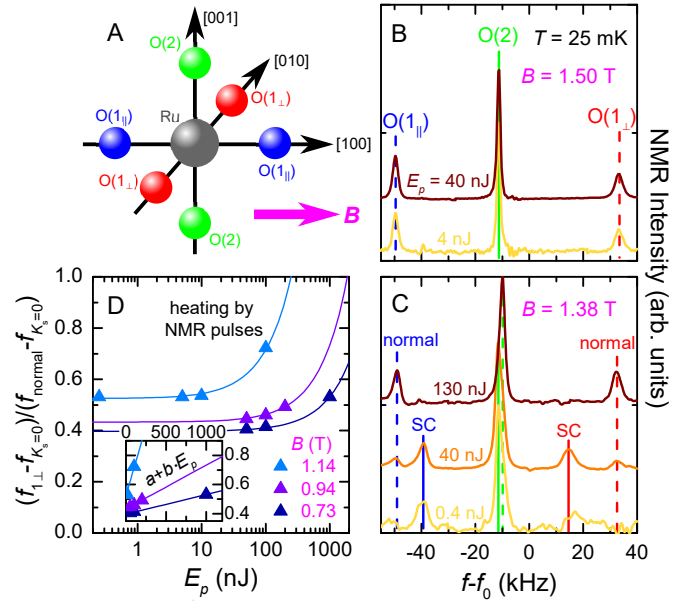


Fig. 1. (A) Sr_2RuO_4 involves three distinct oxygen sites for field direction $\mathbf{B} \parallel [100]$. (B) The three associated ^{17}O NMR central transitions ($\text{O}(1_{\parallel})$, $\text{O}(2)$, $\text{O}(1_{\perp})$ from left to right) are independent of pulse energy E_p at 1.50 T $> B_{c2} \simeq 1.45$ T. (C) Also at $B = 1.38\text{T} \lesssim B_{c2}$ the normal-state spectrum is observed for $E_p \geq 10^{-7}$ J. Reducing to $E_p = 40$ nJ leads to doubled spectral features, most pronounced for $\text{O}(1_{\parallel, \perp})$, which we assign to coexisting normal (dashed vertical lines) and superconducting (solid) contributions around the first-order transition. Further reduction of E_p reveals the pure superconducting-state spectrum. (D) $\text{O}(1_{\perp})$ frequencies normalized to normal-state (f_{normal}) and zero-shift ($f_{K_s=0}$; see Fig. 2) positions at $B < B_{c2}$ for variable E_p . Linear fits (solid lines, see inset) indicate that heating is less problematic at lower field due to larger $T_c(B)$. Knight shifts K_s were determined using the frequency values leveling off at $E_p \rightarrow 0$.

112 from FID measurements carried out with RF pulse energies
 113 sufficiently small to avoid heating, as illustrated in Fig. 1(d).

114 Field-Dependent Knight Shifts in Superconducting State.

115 Having established a threshold for heating effects, we now
 116 inspect the spectra recorded at variable field strength. In
 117 Fig. 2, we show the NMR intensity as a function of $f - f_0$,
 118 where $f_0 \equiv ^{17}\gamma B$. The central transitions ($-1/2 \leftrightarrow 1/2$) for
 119 the $\text{O}(1_{\parallel,2,1\perp})$ sites [left to right in the spectrum] exhibit
 120 pronounced variations with changing B . The shifts of the
 121 planar sites $\text{O}(1_{\parallel})$ and $\text{O}(1_{\perp})$ have opposite sign; this is a
 122 consequence of the applied field direction relative to the local
 123 environment. $\text{O}(2)$ is the apical site [Fig. 1(A)]. The dotted
 124 curves include only the quadrupolar and orbital contributions;
 125 more information on these corrections appear below and in
 126 (25): crucially, simultaneous scrutiny of the field-dependent
 127 quadrupolar effects at both in-plane O sites leads to a quan-
 128 titative upper bound on the condensate contribution. Open
 129 symbols line up with these spectral ‘‘baselines’’ at each field at
 130 which data were recorded. Also shown, using the dashed lines
 131 and closed symbols, are transition frequencies at each field,
 132 generated using the *known* normal state NMR parameters (25).
 133 Then, the frequency *differences* between closed and open sym-
 134 bols are proportional to the hyperfine fields, and constitute
 135 the product of (normal-state) Knight shifts with applied field,
 136 $K_{s,\text{normal}} ^{17}\gamma B$, for $\text{O}(1_{\parallel})$, $\text{O}(2)$ and $\text{O}(1_{\perp})$. When decreasing
 137 the field $B < B_{c2}$, the NMR lines in Fig. 2 are displaced from
 138 the normal-state positions, towards the frequency correspond-
 139

