X-ray radiative transfer in protoplanetary disks

The role of dust and X-ray background fields

Ch. Rab\textsuperscript{1,3}, M. Güdel\textsuperscript{1}, P. Woitke\textsuperscript{2}, I. Kamp\textsuperscript{3}, W.-F. Thi\textsuperscript{4}, M. Min\textsuperscript{5,6}, G. Aresu\textsuperscript{7}, and R. Meijerink\textsuperscript{8}

\textsuperscript{1} University of Vienna, Dept. of Astrophysics, Türkenschanzstr. 17, 1180 Wien, Austria e-mail: christian.rab@univie.ac.at
\textsuperscript{2} SUPA, School of Physics & Astronomy, University of St. Andrews, North Haugh, St. Andrews KY16 9SS, UK
\textsuperscript{3} Kapteyn Astronomical Institute, University of Groningen, P.O. Box 800, 9700 AV Groningen, The Netherlands
\textsuperscript{4} Max-Planck-Institut für extraterrestrische Physik, Giessenbachstrasse 1, 85748 Garching, Germany
\textsuperscript{5} SRON Netherlands Institute for Space Research, Sorbonnelaan 2, 3584 CA Utrecht, The Netherlands
\textsuperscript{6} Astronomical institute Anton Pannekoek, University of Amsterdam, Science Park 904, 1098 XH, Amsterdam, The Netherlands
\textsuperscript{7} INAF, Osservatorio Astronomico di Cagliari, via della Scienza 5, 09047 Selargius, Italy
\textsuperscript{8} Leiden Observatory, Leiden University, PO Box 9513, 2300 RA Leiden, The Netherlands

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ABSTRACT

Context. The X-ray luminosities of T Tauri stars are about two to four orders of magnitude higher than the luminosity of the contemporary Sun. As these stars are born in clusters, their disks are not only irradiated by their parent star but also by an X-ray background field produced by the cluster members.

Aims. We aim to quantify the impact of X-ray background fields produced by young embedded clusters on the chemical structure of disks. Further we want to investigate the importance of the dust for X-ray radiative transfer in disks.

Methods. We present a new X-ray radiative transfer module for the radiation thermo-chemical disk code PRODImo (PROtoplanetary DIsk MOdel), which includes X-ray scattering and absorption by both the gas and dust component. The X-ray dust opacities can be calculated for various dust compositions and dust size distributions. For the X-ray radiative transfer we consider irradiation by the star and by X-ray background fields. To study the impact of X-rays on the chemical structure of disks we use the well established disk ionization tracers N\textsuperscript{2+}\textsubscript{H} and HCO\textsuperscript{+}.

Results. For evolved dust populations (e.g. grain growth), X-ray opacities are mostly dominated by the gas; only for photon energies $E \gtrsim 5 \to 10 \text{keV}$, dust opacities become relevant. Consequently the local disk X-ray radiation field is only affected in dense regions close to the disk midplane. X-ray background fields can dominate the local X-ray disk ionization rate for disk radii $r \gtrsim 20 \text{au}$. However, the N\textsuperscript{2+}\textsubscript{H} and HCO\textsuperscript{+} column densities are only significantly affected in case of low cosmic-ray ionization rates ($\lesssim 10^{-19} \text{ s}^{-1}$), or if the background flux is at least a factor of ten higher than the flux level of $\approx 10^{-5} \text{ erg cm}^{-2} \text{s}^{-1}$ expected for clusters typical for the solar vicinity.

Conclusions. Observable signatures of X-ray background fields in low-mass star-formation regions, like Taurus, are only expected for cluster members experiencing a strong X-ray background field (e.g. due to their location within the cluster). For the majority of the cluster members, the X-ray background field has only little impact on the disk chemical structure.

Key words. Stars: formation - Stars: circumstellar matter - Radiative transfer - Astrochemistry - Methods: numerical

1. Introduction

Strong X-ray emission is a common property of pre-main sequence stars. T Tauri stars, often considered as young solar analogs, show strong X-ray emission with luminosities in the range of approximately $10^{29} \to 10^{31} \text{ erg s}^{-1}$ (e.g. Preibisch et al. 2005; Güdel et al. 2007a), which is about $10^2 \to 10^4$ times higher than the X-ray luminosity of the contemporary Sun (Feigelson et al. 2002). The origin of such high X-ray luminosities is likely the enhanced stellar and magnetic activity of the young stars (e.g. Feigelson et al. 2002), but also jets close to the star and the protoplanetary disk (Güdel et al. 2007c) caused by interaction of the stellar and disk magnetic fields (e.g. X-wind Shu et al. 1997) might contribute. Accretion shocks probably do not contribute significantly to the X-ray emission of T Tauri stars (Güdel et al. 2007b), but accreting material absorbs soft X-rays and might cool the hot coronal gas (Güdel & Telleschi 2007).

