Sensitivity of a calving glacier to ice–ocean interactions under climate change: new insights from a 3-D full-Stokes model

Joe Todd1,2, Poul Christoffersen1, Thomas Zwinger3, Peter Råback3, and Douglas I. Benn2

1Scott Polar Research Institute, University of Cambridge, Cambridge, UK
2Department of Geography and Sustainable Development, University of St Andrews, St Andrews, UK
3CSC-IT Center for Science, Espoo, Finland

Correspondence: Joe Todd (jat39@st-andrews.ac.uk)

Received: 24 January 2019 – Discussion started: 20 February 2019
Revised: 17 May 2019 – Accepted: 20 May 2019 – Published: 14 June 2019

Abstract. Iceberg calving accounts for between 30 % and 60 % of net mass loss from the Greenland Ice Sheet, which has intensified and is now the single largest contributor to global sea level rise in the cryosphere. Changes to calving rates and the dynamics of calving glaciers represent a significant uncertainty in projections of future sea level rise. A growing body of observational evidence suggests that calving glaciers respond rapidly to regional environmental change, but predictive capacity is limited by the lack of suitable models capable of simulating calving mechanisms realistically. Here, we use a 3-D full-Stokes calving model to investigate the environmental sensitivity of Store Glacier, a large outlet glacier in West Greenland. We focus on two environmental processes: undercutting by submarine melting and buttressing by ice mélange, and our results indicate that Store Glacier is likely to be able to withstand moderate warming perturbations in which the former is increased by 50 % and the latter reduced by 50 %. However, severe perturbation with a doubling of submarine melt rates or a complete loss of mélange destabilises the calving front in our model runs. Furthermore, our analysis reveals that stress and fracture patterns at Store’s terminus are complex and varied, primarily due to the influence of basal topography. Calving style and environmental sensitivity vary greatly, with propagation of surface crevasses significantly influencing iceberg production in the northern side, whereas basal crevasses dominate in the south. Any future retreat is likely to be initiated in the southern side by a combination of increased submarine melt rates in summer and reduced mélange strength in winter. The lateral variability, as well as the importance of rotational and bending forces at the terminus, underlines the importance of using the 3-D full-Stokes stress solution when modelling Greenland’s calving glaciers.

1 Introduction

Iceberg calving and submarine melt are important ablation mechanisms in the cryosphere, collectively accounting for around half of the net annual ice loss in Greenland over the last decade (van den Broeke et al., 2009) and more (up to two-thirds) when warm subtropical waters periodically flow into coastal seas and fjords (Rignot and Kanagaratnam, 2006; Holland et al., 2008; Straneo et al., 2010; Christoffersen et al., 2011). The remaining loss is caused by surface melting (Enderlin et al., 2014; van den Broeke et al., 2016). In Antarctica, ice sheet mass loss is partitioned evenly between calving flux and ablation tied to basal melting of large ice shelves (Depoorter et al., 2013; Rignot et al., 2013).

The importance of calving as a contributor to global sea level rise is demonstrated by the sustained retreat, acceleration and dynamic thinning triggered at the termini of many Greenlandic outlet glaciers in the past 2 decades (Howat et al., 2005; Holland et al., 2008; Rignot and Kanagaratnam, 2006). Recent observational studies (James et al., 2014; Murray et al., 2015; Chudley et al., 2019; Medrzycka et al., 2016; Luckman et al., 2015) have captured the calving process in unprecedented detail, yet the physical links between calving and climate remain poorly understood.

Several environmental and internal factors are hypothesised to affect calving, which occurs when fractures propagate through glacier termini in response to growing stresses...
The dynamics of outlet glaciers strongly modulate the effect of external forcing on calving (Moon and Joughin, 2008; Schild and Hamilton, 2013). The fact that nearby glaciers may respond differently to the same regional-scale climatic shifts is evidence of this. Bedrock topography (Fig. 1c) strongly influences glacier dynamics, providing both basal and lateral pinning points, both of which tend to define stable terminus positions (Benn et al., 2007a). Related to this, spatial and temporal variability in basal friction (Fig. 1d), which is a function of subglacial hydrology as well as glacier geometry, has been suggested as a potential first-order control on calving (Benn et al., 2007a).

A range of approaches have been developed to represent calving processes in numerical models (e.g. Nick et al., 2010; Cook et al., 2014; Todd and Christoffersen, 2014; Krug et al., 2014; Morlighem et al., 2016). These typically adopt simplified representations of stress and calving processes, and are generally tuned against observations rather than independently validated. Recently, calving has been incorporated into a 3-D full-Stokes model (Todd et al., 2018), allowing calving processes to be simulated in much greater detail than previously possible. In this study, we use this model (Elmer/Ice) to investigate the environmental sensitivity of Store Glacier (Fig. 2), a large outlet glacier flowing into Uummannaq Bay in West Greenland. Store Glacier (henceforth referred to as “Store”) is 5 km wide at the terminus, where ice velocity reaches 20 m d\(^{-1}\). The glacier has remained in a stable position for at least the past 40 years (Howat et al., 2010), through periods when several nearby glaciers have undergone concurrent retreat. While interannually stable, Store’s terminus displays a distinct seasonal advance and retreat cycle of up to 1 km; Todd et al. (2018) were able to reproduce the observed calving seasonality of Store Glacier by applying only two types of environmental forcing: undercutting of the terminus by submarine melting and buttressing from seasonally rigid ice mélange. That study found buttressing by ice mélange to be the primary driver of observed seasonal advance and retreat, while submarine melting prevents the terminus from advancing beyond its current stable position.