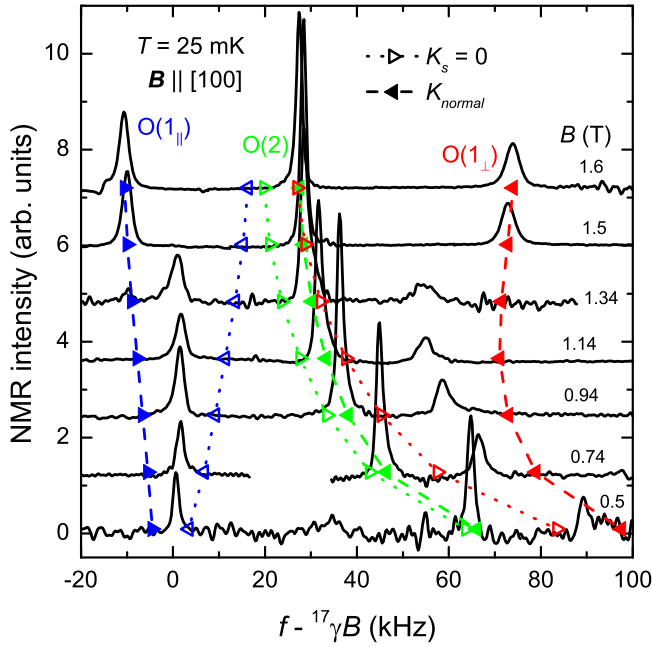


Fig. 2. Spectra for central ^{17}O NMR transitions at different field strengths, for $\text{O}(1_{\parallel})$, $\text{O}(2)$, $\text{O}(1_{\perp})$ sites, respectively *left-right*, plotted as intensity vs. $f - ^{17}\gamma B$. The dotted curves running vertically through the spectra follow the expected field dependence after taking into account quadrupolar and orbital couplings; the dashed curves also include the normal-state hyperfine fields. See (25) for details of quadrupolar and orbital contributions to the transition frequencies, as well as an analysis of the sample orientation relative to \mathbf{B} .

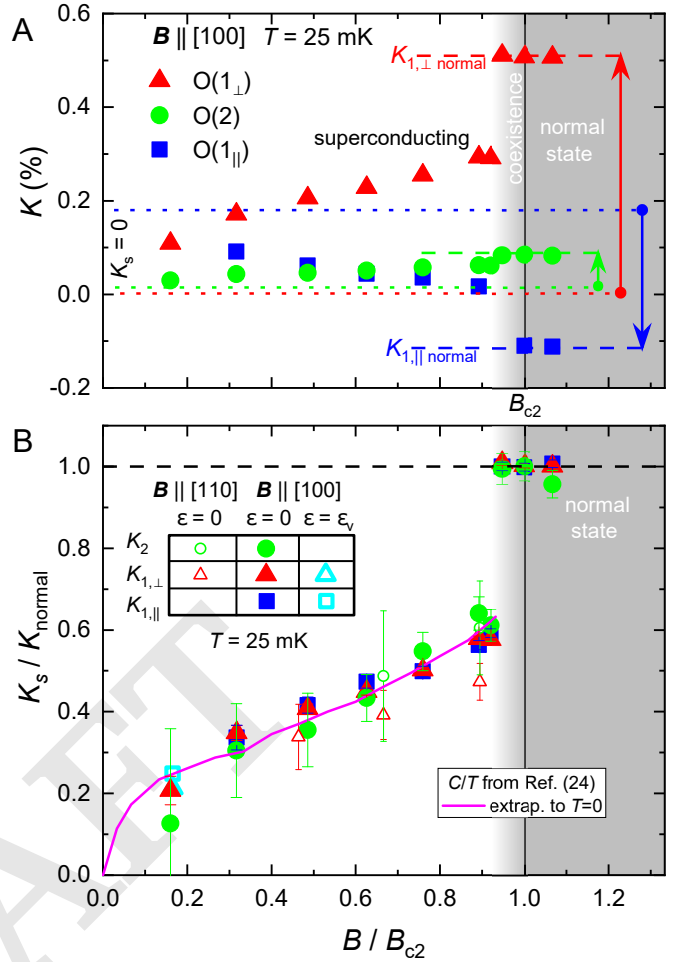


Fig. 3. (A) NMR shifts $K = K_s + K_o$ determined from the spectra in Fig. 2. While the shifts are positive and the assigned $K_o \simeq 0.0\%$ for $\text{O}(2)$ and $\text{O}(1_{\perp})$, the $\text{O}(1_{\parallel})$ line occurs at a positive value $K_o = 0.18\%$ at $B = 0$ and $K_{1,\parallel} < 0$ (6, 26). (B) The field-dependent drop of NMR Knight shift determined in the present work at $T = 25$ mK is compared to specific heat C/T (24) extrapolated to $T = 0$ (28), all normalized to the normal state value. The values of K_s coincide with the zero-temperature extrapolations of C/T , providing compelling evidence that this is the contribution of unpaired quasiparticles in the superconducting state. Measurements along $[110]$ (small open symbols) reveal a similar jump at the transition and also uniaxial strain results (open cyan symbols, $\mathbf{B} \parallel [100]$, $\varepsilon_{\alpha\alpha} = \varepsilon_v$) from Ref. (13) coincide at low B/B_{c2} .