X-ray irradiation plays an important role for the thermal and chemical structure of protoplanetary disks. Soft X-rays heat the upper disk layers to temperatures larger than 5000 K (Glassgold et al. 2004; Nomura et al. 2007; Aresu et al. 2011) and possibly drive, together with far and extreme ultraviolet radiation, disk photo-evaporation (e.g. Ercolano et al. 2008a; Gorti \& Hollenbach 2009). Diagnostics of the interaction of X-rays with the disk atmosphere are mainly atomic lines (e.g. Gorti \& Hollenbach 2004; Meijerink et al. 2008; Ercolano et al. 2008a; Ádámkovics et al. 2011; Aresu et al. 2012). These lines trace the hot upper layers (vertical column densities of $10^{19} \to 10^{20} \text{ cm}^{-2}$) in the inner $\approx 10 \to 50 \text{ au}$ of protoplanetary disks (Glassgold et al. 2007; Aresu et al. 2012). X-rays can influence atomic line emission via heating (e.g. [OI], Aresu et al. 2014) and/or direct ionization (e.g. the neon ion fine-structure lines Glassgold et al. 2007). Güdel et al. (2010) found a correlation between the [NeII] 12.81 \text{ } \mu \text{m} line, observed with the \textit{Spitzer} Space telescope, and stellar X-ray luminosity in a sample of 92 pre-main sequence stars. Such a correlation is consistent with predictions of sev-
eral thermo-chemical disk models (Meijerink et al. 2008; Gorti & Hollenbach 2008; Schisano et al. 2010; Aresu et al. 2012).

2. Methods

We use the radiation thermo-chemical disk code PtoDiMo (PROtoplanetary DIsk MOdel) to model the thermal and chemical structure of a passive disk irradiated by the stellar and interstellar radiation fields. PtoDiMo solves consistently for the dust temperature, gas temperature and chemical abundances in the disk (Woitke et al. 2009) and includes modules producing observables like spectral energy distributions (Thi et al. 2011) and line emission (Kamp et al. 2010; Woitke et al. 2011).

The disk model we use here is based on the so-called reference model developed for the DIANA\(^1\) (DiscAnalysis) project. This model is consistent with typical dust and gas observational properties of T Tauri disks, and is described in detail in Woitke et al. (2016) and Kamp et al. (2017). We therefore provide here only a brief overview of this reference model (Sect. 2.1). For this work we also use different dust size distributions to study the impact of dust on the X-ray RT; those models are described in Sect. 2.2. The new X-ray radiative transfer module of PtoDiMo is described in Sect. 2.3.

2.1. Reference model

In the following we describe the gas and dust disk structure of the reference model and the chemical network we used. In Table 1 we provide an overview of all model parameters including the properties of the central star. The stellar and interstellar X-ray properties are described in Sect. 2.3.

2.1.1. Gas disk structure

We use a fixed parameterized density structure for the disk. The axisymmetric flared 2D gas density structure as a function of the cylindrical coordinates \(r\) and \(z\) (height of the disk) is given by (e.g. Lynden-Bell & Pringle 1974; Andrews et al. 2009; Woitke et al. 2016)

\[
\rho(r,z) = \frac{\Sigma(r)}{\sqrt{2 \pi} \cdot h(r) \cdot \exp\left(-\frac{z^2}{2h(r)^2}\right)} \, [g \, cm^{-3}] ,
\]

(1)

For the vertical disk scale height \(h(r)\) we use a radial power-law

\[
h(r) = H(100 \, au) \left(\frac{r}{100 \, au}\right)^\beta
\]

(2)

where \(H(100 \, au)\) is the disk scale height at \(r = 100 \, au\) and \(\beta = 1.15\) is the flaring power index. For the radial surface density we use again a power-law with a tapered outer edge

\[
\Sigma(r) = \Sigma_0 \left(\frac{r}{R_{\text{out}}}ight)^{-\epsilon} \exp\left(-\frac{r}{R_{\text{tap}}}^{2-\epsilon}\right) \, [g \, cm^{-2}] .
\]