Here, we extend the analysis of Todd et al. (2018) by investigating the sensitivity of iceberg calving at Store, with the aim of understanding how the glacier will respond to future changes in environmental forcings associated with a warming climate. With calving simulated over multiple years and with individual calving events resolved in 3-D, we present an analysis which is unprecedented in detail. We show that a doubling of submarine melting at Store Glacier’s terminus would likely lead to accelerated calving and retreat, predominantly in the floating southern half of the glacier’s terminus. We find that the distribution of submarine melting is critical to the glacier’s stability, and that the loss of winter–spring ice mélange buttressing could have knock-on effects on summer stability. We also find that subglacial topography is critical in determining calving dynamics and glacier stability.
2 Methods

To determine climatic influences on Store Glacier’s calving, ice flow and stability, we perform sensitivity experiments in which calving in our model responds to changed environmental conditions. The starting point is a present-day control simulation which includes three types of climate forcing on the terminus: (1) distributed submarine ice-wall melting at the submerged portion of the terminus, (2) concentrated submarine melting associated with convective plumes forming at two known locations where glacial meltwater is subglacially discharged, and (3) ice mélange buttressing.

2.1 Environmental forcing in control simulation

Submarine ice-wall melting occurs when cold, fresh, buoyant subglacial meltwater is discharged into warm and dense fjord water, creating a forced convective plume (Fig. 1b); melt rates are linked to rate of subglacial discharge and the temperature and salinity of the fjord water (Xu et al., 2013; Jenkins, 2011; Slater et al., 2015). Patterns of submarine ice-wall melting are complex (Chauché et al., 2014; Chauché, 2016; Rignot et al., 2015), but can be decomposed into distributed (“planar”) plume melting, driven by distributed subglacial discharge across the entire front, and localised concentrated (“conical”) plume melting from highly channelised discharge (Fig. 1a). As in Todd et al. (2018) we investigate the effects of the undercutting caused by these endmembers, using a numerical model based on buoyant plume theory (Slater et al., 2016). This plume model, which runs in MATLAB, produces vertical melt profiles from fjord temperature and salinity profiles and subglacial hydrological discharge, which we then apply to the calving front in Elmer/Ice. Here, we use temperature and salinity profiles from CTD casts in Store Glacier’s fjord (Chauché et al., 2014). However, rather than supplying subglacial discharge as an input to the plume model, we define target melt rates, described below, and run the model multiple times to find realistic melt distributions which match the target.

Chauché (2016) estimated mean submarine melt rates at Store to be 3.1 and 1.3 m d$^{-1}$ for summer and winter, respectively. For the control experiment, we use these observationally derived melt rates as targets for the distributed plume model; this allows us to determine realistic vertical melt profiles from estimates of spatially averaged melt rate. Summer melt profiles are applied in June, July, and August and winter profiles are applied from September to May. We apply these vertical profiles uniformly across the front. For the sensitivity experiments, we increase these target melt rates as described in Sect. 2.2 below.

Concentrated plume melting occurs in summer (JJA) when runoff from the surface is routed along the bed and discharged subglacially into the fjord through large channels. In winter (all other months) we assume that the subglacial hydrology consists of a wholly distributed system. Concentrated plumes are applied as conical melt features that expand as they rise, reaching a radius of 162 m at the surface. Concentrated plume melting is included at two known locations along the calving front (Fig. 3b) where plumes are frequently observed as sediment-laden water reaching the surface of the fjord in summer. As with distributed melting, we use the numerical plume model to determine vertical melt and width profiles for the two concentrated plumes, although in this case we prescribe a maximum in-plume melt rate (12 m d$^{-1}$ in the control experiment). We use a target maximum melt rate, as opposed to mean melt rate, as direct observations of maximum melt rates are available for the concentrated plumes, whereas estimates of distributed melt rate are average values across the entire front (Chauché, 2016). While the maximum rate of concentrated melting is high relative to that of distributed melting, concentrated plumes are spatially confined to a relatively small portion of the submerged ice front (3 %), whereas the distributed plume melting covers the entire ice wall and therefore melts more ice.

The third environmental forcing we consider is proglacial ice mélange, which forms a seasonally rigid mixture of icebergs, bergy bits and sea ice in front of most Greenlandic out-
2.2 Sensitivity analysis

In the sensitivity experiments, we examine changes to all three types of environmental forcing, as well as their combined effect (Table 1). We run 5-year simulations in which we modify the magnitude of these environmental processes, consistent with an ongoing trend of warming ocean and atmosphere, in order to test the glacier’s short-term response to these perturbations. Distributed and concentrated melt rates are scaled separately by a factor of 1.5 (Runs MD1, MC1) and 2.0 (Runs MD2, MC2) in order to test the glacier’s response to 50% and 100% increases. For the distributed plume experiments (MD1, MD2), we recalculated the melt profiles to match the new, scaled target melt rate. For concentrated plume melting (MC1 and MC2), we found it difficult to achieve the desired maximum melt rates with the concentrated plume model, due to the nonlinear relationship between subglacial discharge and melt rate; melt rates scale sublinearly with subglacial discharge (Xu et al., 2013), meaning that disproportional amounts of additional discharge were needed to double the maximum melt rate. Thus, we instead directly scale the present-day concentrated plume melt profile from the control experiment.

The ice mélange thickness is scaled by factors of 0.5 (Run MM1) and 0 (Run MM2) in the sensitivity experiments, creating scenarios which reflect halving of mélange thickness and a complete loss of the mélange, respectively. Finally, we combine the scaling of all three forcings in intermediate (Runs MA1) and severe (Runs MA2) perturbation scenarios. We also run a control simulation (Run CONTROL) in which the environmental forcings are identical to those in Todd et al. (2018). All of the sensitivity experiments outlined above were run for 5 years. In two of our extreme forcing scenarios (MD2, MA2), the rapid and extensive retreat caused the calving model to break down irrecoverably. This occurs due to the sudden change in geometry; the remeshing algorithm struggles with the extreme change, which in turn leads to instability in the free surface evolution. In future work, we intend to overhaul the remeshing algorithm to improve the robustness of the model.