Comparison to Specific Heat: Condensate Polarization vs. Field-Induced Quasiparticles. The main results of this work are displayed in Fig. 3(B), where the Knight shifts are compared to previous heat capacity results (24), $C_e(B)/T$ (C_e the electronic contribution), both normalized to the normal state. As shown, the field-induced trends are similar, and particularly relevant to the open question of order-parameter symmetry. Simply put, at non-zero field, an NMR shift can originate from quasiparticles, and, in the case of triplet pairing, also from the condensate. In contrast, the specific heat is sensitive only to the quasiparticle response with no contribution from the condensate. Note that in a fully gapped superconductor, gapless excitations are created in vortex cores, where the order parameter is suppressed. Whereas, in the case of a nodal state, the quasiparticle perturbations arising from both Zeeman and orbital coupling lead to additional contributions to the DOS at E_F . (The latter is widely referred to as the

ing to $K_s = 0$, due to the drop of K_s in the superconducting state. Below, we compare and contrast the measured shifts K_s with results of field-dependent specific heat experiments, which are sensitive to the field-induced quasiparticles.

The parameters needed for the quadrupolar corrections were determined previously (6, 26, 27) and confirmed here in field-dependent measurements (25). In particular, we determined the field orientation as deviating $\simeq 3.0^\circ \pm 0.4^\circ$ from the $[100]$ direction, and otherwise aligned orthogonal to the c -axis, $\theta = 90^\circ \pm 0.2^\circ$. Due to several factors, including reduced signal strength and resolution, as well as the strong increase of the $\text{O}(1_{\parallel})$ quadrupolar component at low fields, we limited the measurements to $B \geq 0.24$ T. In addition to the well-known quadrupolar effects, one has to include purely orbital contributions. These were evaluated in Ref. (6), yielding $K_o = +0.18\%$ for the $\text{O}(1_{\parallel})$ site and a value indistinguishable from zero for $\text{O}(1_{\perp})$ and $\text{O}(2)$. See (25) for further comment.

The shifts $K_{1\parallel,2,1\perp}$, are plotted as a function of B in Fig. 3. Results are shown in panel (A) as total shift, $K = K_s + K_o$. In the normal state, $K_{1\parallel} < 0$, while $K_{2,1\perp} > 0$; each exhibits a reduction in the superconducting state. B_{c2} is marked by the discontinuous change of each of the three sites, accompanied by a coexistence regime [cf. Fig. 1(b,c)]. Consistent with expectations ($B \gg B_{c1}$) (29), the results indicate that diamagnetic shielding is a small effect. Otherwise, the discontinuous drop ΔM (Figs. 1,2) would be similar for all three sites. Instead, only the hyperfine field, which is much greater for the planar sites than it is for the apical site, and opposite in sign for $\text{O}(1_{\parallel})$ relative to $\text{O}(2)$ and $\text{O}(1_{\perp})$, decreases on entering the superconducting state.

Volovik Effect (30).

As can be seen by inspection of Fig. 3(B), we observe no systematic difference between the $T \rightarrow 0$ extrapolation of the heat capacity data of Ref. (24) and the spin susceptibility deduced from our measurements. Taking into account systematic uncertainties we estimate an upper limit for the condensate response of $< 10\%$ of that of the normal state, for fields applied both along [100] and [110] (see (25) for detailed discussion). Similar $K_{1\parallel,\perp}$ are found at $B/B_{c2} = 0.17$ under strained conditions (13). These observations place such strong constraints on the magnetic polarizability of the condensate that we believe they rule out any pure p -wave order parameter for the superconducting state of Sr_2RuO_4 , as we now discuss.

