

1 **Accounting for stochasticity in demographic compensation along the elevational range**
2 **of an alpine plant**

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30 **AUTHORSHIP**

31 MA, ITB and OEG planned the study. MA, PDV and ITB carried out field work. MA, PDV, DB and MC
32 analysed the environmental data. MA analysed the vital rates data with help from MJF. MA constructed
33 and analysed the population dynamics model and led the writing. All authors contributed to the writing.

34 **DATA ACCESSIBILITY**

35 The data and R code used in this study are openly available in GitHub at
36 https://github.com/MarcoAndrello/Stoch_Demogr_Comp_Arabis

37 **ABSTRACT**

38 Demographic compensation arises when vital rates change in opposite directions across populations,
39 buffering the variation in population growth rates, and is a mechanism often invoked to explain the
40 stability of species geographic ranges. However, studies on demographic compensation have disregarded
41 the effects of temporal variation in vital rates and their temporal correlations, despite theoretical
42 evidence that stochastic dynamics can affect population persistence in temporally varying environments.
43 We carried out a seven-year-long demographic study on the perennial plant *Arabis alpina* across six
44 populations encompassing most of its elevational range. We discovered demographic compensation in
45 the form of negative correlations between the means of plant vital rates, but also between their
46 temporal coefficients of variation, correlations and elasticities. Even if their contribution to demographic
47 compensation was small, this highlights a previously overlooked, but potentially important, role of
48 stochastic processes in stabilizing population dynamics at range margins.

49 INTRODUCTION

50 One of the processes shaping population performance across species ranges is demographic
51 compensation between different vital rates, such as recruitment, survival, growth and reproduction
52 (Doak & Morris 2010; Vilellas *et al.* 2015). Demographic compensation arises when different vital rates
53 change in opposite directions across populations in response to environmental gradients, and has been
54 proposed as a mechanism increasing the range of environments over which a species can occur and to
55 explain the apparent stability of species range margins despite strong temporal environmental changes
56 (Doak & Morris 2010; Sheth & Angert 2018). So far, the paradigm of demographic compensation has
57 considered spatial differences in vital rates averaged over years, while disregarding the role of spatial
58 differences in temporal variation of vital rates (Vilellas *et al.* 2015). However, because temporal
59 variation in vital rates can be higher in some parts of a species geographical range (for example, at range
60 margins; Angert 2009; Pironon *et al.* 2017), population growth rates might vary across species ranges not
61 only because of spatial variation in mean vital rates, but also in their temporal variability.

62 Population dynamics in temporally varying environments have received much attention in ecology and
63 conservation (Tuljapurkar 1990; Lande *et al.* 2003). Theory predicts that temporal variability should
64 decrease population growth rates in both structured and unstructured populations (Lewontin & Cohen
65 1969; Tuljapurkar 1990) and empirical studies support these predictions (Morris *et al.* 2008). In addition,
66 positive temporal covariations between vital rates can potentially amplify the effects of environmental
67 stochasticity on population dynamics, while negative temporal covariation can buffer it (Doak *et al.*
68 2005; Jongejans *et al.* 2010; Compagnoni *et al.* 2016). For example, positive covariances between
69 reproduction and survival rates tend to magnify the effect of variability and lead to lower population
70 growth rates than in the case of zero or negative covariances (Jongejans *et al.* 2010). Finally, the
71 elasticities of population growth rates, which measure the change in population growth rate caused by a

72 change in demographic parameters, determine the ultimate effects of temporal variation and vital rate
73 correlations on the population growth rate (Caswell 2001; Tuljapurkar *et al.* 2003). The interplay of these
74 factors is perhaps best summarized by writing the stochastic population growth rate $\log\lambda_s$ using the
75 small-noise approximation, as a function of the intrinsic growth rate $\log\lambda_d$ (calculated using the temporal
76 means of vital rates) minus a product containing temporal coefficients of variation of vital rates (CV_k and
77 CV_l), correlations between vital rates (ρ_{kl}) and vital rate elasticities (e_k and e_l) (Tuljapurkar 1990):

$$78 \log\lambda_s \approx \log\lambda_d - \frac{1}{2} \sum_{k,l} CV_k CV_l \rho_{k,l} e_k e_l \quad (\text{eq. 1})$$

79 Thus, a full picture of how population dynamics change across populations requires quantifying the
80 differences in how mean vital rates, their temporal variation, their correlations and the elasticities
81 change between populations. Such differences between populations can ultimately determine processes
82 of demographic compensation and can thus inform on the stability and dynamics of species ranges (Doak
83 & Morris 2010; Villellas *et al.* 2013).

84 Elevational ranges offer a unique opportunity to study range-wide variation in vital rates and population
85 dynamics at a tractable spatial scale. For plants, elevational ranges have been associated with large
86 differences in life-histories (Laiolo & Obeso 2017). Species living at lower elevations have often larger
87 sizes, higher mortality rates, shorter lifespans and higher fecundities, while species living at higher
88 elevations have smaller sizes, lower mortality rates, longer life spans and reduced flowering rates (Nobis
89 & Schweingruber 2013; Laiolo & Obeso 2017). These life-history patterns have been related to
90 predictions from the r-K selection theory (Pianka 1970), the metabolic theory of ecology (Brown *et al.*
91 2004) and the acquisitive and stress-tolerant strategies of functional ecology (Read *et al.* 2014). While
92 many studies have uncovered elevational patterns in plant life-histories across species, studies on
93 population dynamics are less common, and patterns of variation in plant population growth rates along
94 elevational gradients are less clear. Indeed, the few studies focusing on dynamics of herbaceous plant

95 populations on elevational gradients report increasing (Miller *et al.* 2009; Giménez-Benavides *et al.*
96 2011), decreasing (Kim & Donohue 2011; Pena-Gomez & Bustamante 2012) and stable (García-Camacho
97 *et al.* 2012) patterns of population growth rates with elevation.

98 Here, we aimed at testing whether spatial patterns in temporal variation, temporal correlations and
99 elasticities could be involved in demographic compensation beyond the spatial variation of average vital
100 rates, thereby contributing to the stabilization of species elevational ranges. To this end, we carried out a
101 population dynamics study on *Arabis alpina* (Brassicaceae), a broadly distributed arctic-alpine perennial
102 herb, across most of its elevational range in the European Alps. Specifically, our goals were twofold. First,
103 we aimed at quantifying the spatial variation of four different descriptors of stochastic population
104 dynamics (means, coefficients of variation, correlations and elasticities of plant vital rates) across an
105 elevational gradient. Second, we aimed at quantifying the contributions of each of the four descriptors
106 to the stochastic population growth rate and test for demographic compensation between different
107 descriptors.