2.3 3-D calving model

We use Elmer/Ice’s 3-D calving implementation, presented in Todd et al. (2018), to investigate Store Glacier’s sensitivity to changes in environmental forcing. The model implements the crevasse depth calving criterion (Benn et al., 2007b; Nick et al., 2010), modified to take advantage of the full-Stokes stress solution and third dimension (Todd et al., 2018). Calving is predicted to occur either when surface and basal crevasses meet, separating an iceberg from the terminus, or when surface crevasses reach the waterline, which is assumed to lead to hydrofracturing and full crevasse penetration. Crevasse penetration is computed using a zero stress condition (Nye, 1957), such that open crevasses exist wher-
Table 1. Simulations performed in the sensitivity analysis. Run codes begin “M” to distinguish magnitude perturbations as opposed to duration (D) perturbations (Sect. S1 in the Supplement). Two simulations each were performed for mélange (M), distributed melt (D), concentrated melt (C) and all (A) forcings. The digit refers to either the first or second perturbation, where the second is more “severe”. The parameter values which deviate from the control simulation are shown in italics (i.e. the active perturbation).

<table>
<thead>
<tr>
<th>Run code</th>
<th>Ice mélange thickness (m)</th>
<th>Submarine melt</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Dist. summer ave. (m d(^{-1}))</td>
<td>Dist. winter ave. (m d(^{-1}))</td>
</tr>
<tr>
<td>Control</td>
<td>140</td>
<td>3.1</td>
</tr>
<tr>
<td>MM1</td>
<td>70</td>
<td>3.1</td>
</tr>
<tr>
<td>MM2</td>
<td>0</td>
<td>3.1</td>
</tr>
<tr>
<td>MD1</td>
<td>140</td>
<td>4.65</td>
</tr>
<tr>
<td>MD2</td>
<td>140</td>
<td>6.2</td>
</tr>
<tr>
<td>MC1</td>
<td>140</td>
<td>3.1</td>
</tr>
<tr>
<td>MC2</td>
<td>140</td>
<td>3.1</td>
</tr>
<tr>
<td>MA1</td>
<td>70</td>
<td>4.65</td>
</tr>
<tr>
<td>MA2</td>
<td>0</td>
<td>6.2</td>
</tr>
</tbody>
</table>

ever a net tensile stress exists in some direction. We opt for the Nye approach as opposed to a more complex linear elastic fracture mechanics (LEFM) approach because theory suggests that the two approaches are consistent when crevasses are closely spaced (Weertman, 1973). We define the effective principal stress (EPS) for both surface and basal crevasses:

\[
\text{EPS}_{\text{surf}} = \sigma_1, \\
\text{EPS}_{\text{basal}} = \sigma_1 + P_w,
\]

where \(\sigma_1\) is the largest principal stress and \(P_w\) is water pressure acting to open basal crevasses. Water pressure in basal crevasses near the terminus is taken equal to that in the proglacial fjord, assuming an efficient drainage system links the subglacial hydrology to the fjord. The calving algorithm, as well as the model’s remeshing and time evolution, are described in detail and discussed in Todd et al. (2018).

2.4 Domain and boundary conditions

Model domain and boundary conditions are identical to those in Todd et al. (2018), aside from changes to the climate forcings described below. The model domain extends 112 km inland, and is laterally constrained by Store’s ice-flow catchment (Fig. 2a). The domain is discretised into a mesh with 15 vertical layers, with horizontal resolution varying from 100 m at the terminus to 2 km in the interior. We solve the full-Stokes equations for ice flow using Glen’s flow law (Cuffey and Patterson, 2010). On the inflow boundary, velocity is set equal to mean observed velocity from TerraSAR-X imagery (April 2014–April 2015). A no-penetration condition is imposed on the lateral boundaries, with a slip coefficient of \(1.0 \times 10^{-3}\) for ice–ice interfaces and \(1.0 \times 10^{-2}\) for ice–rock interfaces. A similar condition applies to the base of the ice, but inverse methods (Gillet-Chaulet et al., 2012) are used to determine basal slip coefficient (\(\beta\)), which varies through the season, in order to reproduce observed seasonal patterns of velocity. Where the model predicts that ice is floating, basal traction disappears (\(\beta = 0\)) and the bottom surface is permitted to lift off the bed. On the calving front, external pressure from the fjord water is applied to ice below sea level. Ice above the waterline is stress free, as is the upper ice surface. Evolution of the upper ice surface is computed throughout the simulation, and surface mass balance is applied as an annual average, determined from RACMO data (Noël et al., 2015). The calving model runs on a nominal 0.01-year time step, although when large calving events occur (> \(1.0 \times 10^6\) m\(^3\)), we effectively pause the time evolution in order to allow for secondary calving events. More details of this time-stepping scheme are available in Todd et al. (2018).

A novel feature of our model is that the shape of the calving front is allowed to evolve freely in response to flow, submarine melting and icebergs breaking off in discrete calving events. As the model is 3-D, we are not restricted to assuming a vertical calving front, meaning we are able to directly simulate the stress effects of submarine melt undercutting. We assume, however, that crevasses propagate vertically, such that freshly calved sections of the ice front are vertical until deformation and melting reintroduce undercutting.