The p -wave order parameters most commonly discussed in the context of Sr_2RuO_4 are the so-called chiral ($\hat{\mathbf{z}}(p_x \pm ip_y)$) and helical ($p_x \hat{\mathbf{x}} + p_y \hat{\mathbf{y}}$) states. Assuming that the unit vectors encoding spin directions are pinned to the lattice, they are predicted in the simplest models to result in condensate polarizabilities of 100% (chiral) and 50% (helical) of the normal state value. The chiral state was ruled out by our previous work (13), but the helical state and certain others were not. The data presented in Fig. 3 allow us to go much further; it is unclear how to reconcile an upper bound of 10% of the normal state susceptibility with any p -wave state: While Fermi Liquid corrections may reduce the condensate response to $\sim 30\%$ of the normal state value (14), this still far exceeds our observations. Spin-orbit coupling effects tend to weaken the distinction between spin-singlet and spin-triplet states (31), in that a nonzero magnetic response survives in the limit $T, B \rightarrow 0$ (16). Thus, we conclude that SOC effects are not significantly impacting our results, an outcome we tentatively attribute to the dominant normal state DOS (and magnetic response) arising from those states at E_F proximate to a van Hove singularity, where the SOC is relatively weak (27). One could also postulate extreme situations such as a momentum independent \mathbf{d} aligned along either [100] or [110], or an unpinned \mathbf{d} free to rotate in response to the applied field. None can predict a spin susceptibility suppression that would be compatible with our results; a few remaining possibilities have been ruled out by our use of both [100] and [110] fields in the current experiments. We therefore assert that our measurements have ruled out any p -wave order parameter candidate for the superconducting state of Sr_2RuO_4 .

Summary and Outlook

Given this input, we close with an evaluation of the current understanding of superconductivity in Sr_2RuO_4 . In isolation, our NMR findings are consistent with even-parity states (32), such as $d_{x^2-y^2}$ (B_{1g}), d_{xy} (B_{2g}) or $\{d_{xz}; d_{yz}\}$ (E_{1g}), or $g_{xy(x^2-y^2)}$ (A_{2g}). Indeed, STM measurements are interpreted as most consistent with the B_{1g} state (33), similar to thermal transport experiments (9). Further emphasizing the constraints imposed by the present work, the viability of proposed even parity states based on interorbital pairing (34–36), and that of a mixed-parity order parameter of the form $d \pm ip$ (37) necessarily depend on a sufficiently small condensate response to in-plane fields.

In considering other recent experimental developments, we would like to note in particular reports of a discontinuity in the shear elastic constant c_{66} (corresponding to B_{2g} deformations) (38, 39), but not in $(c_{11} - c_{12})/2$ (B_{1g}) (38). This

is the expected outcome for a coupling of nearly degenerate even-parity states such as $\{d_{x^2-y^2}; g_{xy(x^2-y^2)}\}$ (21, 40) or $\{s'; d_{xy}\}$ (41), but not for the degenerate combination $\{d_{xz}; d_{yz}\}$, for which a discontinuity in $(c_{11} - c_{12})/2$ is also expected. On the other hand, μ^+ SR measurements have confirmed the early results and observed transition splitting between the TRSB signature and the onset of SC under uniaxial pressure (42). It will be intriguing to see how the quest to finalize identification of the order parameter of Sr_2RuO_4 develops. We believe that by ruling out any pure odd-parity p -wave order parameter possibility, the research we have reported here makes a significant contribution to that process.

Materials and Methods

Sample Preparation. As in previous NMR studies on Sr_2RuO_4 (6), the labelled ^{17}O ($^{17}I=5/2$, $^{17}\gamma=-5.772$ MHz/T (43)) is introduced by high-temperature annealing (6), here in 90% $^{17}\text{O}_2$ atmosphere at 1050 °C. Single-crystal dimensions were (3.5 mm x 1 mm x 0.2 mm), with the shortest dimension corresponding to the out-of-plane [001]-direction, and the longest dimension parallel to [100], see Fig. 1A.

NMR Experiments. To facilitate access to relatively low frequencies covering several octaves, we adopted a top tuning/matching configuration. The NMR coil containing the crystal under study, was mounted on a single-axis piezo-rotator inside the mixing chamber of a bottom-loading dilution refrigerator. Sample alignment enabled in-plane orientation to within $\pm 0.2^\circ$, based on RF susceptibility measurements sensitive to B_{c2} , described in Ref. (13), and discussed in the Supporting Information (25). ^{63}Cu NMR relaxation rate measurements were used to determine the equilibrium bath temperature $T = 25$ mK. As in our previous work (13), low-power RF experiments were carried out to make sure the results were not measurably altered by RF pulse heating effects. The applied field strength B was determined to within uncertainties less than 10's of μT from the NMR resonance of ^3He in the $^3\text{He}/^4\text{He}$ mixture of the dilution refrigerator.

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356 Ref. (24) by finding a larger residual electronic specific heat at low temperatures. While sam-
357 ple quality is the most obvious source of such a discrepancy, it merits further experimental
358 attention. However, since those results indicate a larger quasiparticle contribution (than that
359 of Ref. (24)), the central conclusion of the present work is not invalidated: we find no evidence
360 for a condensate contribution to the spin susceptibility.
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