108 MATERIALS AND METHODS

109 Model species

110 *Arabis alpina* (L., Brassicaceae) is emerging as a new model organism in plant ecology and evolutionary
111 biology (e.g. Wang *et al.* 2009; de Villemereuil *et al.* 2018) due to its perennial life-cycle and wide
112 elevational distribution. It occurs primarily in the subalpine and alpine belts, predominantly in open,
113 unstable, moist sites with low vegetation cover such as glacier forelands, scree slopes, rock ledges,
114 footpaths and small streams, often in association with calcareous soil (Lauber *et al.* 2018). Seedlings
115 germinate and establish throughout the growing season, plants flower for a few weeks and produce
116 fruits (siliques), and flowering stems eventually wilt and die (Wang *et al.* 2009). Seeds can persist in the
117 soil and form a permanent seed bank (Diemer & Prock 1993; Philipp *et al.* 2018).

118 Data collection

119 This study was conducted in six sites spanning most of the elevational range of *A. alpina* in the European
120 Alps using permanent plots (**Table 1, Figure S1**), which were visited once a year after flowering between
121 2008 and 2014 to record the number of stems and siliques of each individual (See **Appendix S1.1** in
122 **Supporting Information**). *In-situ* germination tests were not successful, so germination rates could not
123 be estimated locally and seed bank dynamics was disregarded in the matrix population model, but we
124 conducted a sensitivity analysis to assess the effects of uncertainty in seed germination on the results
125 (Nguyen *et al.* 2019; **Appendix S1.5, S2.2**).

126 Microclimatic conditions, soil chemistry and species composition of the vegetation were measured in
127 each plot to model plant vital rates in function of environmental conditions. Temperature data loggers
128 (iButton® Hygrochron, Maxim Integrated™) provided estimates of summer daily mean temperature
129 (T_{mean}) and daily temperature range (T_{range} ; **Table 1**). Missing records (due to malfunctioning of the data-
130 loggers) were imputed using data from nearby weather stations, resulting in ten resampled datasets

131 **(Appendix S1.2)**. Soil acidity (pH), total soil carbon and nitrogen content were determined following
132 standard methods (Schinner *et al.* 1996). Abundance-dominance (Braun-Blanquet) lists of plant species
133 were used to calculate abundance weighted means for vegetative height and specific leaf area (SLA),
134 using values from the ANDROSACE (Thuiller *et al.* 2014) and the TRY (Kattge *et al.* 2011) databases. After
135 performing a principal component analysis on the three soil variables and the two vegetation variables
136 **(Appendix 2.1, Figure S3, S4)**, we retained the first two axes to predict plant vital rates: *SoilVeg₁*
137 (explaining 52% of the variance), positively related to acidic soils with high C and N content, and *SoilVeg₂*
138 (explaining 29% of the variance), summarizing variation from slow-growing short vegetation to fast-
139 growing tall vegetation.

140 **Analysis**

141 We used a five-step approach to test how four *descriptors* (μ : means; *CV*: coefficients of variation; *E*:
142 elasticities; ρ : temporal correlations) of seven *life-cycle components* (*S*: survival; *G*: retrogressive growth;
143 G^- : stasis; G^+ : progressive growth; F_0 : reproduction; F_1 : fecundity; F_2 : recruit size) contribute to
144 demographic compensation across the elevational range of *A. alpina*. First, we constructed matrix
145 population models for each site and year using statistical models predicting plant vital rates from
146 environmental variables (Step 1). Second, we used the matrix models to calculate the seven life-cycle
147 components, stochastic population growth rate $\log\lambda_s$ and elasticities of $\log\lambda_s$ (Step 2). Third, we tested
148 for significant relationships between elevation and population dynamics variables (Step 3). Fourth, we
149 performed a stochastic life-table response experiment (SLTRE) in order to decompose the differences in
150 $\log\lambda_s$ between sites into contributions C_l^k of each life-cycle component *l* and each descriptor *k* (Step 4).
151 Finally, we assessed demographic compensation by testing for negative and positive correlations
152 between the SLTRE contributions C_l^k (Step 5).

153 *Step 1. Prediction of plant vital rates*

154 The plant vital rates used to construct the matrix population models were survival (whether the plant
155 survives to $t + 1$ or not), size (the size of the plant at time $t + 1$, conditional on survival), reproduction
156 (whether the plant bears siliques or not at time t), reproductive output (the number of siliques of the
157 plant at time t , conditional on reproduction) and recruit size. Plant vital rates were predicted using
158 generalized linear mixed models (GLMMs; Zuur *et al.* 2009) as a function of plant size at time t (except
159 for recruit size that, by definition, did not exist at time t), T_{mean} , T_{range} , $SoilVeg_1$ and $SoilVeg_2$ treated as
160 fixed effects; plant size at time t and T_{mean} were also included as quadratic terms. Site, year nested within
161 site and plot nested within site were included as random effects on the intercept and the slopes when
162 significant. The error structure of the models was Gaussian (for \log_{10} -transformed reproductive output),
163 Bernoulli (for survival and reproduction), or negative binomial (for growth and recruit size). We
164 accounted for uncertainty in the data using a total 2000 bootstrap samples over the ten imputed climatic
165 datasets. For each bootstrap sample, we fitted the $2^7=128$ models corresponding to the combinations of
166 the predictors, sampled one of them according to its Akaike weight (Burnham & Anderson 2002),
167 obtained site- and year-specific predictions of vital rates (by setting predictors to their mean values over
168 the plots of each site and year) and constructed matrix models to perform all the subsequent population
169 dynamics analyses. Means and 95% confidence intervals for the reported results were calculated from
170 the 2000 predicted values using the percentile method. All analyses were run in R 3.6.0 with packages
171 *lme4* 1.1-21 and *MuMIn* 1.43.6 (Bartoń 2009; Bates et al. 2015; **Appendix S1.3**).

172 *Step 2. Population dynamics analyses*

173 We defined a matrix population model (Caswell 2001) with 50 size classes of one-stem each, which
174 covered the range of variation in plant sizes observed in the field. The projection matrix **A** was the sum
175 of the transition matrix **P** = [p_{ij}] and the fecundity matrix **F** = [f_{ij}], which were constructed using the
176 predicted vital rates obtained in Step 1:

177 $p_{ij} = s_j g_{ij}$

178 $f_{ij} = \varepsilon F_{0,j} F_{1,j} F_{2,i}$ (eq. 2)

179 where j is plant size in year t ; i is plant size in year $t+1$; s_j (survival) g_{ij} (growth), $F_{0,j}$ (reproduction), $F_{1,j}$
180 (reproductive output) and $F_{2,i}$ (recruit size) are the predicted vital rates. $\varepsilon = 0.02$ is a seedling
181 establishment coefficient converting the number of fruits in one year to the number of seedling in the
182 following year, and was set equal to the median value of the ratio of the observed number of seedlings
183 to the number of fruits in the previous year over all plots and sites.

184 Life-cycle components for each site and year were calculated as averages of the predicted vital rates over
185 size classes weighted by the stable stage distribution vector (Salguero-Gómez *et al.* 2016). Specifically, S ,
186 F_0 and F_1 were calculated as weighted averages of the s_j 's, $F_{0,j}$'s and $F_{1,j}$'s (eq. 2), respectively. G^-
187 represents transitions from larger to smaller size classes and was calculated as the weighted average of
188 all the g_{ij} 's for which $i < j$. Similarly, G^- (representing individuals not changing in size) and G^+ (representing
189 transitions to larger size classes) were calculated as weighted averages of all the g_{ij} 's for which $i = j$ and i
190 $> j$, respectively. F_2 was calculated as the mean recruit size distribution $F_{2,i}$.