2.5 Model spin-up

The simulations presented here run from the end of the 5-year “present-day” simulation presented in Todd et al. (2018), which in turn runs from the end of a 300-year spinup in which the calving front is held fixed and the ice temperature and upper and lower ice surfaces are allowed to evolve. Ice temperature is then held constant during the calving simulations for...
reasons of computational efficiency. This is justified because significant changes in the temperature field are unlikely to occur over such short timescales. For the computation of the temperature field, ice temperature on the upper surface and inflow boundary are set using the MODIS IST product, averaged from 2000 to 2014. Geothermal heating is applied to the base at 75 mW m$^{-2}$ (Greve, 2005), and basal frictional heating and internal strain heating are also accounted for using Elmer/ice's temperature subroutines. Ice flow and temperature are linked by the temperature-dependent rate factor of Glen's flow law.

3 Results

3.1 Control simulation

The control simulation in this study represents present-day environmental forcing, as in Todd et al. (2018). In this present-day baseline scenario, Store’s terminus displays a seasonal range which varies from north to south (Fig. 3), with greater seasonal range in the south. Seasonal advance begins in February, and up to the end of May the terminus advances by 500 m on average, followed by a rapid retreat as soon as mélange is removed (Fig. 4). The terminus then maintains a fairly stable position through the rest of the year, varying stochastically by around 100 m on average. With the exception of the 200 m retreat at 1.6 years (Fig. 4), terminus position shows no sensitivity to increased melting in summer.

3.2 Response to intensification of distributed submarine melting

We find that a 50 % increase in distributed melting at the calving terminus (Run MD1) has only a small effect on the seasonal evolution of the modelled terminus geometry (Fig. 3a). The span of the maximum seasonal advance in late spring and retreat in summer is around 750 m, as opposed to 600 m for the control run (Fig. 4a), and the seasonality of advance and retreat remains periodic and similar to the control experiment throughout the simulation.

Doubling the distributed melt rate (Run MD2) has, however, a significant and destabilising effect on the terminus geometry (Fig. 3a). For the first model year of this simulation, the mean terminus position is very similar to that of Run MD1 (Fig. 4a). However, at the start of the summer melt season in model year 2, the terminus rapidly retreats by 900 m on average. This retreat is far greater than that in the control simulation and the perturbation triggers a transient increase in the terminus velocity from around 5200 to 5700 m a$^{-1}$, lasting 4 d (Fig. S3a in the Supplement). Just over a month later, the terminus calves back another 470 m on average. Figure 3a shows that the additional calving retreat occurs in the southern half of the terminus, where the glacier is afloat, and the terminus retreats by up to 3 km in just 40 d (Fig. 5b). The rapid retreat causes the simulation to break down irrecoverably (Sect. 2.2).

A calculation of the mean annual terminus mass budget components reveals that the calving rates in Runs MD1 and MD2 are less than those in the control simulation (Table S3 in the Supplement). In Run MD1, the 50 % increase in distributed melting decreases the average annual mass loss from calving from 7.2 to 6.7 Gt. Doubling the distributed melt rate (Run MD2) causes calving rate to increase slightly compared with MD1 to 7.07 Gt yr$^{-1}$, due to the collapse of the southern side of the terminus. Importantly, the reduction in calving mass loss is more than offset by the increase in loss through distributed melting.
3.3 Response to intensification of concentrated submarine melting

Increasing the melt rate from concentrated plumes by a factor of 1.5 (Run MC1) has no systematic effect on the shape of the terminus (Fig. 3b) nor its velocity (Fig. S3b) over the 5-year simulation. There are some minor differences in the minimum extent of the terminus, but the pattern varies between years. However, doubling the concentrated melt rate (Run MC2) has a significant effect on the retreat of the terminus in summer (Fig. 4b). In every year, the terminus retreats further than the control simulation; in year 1 the minimum mean terminus position is almost 600 m further upstream than the control. Figure 3b shows that, as with distributed melting, this extra retreat occurs exclusively in the floating region in the southern half of the terminus. In fact, the region of the terminus which retreats further than the control is constrained on either side by the two concentrated plumes. No significant changes in terminus velocity accompany the additional retreat.

3.4 Response to reduced ice mélange buttressing

While the seasonal formation and collapse of rigid proglacial ice mélange is the primary control on the seasonal advance and retreat of the terminus (Todd et al., 2018), we find that reducing the ice mélange thickness to half (Run MM1) has only a limited effect on seasonal position (Fig. 3c). In the winters of years 3–5 the terminus advanced slightly less than the control, and in the summer of year 1 the terminus retreated around 150 m further upstream (Fig. 4c). However, the broad pattern of both terminus range (Fig. 3c) and seasonal evolution (Fig. 4c) was much the same as the control. The deceleration of the terminus during the mélange season (300 m a\(^{-1}\)) was less than the control simulation (650 m a\(^{-1}\)), due to the reduced mélange thickness (Fig. S3c).

Removing the mélange entirely has a significant effect on the seasonal range in terminus position. The characteristic spring advance of the floating tongue is absent (Fig. 4c), and in year 4 the terminus retreats 350 m further than the control simulation, implying that the mélange has an important stabilising effect on timescales longer than a year. Again, this retreat occurs in the floating southern region of the terminus.

3.5 Response to combined intensified forcing

When all three forcings are applied together we find limited sensitivity in Run MA1 where both types of melting were increased by 50% and the mélange thickness decreased to half. The mean terminus position remains quite consistently around 150 m upstream of the control simulation (Fig. 4d). The advance due to ice mélange occurs more slowly, and increased melting keeps the terminus in a slightly retreated position compared to the control. As with previous magnitude perturbation experiments, the retreat is mostly confined to the southern side of the terminus (Fig. 3d).

In Run MA2, when submarine melting is doubled and mélange is entirely absent, the behaviour of the terminus is drastically different compared to run MA1 as well as the control. The terminus immediately begins a gradual retreat, which accelerates during the first summer melt season, retreating 450 m in total (Fig. 4d). There is a gradual readvance of 400 m in the following winter, but the glacier rapidly retreats by 800 m in the following summer. The terminus remains in this retreated position until the end of August, after which the simulation breaks down due to further calving, which causes problems for the model’s remeshing algorithm. Figure 3d shows that this retreat is confined to the southern, floating portion of the terminus, the same region as was observed to retreat in all the other magnitude forcing simulations. In this case, the entire southern side of the terminus has retreated more than 1 km beyond the minimum position...
observed in the control simulation. The velocity of the terminus in Run MA2 is fairly consistent with the control, with two exceptions. First, the lack of mélange means there is no terminus slowdown in spring. Second, for half a year following the start of the dramatic retreat, the terminus velocity was at least 300 m a$^{-1}$ faster than the control, after which the simulation breaks down.

As an alternative, we also tested model sensitivity to changes in the duration of the applied forcings. In these experiments, we simultaneously increased the melt season and reduced the mélange season by 1 month (Run D1) and 2 months (Run D2). We also performed the same experiments, but simultaneously increased and decreased the magnitude of melt and mélange forcings by 50 % (Run DM1) and 100 % (Run DM2) (Table S1). Overall, we found that changing the duration (i.e. season length) had a limited effect on calving and the stability of the glacier’s terminus position, highlighting the importance of forcing magnitude (i.e. melt rate and mélange strength) (see Sect. S1).

4 Discussion

Our results indicate that Store Glacier should remain relatively unchanged under intermediate perturbation scenarios (MD1, MC1, MM1, MA1), but that it may undergo retreat in response to more severe forcing (MD2, MC2, MM2, MA2). We base these assertions on novel model simulations in which a 50 % increase in the rates of submarine melting compared with observations (Chauché, 2016) had an overall limited effect on glacier dynamics, whereas a doubling led to retreat of more than a kilometre or more compared with the control, with (Figs. 3a, 4a) or without (Figs. 3d, 4d) mélange buttressing. Retreat in these simulations led to breakdown of the model due to rapid changes in the shape of the domain. While we can interpret the breakdown to be a loss of stability in our model, we are, at present, unable to speculate as to whether the retreat would continue or if the terminus would stabilise. Velocity at the terminus in Run MA2 shows a sustained acceleration relative to the control (Fig. S3d), which may indicate instability, but further model developments are required to simulate the longer-term evolution of the calving front. In addition to the effect of submarine melting, we found that the absence of winter mélange not only prevents the annual advance of the terminus, but also has a knock-on effect on the calving rates in the following summer.

We also found topographic setting is a critical control on calving and terminus stability. In previous work, the Ice Sheet System Model (ISSM) has been used with a vertically integrated shallow shelf approximation (SSA) solver and a calving rate parameterisation to investigate the effect of submarine melting on calving at Store Glacier (Morlighem et al., 2016). This analysis found no significant effect on terminus position from a doubling of submarine melting to 6 m d$^{-1}$, in contrast to our own results. This may be because vertically integrated models cannot directly simulate the stress effects of melt undercutting. Interestingly, in ISSM both the “control” and “double melt” simulations retreat to a steady state, which looks qualitatively similar to our MD2 minimum position (Fig. 3a) just before our simulation breaks down. This similarity in retreat pattern underscores the importance of basal topography in controlling calving; two very different ice flow models equipped with different calving laws show similar spatial patterns of retreat, though in response to different forcing.

The sensitivity analysis performed here emphasises the complex relationship between submarine melting and calving. The potential destabilising effect of submarine melting depends on the distribution of the melt forcing, and appears significantly greater in the southern side of the terminus than in the north, due to the effect of topography, which we discuss below. In the short term, Store Glacier appears to be able to withstand a 50 % increase in submarine melt rate compared to our control, which represents present-day conditions (Figs. 3, 4). Given that our simulations last 5 years, we cannot, however, rule out the possibility that a 50 % increase in submarine melt rates could lead to changes in terminus geometry over longer periods. For instance, in Run MD2, although we force the model with doubled melt rates in summer from the beginning, broad-scale terminus retreat does not begin until year 2, indicating the importance of the interannual mass budget. Sustained interannual mass loss near the terminus could lead to dynamic thinning; the simulations performed here are not long enough to capture this effect, but the positive feedback between retreat, acceleration and thinning could be a major destabilising influence.

The model seems relatively insensitive to an increase in the duration of submarine melting (Figs. S1a, S2a), even when the summer season is extended by 2 months, suggesting that longer summers would not necessarily destabilise Store. This relative insensitivity contrasts with previous studies which suggest that submarine melting has a significant effect on glacier calving rate and terminus stability (Rignot et al., 2010; Luckman et al., 2015). O’Leary and Christoffersen (2013) used a simple idealised 2-D model to demonstrate that undercutting by submarine melting might increase tensile stress at the ice surface, potentially opening crevasses farther from the front and thus promoting calving events. The reason that Store Glacier is relatively insensitive to intensification of submarine melting is twofold. One factor is the glaciers’ fast flow, which advects ice across the grounding line much faster than the rate of undercutting, and the other is the glacier’s topographic setting. Below, we discuss both aspects in more detail.