191 For each site, we calculated the temporal means and coefficients of variation of each life-cycle
192 component and temporal correlations between pairs of life-cycle components (Pearson's correlation)
193 over years. The stochastic population growth rate $\log \lambda_s$ was calculated via the simulation method by
194 randomly sampling one of the year-specific matrix at each iteration (Caswell 2001, p. 396). We then
195 calculated the elasticities of $\log \lambda_s$ to changes in the mean and standard deviation of the stage-specific
196 vital rates (Tuljapurkar *et al.* 2003). We obtained the elasticities to the mean and standard deviation of
197 life-cycle components by summing the elasticities of the respective vital rates (Franco & Silvertown 2004;
198 **Appendix S1.4**).

199 *Step 3. Elevational patterns*

200 We used linear regressions to test for significant relationships between elevation and population
201 dynamics variables: mean life-cycle components, coefficients of variation of life-cycle components,
202 temporal correlations between life-cycle components, $\log\lambda_s$ and elasticities.

203 *Step 4. Stochastic life-table response experiment (SLTRE)*

204 We calculated the differences in $\log\lambda_s$ ($\Delta \log\lambda_s^{(m)}$) between each site m and a common reference site
205 defined by the means of vital rates over sites. The $\Delta \log\lambda_s^{(m)}$ were decomposed into the contributions
206 $C_{x_i, x_j}^{k, (m)}$ of differences of each descriptor k (mean μ ; coefficient of variation CV ; temporal correlations ρ ;
207 elasticities e) of stage-specific vital rates x_i (survival s_j , growth g_{ij} , reproduction F_{0j} , reproductive output
208 F_{1j} and recruit size F_{2i}) according to the SLTRE of Davison *et al.* (2013; **Appendix S1.6**):

$$209 \Delta \log\lambda_s^{(m)} \approx \sum_i C_{x_i}^{\mu, (m)} + \sum_{i,j} C_{x_i, x_j}^{CV, (m)} + \sum_{i,j} C_{x_i, x_j}^{\rho, (m)} + \sum_{i,j} C_{x_i, x_j}^{e, (m)} \quad (\text{eq. 3})$$

210 From this decomposition, we derived the *net contributions* C_l^k of each life-cycle component l and each
211 descriptor k by summing the $C_{x_i, x_j}^{k, (m)}$ according to the definition of life-cycle components given above. The
212 *total effect* C_l of each life-cycle component was calculated by summing the absolute values of its
213 contributions over the four descriptors, $C_l = \sum_k |C_l^k|$. Similarly, the *total effect* C^k of each descriptor was
214 calculated by summing the absolute values of its contributions over life-cycle components, $C^k = \sum_l |C_l^k|$.
215 Finally, we used linear regressions to test for significant relationships between elevation and the net
216 contributions C_l^k .

217 *Step 5. Demographic compensation*

218 To test for demographic compensation and its effectiveness in reducing the spatial variation in
219 population growth rates, we extended the approach of Villellas *et al.* (2015) to all descriptors of life-cycle
220 components. We tested for demographic compensation by testing for negative and positive Spearman

221 correlations between the net contributions C_i^k . The occurrence of a significantly higher number of
222 significant negative correlations (or a significantly lower number of significant positive correlations) than
223 expected by chance is indicative of demographic compensation and was tested by permuting 1000 times
224 the C_i^k over sites. This permutation test assesses only the occurrence of demographic compensation but
225 not its effectiveness in reducing the variance in $\log\lambda_s$ among sites, $\sigma_{\log\lambda_s}^2$. We then performed additional
226 randomization tests where we calculated $\sigma_{\log\lambda_s}^2$ following the permutation of each net contribution C_i^k
227 at a time (thus 28 parameters). Higher values of $\sigma_{\log\lambda_s}^2$ in the randomization indicated that the focal
228 parameter reduced $\sigma_{\log\lambda_s}^2$ through its negative correlations; conversely, lower values for $\sigma_{\log\lambda_s}^2$ indicated
229 that the focal parameter increased $\sigma_{\log\lambda_s}^2$ through its positive correlations. Finally, we ran a
230 randomization test where we permuted only those C_i^k that reduced $\sigma_{\log\lambda_s}^2$: this randomization
231 procedure eliminates as much as possible the negative correlations while preserving the important
232 positive correlations and indicates the overall effectiveness of demographic compensation (Villellas *et al.*
233 2015).

234 RESULTS

235 Step 1. Prediction of plant vital rates

236 Plant size had significant effects on all vital rates (**Table 2**). Size and reproductive output were positively
237 affected by *SoilVeg₂*, which was itself positively related to vegetative height and SLA of the surrounding
238 vegetation (**Appendix S2.1**). Survival was positively affected by mean temperature squared (T_{mean}^2),
239 while recruit size was negatively affected by temperature range (T_{range}). However, the models for survival
240 and recruit size had remarkably low explanatory power (marginal $R^2 = 0.07$ and 0.04 , respectively). All
241 vital rates showed considerable spatial and temporal variation that was unexplained by our
242 environmental variables (conditional R^2 larger than marginal R^2).

243 Step 2. Population dynamics analyses

244 On average, survival probability was $S = 0.5$ (except in GAL where $S = 0.75$), progressive growth (G^+) was
245 larger than retrogressive growth (G^-) and stasis ($G^=$), reproduction was $F_0 = 0.5$, reproductive output was
246 $F_1 = 12$ siliques and recruit size was $F_2 = 1.5$ stems (**Figure 1 and S5**). Coefficients of variations (CV) were
247 mostly comprised between 0.1 and 0.6 across all life-cycle components. Over all sites and pairs of life-
248 cycle components, we observed 21 (17%) significant negative temporal correlations and 21 (17%)
249 significant positive temporal correlations (**Figure S6**).

250 The stochastic population growth rate $\log\lambda_s$ was negative in all sites (**Table 1**). One site (GAL) had higher
251 $\log\lambda_s$ than the other sites. The largest elasticities of $\log\lambda_s$ to the temporal means of life-cycle components
252 were associated with S , while the elasticities to G^+ were the second-largest (**Figure 1**). The elasticities of
253 $\log\lambda_s$ to the standard deviation of life-cycle components were largest and negative for S , intermediate for
254 G^+ and F_1 , and smallest for G^- , $G^=$, F_0 and F_2 .

255 **Step 3. Elevational patterns**

256 Mean survival (S), retrogressive growth (G^-) and stasis ($G^=$) increased significantly with elevation (**Figure**
257 **1**), while mean progressive growth (G^+), reproductive output (F_1) and recruit size (F_2) decreased
258 significantly with elevation. The CV of S , G^- and $G^=$ decreased significantly with elevation.

259 While the elasticities to mean S did not change with elevation, the elasticities to mean G^+ significantly
260 decreased with elevation. The elasticities to the means of the other life-cycle components were much
261 smaller and showed significant positive (G^- and $G^=$) or negative (F_0 , F_1 and F_2) relationships with elevation.
262 The elasticities to the standard deviation of life-cycle components did not change significantly with
263 elevation, nor did the temporal correlations between life-cycle components.

264 The stochastic growth rate $\log\lambda_s$ did not change significantly with elevation (**Figure S7**).

265 **Step 4. Stochastic life-table response experiment (SLTRE)**

266 The SLTRE showed that all four descriptors of life-cycle components (means, coefficients of variation,
267 temporal correlations and elasticities) contributed to differences in $\log\lambda_s$ between sites (**Figure 2**). Means
268 had the largest total effects in all sites, but the other descriptors were not negligible and could account
269 for up to 50% of the difference in the stochastic growth rate (**Figure 2a**): the largest effects were due to
270 coefficients of variation, while elasticities and correlations had smaller effects. When looking at the total
271 effects of each life-cycle component (**Figure 2b**), the largest ones were due to survival (S) and
272 progressive growth (G^+), while the other life-cycle components had smaller effects.

273 The net contributions of means and coefficients of variation of S (C_S^μ and C_S^{CV}) increased (became more
274 positive) with elevation, while the net contributions of mean G^+ ($C_{G^+}^\mu$) decreased (became more
275 negative) with elevation (**Figure S8**).

276 **Step 5. Demographic compensation**

277 There were 18 significant positive correlations and 22 significant negative correlations between the net
278 contributions of life-cycle components across sites. This constitutes substantial evidence for the
279 existence of demographic compensation according to the criterion proposed by Villellas *et al.* (2015),
280 since the number of negative correlations was much higher than expected by chance (permutation test,
281 **Figure 3**).

282 The negative correlations involved all four descriptors of population dynamics. While the correlations
283 linking G^- , G^+ and G^+ together are trivial as they emerge from the same vital process (growth), the other
284 correlations are ecologically meaningful (**Figure S9**). Among these, there were significant negative
285 correlations involving mean life-cycle components (S , G^+ , F_1 and F_2), their coefficients of variation (S),
286 temporal correlations (S , G^- and G^+) and elasticities (G^- and G^+). Significant negative correlations linked
287 together the same descriptor of different life-cycle component (e.g. mean S and mean F_1), different
288 descriptors of the same life-cycle component (e.g. mean G^+ and its elasticity) and different descriptors of
289 different life-cycle components (the CV of S and the mean of G^+ , F_1 and F_2).

290 The parameters contributing the most to demographic compensation were mean S , mean G^+ and mean
291 F_1 , as their permutation generally increased the variance of $\log\lambda_s$ between sites, $\sigma_{\log\lambda_s}^2$ (**Figure 4a-d**).
292 Conversely, the permutation of the CV of S led to smaller $\sigma_{\log\lambda_s}^2$, indicating that this parameter increases
293 the variance in $\log\lambda_s$ relative to what would be expected by chance; this was the result of the numerous
294 positive correlations involving the CV of S (**Figure 3**). The other parameters did not change $\sigma_{\log\lambda_s}^2$
295 considerably. Randomizing only the parameters that reduced the variance in $\log\lambda_s$ between sites
296 indicated that the observed $\sigma_{\log\lambda_s}^2$ was 59% of the median $\sigma_{\log\lambda_s}^2$ expected under the hypothesis of
297 minimal negative correlations, but not significantly smaller ($p = 0.17$; **Figure 4e**).

298 DISCUSSION

299 In this work, we studied variation in population dynamics of *A. alpina* across most of its elevational range
300 in the European Alps (2000m). Contrary to the expectation that peripheral populations have lower
301 demographic performance than central populations (Pironon *et al.* 2017), *A. alpina* showed surprisingly
302 little variation in population growth rates $\log\lambda_s$ across its full elevational range. Conversely, most life-
303 cycle components significantly varied with elevation. We showed that this pattern could be partly
304 explained by demographic compensation, *i.e.* negative correlations between the contributions of
305 different life-cycle components to spatial differences in $\log\lambda_s$. In particular, compensatory effects across
306 the elevational range did not arise only through opposite spatial patterns in mean vital rates, but also in
307 their temporal variation, elasticities and temporal correlations. This highlights a previously overlooked,
308 but potentially important, role of stochastic processes in offsetting mean changes in vital rates and
309 stabilizing population dynamics at range margins. We now discuss the origin, significance and
310 generalities of the patterns of demographic compensation observed in this study.

311 The origin of negative correlations between the different descriptors of life-cycle components should be
312 searched in their patterns of variation along the elevational gradient (**Figure 1**). First, mean vital rates
313 changed in opposite directions: survival (S) increased along the elevational gradient while reproductive
314 output (F_1) decreased, resulting in a negative correlation between C_S^μ and $C_{F_1}^e$ (**Figure S9**). However,
315 stochastic descriptors also contributed to demographic compensation along elevation. For example, the
316 decrease in mean progressive growth (G^+), by itself, should have resulted in lower population growth
317 rates $\log\lambda_s$ at higher elevations. However, the elasticity to mean G^+ also decreased with elevation and
318 counterbalanced the negative effects of lower G^+ , because smaller elasticities dampen the effects of
319 changes in life-cycle components on $\log\lambda_s$. The CV of survival also decreased with elevation, further
320 offsetting the negative effects of lower G^+ , since smaller CV have positive effects on $\log\lambda_s$. The resulting

321 negative correlations between the net contributions of these parameters to $\log\lambda_s$ (namely, between $C_{G^+}^\mu$
322 and $C_{G^+}^e$ and between $C_{G^+}^\mu$ and C_S^{CV}) partly explain why population growth rates did not change with
323 elevation despite marked elevational gradients in life-cycle components. Overall, the observed patterns
324 are in agreement with the known higher occurrences of smaller and longer lived species and individuals
325 at higher elevations (Nobis & Schweingruber 2013; Laiolo & Obeso 2017) and higher variability of survival
326 at lower elevations (Angert 2009).

327 Such elevational patterns could be due to opposite responses of vital rates to common environmental
328 drivers (Knops *et al.* 2007). The main environmental driver of variation in growth and reproductive
329 output was *SoilVeg₂*, which summarizes variation in specific leaf area (SLA) and vegetative height
330 (**Appendix S2.1**), meaning that *A. alpina* tends to grow larger and produce more fruits when the
331 surrounding vegetation is composed of tall plants with large SLA. This relationship could indicate a
332 response to high competitive pressure or a common effect of temperature, because SLA and vegetative
333 height in plants tend to increase with temperature and decrease with elevation (Moles *et al.* 2014; Read
334 *et al.* 2014; Rosbakh *et al.* 2015). In contrast, the environmental drivers of survival are not easy to
335 identify, because the statistical model linking plant survival probability to environmental variables had
336 very low explanatory power. These results seem corroborated by a common garden experiment using
337 the same six populations as this study, which found that temperature was significantly associated with
338 total fruit length (a measure of reproductive output) but not with survival (de Villemereuil *et al.* 2018).
339 Elevational patterns in survival, growth and reproductive output could also be driven by other
340 environmental factors not considered in our analysis, such as soil phosphorus content, diversity of root
341 microbiota or herbivore damage, all of which affect various traits of *A. alpina* across its range (Almario *et al.*
342 2017; Buckley *et al.* 2019). Negative correlations between life-cycle components could also be due to
343 energetic trade-offs and structural constraints (Williams *et al.* 2015). In *A. alpina*, higher rates of
344 flowering are associated with reduction of plant survival, because all stems wilt and die after setting

345 seeds, to the point that mutants for perpetual flowering show an annual life-cycle (Wang *et al.* 2009).
346 Slower rates of stem production and/or lower rates of flowering could thus increase the longevity of the
347 entire plant, resulting in negative correlations between growth, reproduction and survival.