Insofar as stability is concerned, we find that a 100 % increase in distributed submarine melting is required to induce a purely undercut-driven retreat of Store Glacier (Fig. 5b). However, the modelled terminus also underwent significant seasonal retreat in response to increased *concentrated* submarine melting. Concentrated submarine melting cuts
notches into the terminus, isolating the surrounding ice from the sidewalls, reducing lateral drag and promoting calving. Plume modelling studies (Xu et al., 2013; Kimura et al., 2014; Slater et al., 2016) indicate that distributed plume systems melt ice more efficiently than localised concentrated plumes, but our simulations show that concentrated plumes have the potential to destabilise large portions of the calving terminus despite their small contribution to the total melt of the terminus.

Rates of submarine melting by forced convective plumes increase linearly with fjord water temperature and sublinearly with subglacial discharge (Xu et al., 2013), such that doubling the distributed submarine melt rate would require a doubling of thermal forcing (fjord water temperature), a quadrupling of subglacial discharge or some combination of the two. However, a reorganisation of the subglacial hydrology to a more channelled efficient system could promote more concentrated melting at the expense of distributed melting; this could enhance calving without necessarily requiring a large increase in total subglacial discharge or fjord water temperature. Surface velocity records from Store Glacier (Ahlstrøm et al., 2013) show a distinctive late-summer slowdown, similar to that which previous authors have attributed to a switch in the subglacial hydrological system from distributed to channelled subglacial drainage and back (Bartholomew et al., 2010; Sundal et al., 2011). Thus, if a warming climate were to exert an influence on the timing and characteristics of this switch, the resulting change in the subglacial hydrological system could enhance concentrated plume melting and, thus, calving. Additionally, any future changes to the stratification of the fjord water in front of Store Glacier could affect buoyant plume behaviour and melt rates.

Todd et al. (2018) found that ice mélangé was the main driver of seasonal terminus advance at Store under present-day climatic conditions, and our sensitivity analysis confirms this will continue as long as mélangé is present (Figs. 3c, 4c). Mélangé acts to stabilise the calving front by transferring buttressing force from fjord sidewalls through granular jamming (Peters et al., 2015; Robel, 2017). This buttressing force is applied to the terminus around the waterline, inhibiting surface crevasse formation and preventing bergs from overturning. We nonetheless found only a limited response in glacier behaviour when ice mélangé thickness was halved (Fig. 3c), suggesting that proglacial ice mélangé will continue to promote terminus advance by buttressing and calving suppression, even if thickness or strength is reduced. When mélangé was completely removed (Figs. 3c, 4c), the floating tongue failed to advance, corroborating earlier work (Todd and Christoffersen, 2014). However, the model also undergoes significantly greater retreat in summer compared to the control, with mean terminus position retreating 400 m further upstream than the control, despite no additional melt forcing being applied. This implies that mélangé buttressing is not simply an instantaneous stabilising force, but also promotes longer-term interannual stability. Observations from other glaciers in the Uummannaq region (Howat et al., 2010) support this hypothesis: in the spring of 2003, three glaciers failed to undergo their usual spring advance, and subsequently began concurrent multi-year retreat. We propose that terminus advance and reduced calving in winter, driven by mélangé buttressing, contributes to interannual stability through positive “dynamic” mass balance; as the terminus advances, increased basal and lateral drag modifies the force balance, leading to deceleration and dynamic thickening. This counteracts the dynamic thinning and mass loss which occurs in summer. Suppression of calving by mélangé occurs primarily during winter and spring, when iceberg dispersal is prevented by sea ice. The effectiveness of buttressing can be greatly reduced if rigid mélangé fails to form due to warmer air temperatures or surface water, as appears to have happened at Kangerdlugssuaq in 2017–2018 (Bevan et al., 2019). Loss of mélangé buttressing as implemented in Runs MM2 and MA2 is therefore possible in a warming world.

Our sensitivity analysis suggests that Store’s calving response to environmental forcing is both complex and heterogeneous. The results indicate that overall, Store is relatively insensitive to moderate changes in terminus forcing associated with climate warming. Under more severe perturbation, the model shows much greater environmental sensitivity in the southern side of the terminus than in the north. Modelled retreat was especially pronounced in the southern half of the terminus, where enhanced calving creates a new embayment, while the north half remains relatively unchanged (Fig. 5b). We argue that Store’s relative stability and the markedly different response of the two sides of the glacier are evidence of the strong control exerted by topography on the relationship between calving and climate forcing.

Calving glaciers tend to terminate in regions of topographic stability (Warren and Glasser, 1992; Benn et al., 2007a; Post et al., 2011; Catania et al., 2018) and this is particularly true for Store Glacier. Store’s terminus is located at a narrow point between two mountain ridges, beyond which the fjord widens significantly (Fig. 2b). Although bed elevations at the terminus are around 400 m below sea level, a subglacial trough deepens inland to depths of 1000 m below sea level. Thus, Store’s terminus is at a local maximum in terms of both basal and lateral resistive stress. Ice flowing towards the terminus from upstream will experience rapidly increasing resistive stress, which suppresses calving. As the ice passes the lateral and basal pinning points, this resistive stress is rapidly lost, promoting calving. Thus, Store Glacier is characterised by the rapid delivery (16–20 m d$^{-1}$) of ice to a terminus position where calving is inevitable; the system is akin to a conveyor belt dropping icebergs into Uummannaq Fjord. This setting contrasts strongly with several Svalbard glaciers where calving rates are observed to vary linearly with ocean temperature (Luckman et al., 2015). There is no information about the submarine melt rates of these
glaciers, but their velocities are an order of magnitude lower than Store’s, suggesting that changes in their terminus position may reflect the balance between delivery of ice to the terminus and the rate of undercutting by submarine melting. Indeed, in our melt perturbation experiments where Store did show a significant response (MD2, MC2, Figs. 3a, b, 4a, b), submarine melt rates were comparable to ice velocity: distributed melting in MD2 varies linearly from 0 m d\(^{-1}\) at the waterline to 12 m d\(^{-1}\) at the base, while concentrated plume melting in MC2 reaches a maximum of 24 m d\(^{-1}\).