348 Spatial patterns in elasticity are not very documented, but increasing elasticities to survival with
349 elevation could result from their positive correlation with longevity (Silvertown *et al.* 1993; Franco &
350 Silvertown 2004) and from the positive correlation between longevity and elevation (Nobis &
351 Schweingruber 2013). In contrast, decreasing elasticities to fecundity and growth with elevation, as
352 found in our study, could be expected given that these elasticities correlate with SLA (Adler *et al.* 2014)
353 and SLA is known to decrease with elevation (Read *et al.* 2014). However, within-species patterns of
354 elasticities are also influenced by the level of environmental disturbance (Oostermeijer *et al.* 1996;
355 Silvertown *et al.* 1996), which may not show consistent variation with elevation.

356 The correlations between life-cycle components involved all descriptors of population dynamics but their
357 effectiveness for reducing the variance in $\log\lambda_s$ ($\sigma_{\log\lambda_s}^2$) was higher in the case of mean life-cycle
358 components. The effectiveness of a single descriptor for reducing $\sigma_{\log\lambda_s}^2$ through demographic
359 compensation depends on the strength and number of its negative correlations relative to its positive
360 correlations (**Figure 3**) and its contribution to the differences in $\log\lambda_s$ between sites, $\Delta\log\lambda_s$ (**Figure 2**).
361 Only parameters making large contributions change $\sigma_{\log\lambda_s}^2$ through their correlations, decreasing it when
362 most of their correlations are strong and negative. Mean progressive growth was the most important
363 parameter for demographic compensation by offsetting variation in survival. Mean survival and mean
364 reproductive output were the second most important parameters, thanks to their large contributions to
365 $\Delta\log\lambda_s$ and the negative correlation between them. Conversely, temporal correlations and elasticities
366 showed many significant negative correlations but they were not as important for demographic
367 compensation because the net contributions to $\Delta\log\lambda_s$ were small, in line with what is observed in other

368 plant species (Jongejans *et al.* 2010; Compagnoni *et al.* 2016; Davison *et al.* 2019). Finally, the CV of
369 survival made relatively large contributions to $\Delta\log\lambda_s$, but showed too many positive correlations that led
370 to an increase of $\sigma_{\log\lambda_s}^2$ rather than a reduction.

371 Although our results are comparable to findings over multiple species in the deterministic case (Villellas
372 *et al.* 2015), our study is the first assessing demographic compensation in a stochastic framework.

373 Assessing whether the results obtained here are representative of other species will require additional
374 studies quantifying both the contributions of all descriptors of population dynamics to $\Delta\log\lambda_s$ and their
375 pairwise correlations. The first exercise has been done by Davison *et al.* (2019) on a set of 62 species,
376 showing that more than one quarter of contributions to $\Delta\log\lambda_s$ can be attributed to the effect of
377 coefficients of variations, elasticities and temporal correlations. However, the importance of these
378 descriptors of population dynamics for demographic compensation remains unknown, as it depends
379 critically on the relative number and strength of negative vs. positive correlations in which they are
380 involved.

381 Even with demographic compensation, the stochastic population growth rate was negative in all sites,
382 indicating that populations are projected to decline in size and eventually go extinct locally. However, *A.*
383 *alpina* could persist thanks to germination from its persistent seed bank and immigration from other
384 sites (Hastings & Botsford 2006). Its frequent occurrence in unstable sites suggests that populations
385 could show an extinction-recolonization dynamics typical of metapopulations (Ouborg & Eriksson 2004).
386 The inclusion of a seed bank led to higher, sometimes positive population growth rates and confirmed
387 the existence of demographic compensation (**Appendix S2.2**). The effects of immigration are more
388 difficult to study in absence of estimates of seed dispersal rates, but the strong spatial genetic structure
389 of the populations ($F_{ST} = 0.6$, de Villemereuil *et al.* 2018) suggests that dispersal rates might be low. The
390 patterns of demographic compensation revealed here could thus be different in models integrating
391 empirical estimates of seed dormancy and germination rates and extinction-recolonization dynamics,

392 potentially unmasking greater importance for coefficients of variation, elasticities and temporal
393 correlations.

394 So far, demographic compensation has been discussed mainly in terms of spatial variation in mean vital
395 rates (Doak & Morris 2010; Villellas *et al.* 2015; Sheth & Angert 2018). Our study is the first to highlight
396 that temporal variation, elasticities and temporal correlations can be involved in demographic
397 compensation, even if their effect was smaller than that of means. Nonetheless, temporal variation in
398 vital rates could become more important under future expected increasing frequencies of extreme
399 climatic events (Meehl & Tebaldi 2004; Schär *et al.* 2004), such as summer heatwaves and drought, that
400 can cause large temporal variation in vital rates (Smith 2011; Andrello *et al.* 2012). Assessing the
401 importance of all descriptors of population dynamics for demographic compensation could thus provide
402 a more complete understanding of the dynamics of elevational as well as geographical species ranges in
403 a context of global change.

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563

564 **SUPPORTING INFORMATION**

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566 Online Library (www.ecologyletters.com).

567

568 Figure legends

569 **Figure 1. Elevational patterns in life-cycle components and elasticities.** Elevational patterns in mean
570 life-cycle components, coefficients of variation (CV) of life-cycle components, elasticities to means (μ)
571 and elasticities to standard deviation (σ) of life-cycle components. Life-cycle components are survival (S),
572 retrogressive growth (G^-), stasis ($G^=$), progressive growth (G^+), reproduction (F_0), reproductive output (F_1)
573 and recruit size (F_2). Dots are mean values and bars extend over 95% confidence intervals. The blue lines
574 are fitted linear regressions between values and elevation, and the gray areas are 95% confidence
575 intervals. Solid lines indicate significant regressions ($p < 0.05$). Confidence intervals and significance
576 values were calculated by randomly sampling statistical models over 200 bootstrapped demographic
577 datasets and 10 resampled imputed climatic datasets

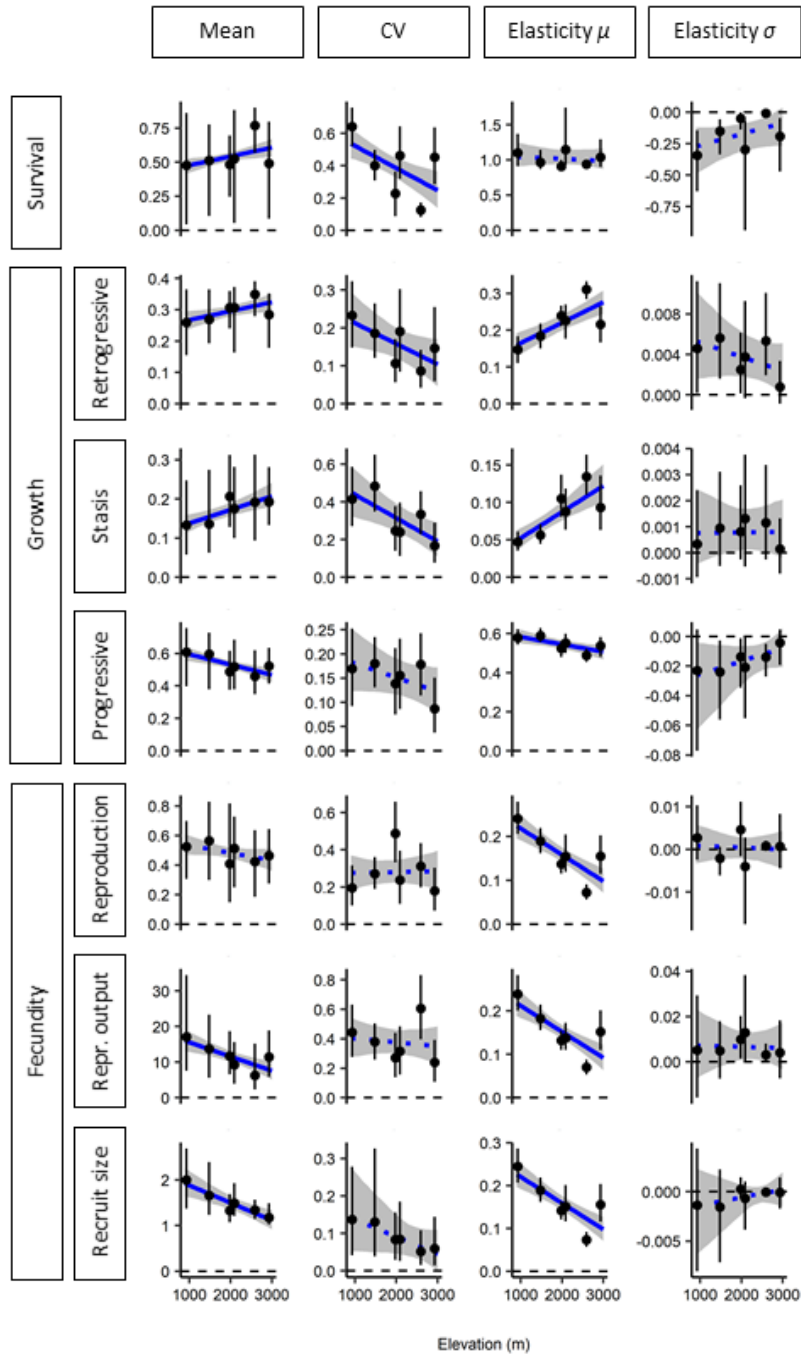
578 **Figure 2. Stochastic life-table response experiment (SLTRE).** Total effects of each descriptor (a) and life-
579 cycle component (b) to differences in stochastic population growth rates ($\log\lambda_s$) between the focal site
580 and a reference site constructed by taking the mean of vital rates over all sites. (c) to (h), net
581 contributions C_l^k of each descriptor k of each life-cycle component l to the difference in $\log\lambda_s$. Negative
582 and positive contributions are plotted separately. Colours indicate the descriptor (μ , means; E ,
583 elasticities; CV , coefficients of variation; ρ , temporal correlations) or the life-cycle component (S,
584 survival; G^- , retrogressive growth; $G^=$, stasis; G^+ , progressive growth; F_0 , reproduction; F_1 , fecundity; F_2 ,
585 recruit size).

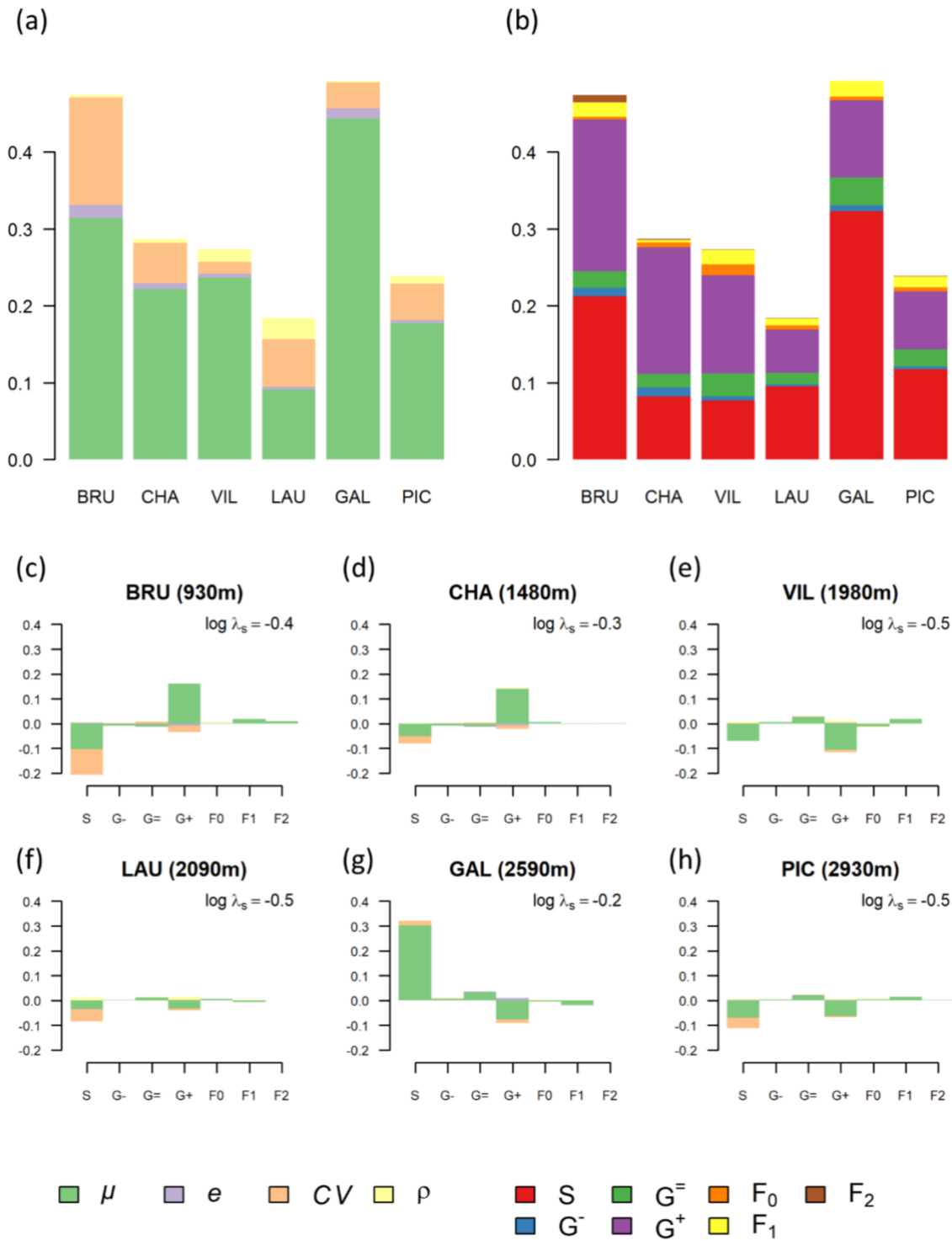
586 **Figure 3. Demographic compensation. Correlogram of Spearman's correlation coefficients between the**
587 **net contributions of different descriptors of life-cycle components to differences in stochastic population**
588 **growth rates ($\log\lambda_s$) between sites (SLTRE contributions).** Negative correlations are in red, positive
589 correlations are in blue. Boxes with thicker borders and an asterisk indicate significant correlations at $p <$
590 0.05. The insets show the number of observed significant positive and negative correlations (vertical