The topographic setting of Store Glacier varies greatly from north to south (Fig. 1b), as does the response to environmental forcing (Fig. 3). In the north, the calving front coincides with a bedrock sill, which acts as a strong basal pinning point. However, in the south, there is a bedrock sill 2.5 km behind the terminus, and this leads to flotation downstream, as the ice is forced to accelerate over or divert around the sill. Thus, only the northern side of the terminus is well grounded, while the southern side is floating. As such, the topographic stability effect described above is weaker in the south, meaning submarine melting is most capable of influencing calving rates there, for the reasons outlined above. The stabilising effect of ice mélange is also greatest in the south, where it promotes a greater seasonal advance compared to the north. Mélange buttresses the glacier, reducing longitudinal tensile stress and inhibiting crevasse opening. In the southern floating section, this effect stabilises the terminus, promoting advance. In the north, however, the tensile stress associated with the sudden loss of basal traction at the basal pinning point is too great to be counteracted by mélange buttressing, which means the mélange is less able to suppress calving there.

In order to explore Store’s north–south divide in more detail, we plot near-terminus surface crevasse depth (Fig. 6a) and basal crevasse height (Fig. 6b) predicted by the model. To investigate the role that flotation plays in crevasse formation and calving, we also show the modelled “hydrostatic imbalance” (Fig. 6c), defined as

\[
1 + \frac{z_b \rho_{sw}}{H \rho_i},
\]

where \(\rho_i\) and \(\rho_{sw}\) are the density of ice and seawater, respectively, \(z_b\) is the elevation of the bed relative to sea level, and \(H\) is the thickness of the ice column. Equation (3) gives a measure of the buoyant forces acting on the ice: the value is positive where ice is resting above neutral buoyancy, zero where ice is neutrally buoyant and negative where ice is superbuoyant, meaning the ice is being held below the level of flotation. Multiplying the hydrostatic imbalance (Eq. 3) by \(H\) gives “height above buoyancy” (Van der Veen, 1996; Vieli et al., 2000), but we note that due to stress bridging effects, this does not give an accurate estimate of whether ice is floating or grounded over the short spatial scales considered here.

The most striking feature in the southern side of the modelled terminus is the superbuoyancy downstream of the grounding line (Fig. 6c) and the associated deep (450 m) basal crevasses that penetrate, in places, all the way through the glacier (Fig. 6b). This pattern arises as the ice in the south flows rapidly downhill over the southern bedrock sill (Fig. 2b). The bedrock geometry and velocity of the ice mean that it continues to flow downhill beyond the level of buoyant equilibrium to become superbuoyant. This superbuoyancy reaches a maximum halfway between the grounding line and the terminus, where surface elevation reaches a minimum of 32 m a.s.l., beyond which point the ice begins to bend upward, as evidenced by the rising surface elevation at the terminus in the south (reaching 55 m a.s.l.). Further evidence that this is an upward bending force comes from the complete closure of surface crevasses just beyond the grounding line (Fig. 6a); this indicates compressional forces at the surface. Figure S4 shows very similar patterns during the mélange season of the control simulation, indicating that these are persistent features relating to the broad-scale geometry of the glacier. Furthermore, we note that the observed and modelled surface geometries are in good agreement (Todd et al., 2018), giving us confidence in our analysis of the terminus geometry and stress.

The patterns of modelled crevasse depths and the influence of buoyancy (Fig. 6) help explain the contrasting environmental sensitivity of the northern and southern sides of Store’s terminus (Fig. 3). In the north, the terminus is firmly grounded on the stoss side of a basal pinning point (Fig. 1b), and there is a rapid transition from a compressive to an extensive stress regime as the ice crests this pinning point. This is further enhanced by the sudden loss of basal drag associated with ungrounding right at the front. This transition strongly promotes calving through enhanced crevasse propagation (Benn and Evans, 2014), resulting in a topographically controlled terminus position. This explains why this side of the terminus remains comparatively fixed in position and why it displays only a limited sensitivity to the perturbations we impose. In the south, however, the upward bending associated with superbuoyancy and flotation (Fig. 6c) causes deep basal crevassing up to 3 km upstream (Fig. 6b). The existence of deep basal crevasses upstream of the terminus means that small perturbations to the stress regime, for example those induced by undercutting from submarine melting, can more readily promote calving than in the north. Furthermore, there is no basally controlled terminus position in the south, as the ice has already lost contact with the bed. This more easily allows the mélange buttressing to stabilise the terminus, leading to advance in winter.

Our analysis demonstrates that basal topography and fjord geometry are critical for the stability of Greenland’s marine-terminating glaciers. It also indicates that the stress conditions associated with calving are considerably more complex than previously thought; without considering 3-D effects such as flotation and bending, it may not be possible to properly understand the calving process at Store Glacier and how it may respond to a warming climate. We therefore cau-
tion against over-reliance on calving models which neglect stress terms or dimensions, and emphasise the need for accurate input data for model geometry and boundary conditions. We note, for example, that the latest IPCC report’s estimates for Greenland’s sea level contribution at 2100 is based on a 1-D calving model, applied to only four outlet glaciers (Nick et al., 2013), and then upscaled on the assumption that environmental sensitivity of calving glaciers is regionally homogeneous (Goelzer et al., 2013). Recent model developments by Morlighem et al. (2016) implement calving in the plan-view ice sheet model ISSM. This is a significant advance, although the need for calibration of that calving model becomes problematic once the terminus migrates to a new position where topography is different. The results presented in this study required no calibration, which suggests that 3-D full-Stokes models, with realistic boundary conditions and forcings, have the potential to shed new light on the future behaviour of calving glaciers. In terms of long-term predictions of calving glaciers and ice sheets, the choice of model physics is likely to be dictated by available computing power. We hope, therefore, that the insights gained from 3-D full-Stokes modelling can be used to guide the development of new calving laws/parameterisations which can be applied in ice sheet models with lower-order physics.