591 dotted lines) compared to the distribution of the number expected by chance obtained through a
592 permutation test (histograms). See Figure 2 for definitions of descriptors and life-cycle components.

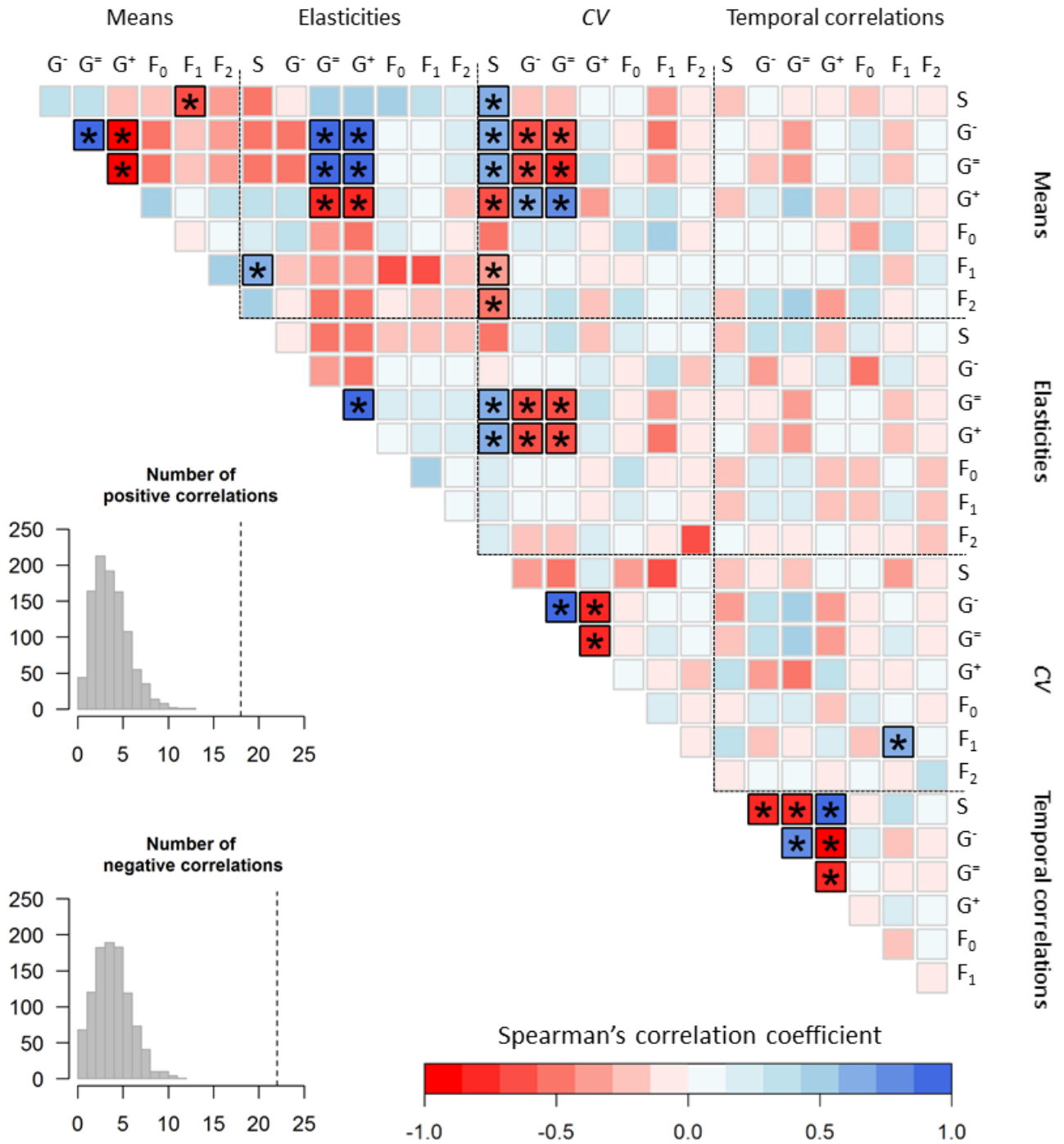
593 **Figure 4. Effectiveness of demographic compensation.** (a), variance of population growth rate $\log\lambda_s$
594 between sites, $\sigma_{\log\lambda_s}^2$, obtained by permuting each descriptor of each life-cycle component at a time.
595 Dots are mean values and bars extend over 95% confidence intervals over 1000 permutations. Values
596 higher than the observed $\sigma_{\log\lambda_s}^2$ (horizontal dashed line) indicate that the corresponding parameter
597 effectively reduces $\sigma_{\log\lambda_s}^2$ through demographic compensation. (b), observed $\sigma_{\log\lambda_s}^2$ (vertical dotted
598 lines) compared to the distribution of $\sigma_{\log\lambda_s}^2$ expected by chance obtained through permuting only the
599 parameters effectively reducing it (histograms). See Figure 2 for definitions of descriptors and life-cycle
600 components.

601





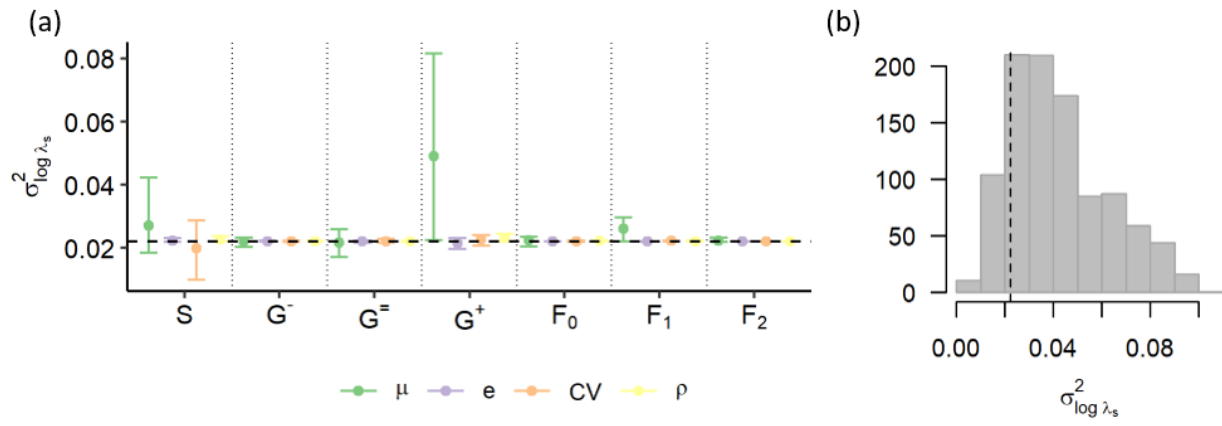
606 **FIGURE 3**



607

608

609 **FIGURE 4**



610

611

Table 1. Characteristics of the study sites.

Site	BRU	CHA	VIL	LAU	GAL	PIC
Longitude	5.61112	5.59267	5.57083	6.39034	6.40375	6.38426
Latitude	45.15065	45.07117	45.01809	45.02846	45.06049	45.06385
Elevation (m)	930	1480	1980	2090	2590	2930
Aspect	South	North	South	North	North	South
Habitat	Calcareous scree	Calcareous grassland, scree	Calcareous scree	Schists, torrent	Calcareous scree	Schistose scree
Initial N	46	145	104	90	110	50
Number of plots	2	3	3	3	3	4
T_{mean}	14.7 (12.8, 17.5)	15.7 (12.9, 18.2)	12.9 (9.3, 17.5)	10.4 (8.0, 12.1)	7.7 (5.3, 10.3)	9.1 (5.9, 12.1)
T_{range}	11 (6.0, 18.6)	16.9 (11.5, 21.9)	15.9 (9.7, 36.1)	6.3 (3.1, 9.6)	8.1 (5.8, 13.3)	16.3 (11.8, 23.2)
$\log\lambda_s$	-0.4 (-0.5, -0.2)	-0.3 (-0.5, -0.2)	-0.5 (-0.6, -0.4)	-0.5 (-0.8, -0.3)	-0.2 (-0.2, -0.1)	-0.5 (-0.8, -0.3)

N , number of individuals. Daily mean temperature (T_{mean}) and daily temperature range (T_{range}) were measured with *in-situ* data-loggers. Values are means and (minimum and maximum) over plots and years for the month of July. Means and 95% confidence interval for the stochastic population growth rate ($\log\lambda_s$) were calculated by randomly sampling the values calculated using matrix populations models constructed using predicted vital rates from 200 bootstrapped demographic datasets and 10 resampled imputed datasets. The N per site per year is shown in

[Figure S2](#).

Table 2. Statistical analysis of plant vital rates.

Predictor	Survival		Growth		Reproduction		Reproductive output		Recruit size	
	mean	95% CI	mean	95% CI	mean	95% CI	mean	95% CI	mean	95% CI
Fixed effects										
Intercept	0.50	(0.31, 0.72)	1.35	(1.24, 1.44)	0.75	(0.35, 1.26)	1.05	(0.99, 1.10)	-0.76	(-1.11, -0.50)
<i>SoilVeg</i> ₁	-0.27	(-0.69, 0.19)	0.17	(-0.18, 0.35)	0.10	(-0.36, 0.77)	0.03	(-0.06, 0.15)	0.57	(-0.16, 1.07)
<i>SoilVeg</i> ₂	-0.29	(-0.77, 0.05)	0.17	(0.03, 0.38)	0.14	(-0.26, 0.69)	0.10	(0.01, 0.18)	-0.04	(-0.80, 0.49)
Plant size	0.79	(0.47, 1.09)	1.26	(1.09, 1.43)	3.78	(3.04, 4.61)	0.58	(0.49, 0.69)	-	-
(Plant size) ²	-0.56	(-0.88, -0.3)	-0.71	(-0.87, -0.57)	-1.37	(-2.21, -0.74)	-0.26	(-0.37, -0.18)	-	-
<i>T</i> _{mean}	-3.52	(-5.08, 0.22)	0.35	(-0.24, 1.75)	0.04	(-2.34, 2.53)	-0.06	(-0.58, 0.41)	0.55	(-2.47, 3.33)
(<i>T</i> _{mean}) ²	3.37	(0.17, 5.04)	-0.51	(-1.76, 0.16)	-0.13	(-2.66, 2.24)	-0.02	(-0.42, 0.52)	0.52	(-2.67, 3.20)
<i>T</i> _{range}	-0.40	(-0.95, 0.05)	0.01	(-0.23, 0.25)	0.33	(-0.10, 1.19)	0.11	(0.00, 0.20)	-0.63	(-1.78, -0.07)
Random effects										
Site (Intercept)	0.00	(0.00, 0.55)	0.08	(0.00, 0.55)	0.00	(0.00, 0.72)	0.12	(0.00, 0.23)	0.00	(0.00, 0.40)
Year (Intercept)	0.51	(0.22, 0.86)	0.41	(0.33, 0.50)	1.09	(0.84, 1.40)	0.15	(0.11, 0.19)	0.00	(0.00, 0.70)
Year (<i>SoilVeg</i> ₂)	1.27	(0.82, 1.83)	-	-	-	-	-	-	-	-
Year (Intercept * <i>SoilVeg</i> ₂)	0.15	(-0.48, 0.98)	-	-	-	-	-	-	-	-
Plot (Intercept)	-	-	-	-	1.28	(0.87, 1.88)	-	-	-	-
Plot (Plant size)	-	-	-	-	1.52	(0.85, 2.56)	-	-	-	-
Plot (Intercept * Plant size)	-	-	-	-	0.95	(0.74, 1.00)	-	-	-	-
Residual	-	-	1.62	(1.39, 1.89)	-	-	0.36	(0.34, 0.38)	2.61	(0.86, 13436)
Marginal <i>R</i> ²	0.07	(0.03, 0.12)	0.25	(0.2, 0.31)	0.46	(0.38, 0.56)	0.44	(0.36, 0.53)	0.04	(0.00, 0.10)
Conditional <i>R</i> ²	0.41	(0.29, 0.56)	0.36	(0.3, 0.49)	0.80	(0.69, 0.88)	0.57	(0.51, 0.64)	0.05	(0.02, 0.18)

For each of the five vital rates, the table reports the standardized coefficients of fixed effect, the standard deviation of random effects (intercepts and slopes), the correlations between random intercept and slopes and marginal and conditional R^2 (Nakagawa *et al.* 2017). Only the random effects that were retained after model selection on the random structure are shown. Means and 95% confidence intervals were calculated by randomly sampling statistical models over 200 bootstrapped demographic datasets and 10 resampled imputed datasets. The predictors whose confidence intervals do not overlap with zero are in **bold**.