5 Conclusions

We have investigated glacier calving in unprecedented detail, using a novel 3-D model of Store Glacier in Greenland to resolve individual calving events. This study builds on the modelling framework developed by Todd et al. (2018), who showed that undercutting by submarine melting and buttressing by rigid proglacial melange control the glacier’s seasonal calving dynamics. Here, we demonstrate that, in the short term, the glacier is fairly insensitive to moderate changes in these processes. This most likely explains why Store’s terminus has remained stable over the past 4 decades, including a recent period when many other glaciers in the Uummannaq region, and elsewhere in Greenland, underwent concurrent and sustained retreat (Howat et al., 2010; Seale et al., 2011). However, we found that more severe changes associated with a warming climate would probably undermine this stability. A complete loss of buttressing due to disappearance of the ice melange may prevent terminus advance in winter while exacerbating summer retreat. A doubling of submarine melt rates, as distributed or concentrated plumes or both, may lead to retreat beyond the current observed range. Behind the current terminus position, Store’s basal topography becomes much deeper (Fig. 2b); if the terminus were to retreat to this point, this might trigger sustained interannual retreat.

An important outcome of this study is that neither the calving style nor the environmental sensitivity of calving glaciers is spatially uniform. For Store Glacier, our model suggests that calving in the south side is driven by deep basal crevassing and is significantly modified by both melt undercutting and melange buttressing. In the north, calving is driven by surface crevassing and is comparatively insensitive to external forcing. While topography clearly exerts a strong influence on the glacier’s calving behaviour, only half of the terminus is topographically pinned, and this partial stability may render the glacier more prone to retreat and less stable compared to recent work (Catania et al., 2018). Remote-sensing studies (Carr et al., 2013; McFadden et al., 2011; Moon et al., 2015) suggest that topography may be an important control on calving at other West Greenland outlet glaciers. The importance of topographic control lends strong support to the use of fracture criteria for predicting calving. Our results suggest that, for glaciers with topographically well-defined terminus positions, calving occurs at specific places rather than at specific rates. The ongoing search for

Figure 6. (a) Surface crevasse penetration and (b) basal crevasse penetration from the beginning of the control simulation. (Note different colour scale.) (c) Hydrostatic imbalance (Eq. 1) at the terminus and 20 m surface elevation contours (black lines). White line indicates the grounding line. Figure S4 shows the equivalent panels for the mélange season, indicating that these patterns are permanent features of the glacier.
universal calving laws should incorporate improved prediction of fracture processes, rather than simply linking hypothetical calving rates to environmental or dynamic factors. Our results also strongly support the use of 3-D full-Stokes models in calving research. Flow line or vertically integrated models may fail to capture lateral variability and vertical stress gradients, respectively, both of which appear to be important at Store Glacier. Finally, our results indicate the importance of accurate input data, particularly basal topography. In this regard, the BedMachine product (Morlighem et al., 2017) has proved to be a vital step forward in Greenland calving research.

**Code availability.** The code constituting the 3-D calving model has been made freely available via integration with the Elmer/Ice source code, available at https://github.com/ElmerCSC/elmerfem/tree/elmerice, last access: 30 May 2019.

**Supplement.** The supplement related to this article is available online at: https://doi.org/10.5194/tc-13-1681-2019-supplement.

**Author contributions.** JT developed the calving model with substantial technical assistance from TZ and PR and scientific guidance from PC and DIB. JT and PC designed the sensitivity experiments and interpreted the results with assistance from DB and TZ. JT prepared the paper with contributions from all co-authors.

**Competing interests.** The authors declare that they have no conflict of interest.

**Acknowledgements.** We are grateful to Mathieu Morlighem and the anonymous reviewer for constructive feedback on how to improve the clarity and quality of this paper. This study was funded by the Natural Environment Research Council through a PhD studentship to Joe Todd (grant no. NE/K500884/1) and a research grant (NE/K005871/1) to Poul Christoffersen. Poul Christoffersen also acknowledges support from the European Research Council under the European Union’s Horizon 2020 Research and Innovation programme (grant agreement 683043). We acknowledge that the results of this research have been achieved using the PRACE-3IP project DynaMITE (FP7 RI-312763) awarded to Joe Todd and Poul Christoffersen with the resource Sisu based in Finland at CSC. We are grateful to Michiel van den Broeke for providing RACMO climate data, and to Olivier Gagliardini, Fabien Gillet-Chaulet and the wider Elmer/Ice developer community for their support. Landsat Surface Reflectance products courtesy of the U.S. Geological Survey.

**Financial support.** This research has been supported by the Natural Environment Research Council (grant nos. NE/K500884/1 and NE/K005871/1).

**Review statement.** This paper was edited by David M Holland and reviewed by Mathieu Morlighem and one anonymous referee.

**References**


Christoffersen, P., O’Leary, M., Van Angelen, J. H., and Van Den Broeke, M.: Partitioning effects from ocean and at-


J. Todd et al.: Sensitivity of a calving glacier to climate change 1693

J. Todd et al.: Sensitivity of a calving glacier to climate change 1693