(3)

The inner disk radius is \(R_{\text{in}} = 0.07 \, au\) (the dust condensation radius), the characteristic radius is \(R_{\text{tap}} = 100 \, au\) and the outer radius is \(R_{\text{out}} = 620 \, au\) where the total vertical hydrogen column density is as low as \(N(H)_{\text{tot}} \approx 10^{20} \, cm^{-2}\). The constant \(\Sigma_0\) is given by the disk mass \(M_{\text{disk}} = 0.01 \, M_\odot\) and determined via the relation \(M_{\text{disk}} = 2\pi \int \Sigma(r) \, dr\) to be 1011 [g cm\(^{-2}\)]. The 2D gas density structure and the radial column density profile of the disk are shown in Fig. 1. The gas density structure is the same for all models presented in this paper.

\(^1\) DIANA website: http://diana-project.com/
We assume a dust to gas mass ratio of $\delta = 0.01$, which also determines the total dust mass. However, due to dust evolution processes like dust growth, dust settling and drift (see e.g. Birnstiel et al. 2012), the dust density structure in a protoplanetary disk does not necessarily follow the gas density structure.

We account for this by including a dust size distribution with a minimum dust grain size of $a_{\text{min}} = 0.05 \mu m$ and a maximum grain size of $a_{\text{max}} = 3000 \mu m$. The size distribution itself is given by a simple power-law $f(a) \propto a^{-3.5}$ (Mathis et al. 1977). Dust settling is incorporated by applying the method of Dubrulle et al. (1995), using a turbulent mixing parameter of $a_{\text{settle}} = 10^{-2}$. This results in a grain size and gas density dependent dust scale height and the dust to gas mass ratio varies within the disk. For example at $r = 100 \ au$ the local dust to gas mass ratio varies from $\delta_{\text{local}} \approx 0.1$ close to the midplane to values $\delta_{\text{local}} \leq 0.001$ in the upper layers of the disk. We note that the total dust to gas mass ratio $\delta$ stays the same (for more details see Woitke et al. 2016). We use porous grains composed of a mixture of amorphous carbon and silicate (see Table 1). The resulting dust grain density is $\rho_{\text{gr}} = 2.1 \ g \ cm^{-3}$. Our model does not account for possible radial drift of large dust particles (see Sect. 4.3 for a discussion).

In ProDiMo the same dust model is consistently used for the radiative transfer, including X-rays and the chemistry. For more details on the dust model and opacity calculations see Woitke et al. (2016); Min et al. (2016).

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**Table 1. Main parameters for the reference disk model.**

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>stellar mass</td>
<td>$M_*$</td>
<td>$0.7 \ M_\odot$</td>
</tr>
<tr>
<td>stellar effective temp.</td>
<td>$T_*$</td>
<td>4000 K</td>
</tr>
<tr>
<td>stellar luminosity</td>
<td>$L_*$</td>
<td>$1.0 \ L_\odot$</td>
</tr>
<tr>
<td>FUV excess</td>
<td>$L_{\text{FUV}}/L_*$</td>
<td>0.01</td>
</tr>
<tr>
<td>FUV power law index</td>
<td>$p_{\text{UV}}$</td>
<td>1.3</td>
</tr>
<tr>
<td>X-ray luminosity</td>
<td>$L_X$</td>
<td>$10^{30} \ erg \ s^{-1}$</td>
</tr>
<tr>
<td>X-ray emission temp.</td>
<td>$T_X$</td>
<td>$2 \times 10^7 \ K$</td>
</tr>
<tr>
<td>strength of interst. FUV</td>
<td>$\chi_{\text{ISM}}$</td>
<td>$1^{\alpha}$</td>
</tr>
<tr>
<td>disk gas mass</td>
<td>$M_{\text{disk}}$</td>
<td>$0.01 \ M_\odot$</td>
</tr>
<tr>
<td>dust/gas mass ratio</td>
<td>$d/g$</td>
<td>0.01</td>
</tr>
<tr>
<td>inner disk radius</td>
<td>$R_{\text{in}}$</td>
<td>0.07 au</td>
</tr>
<tr>
<td>tapering-off radius</td>
<td>$R_{\text{ap}}$</td>
<td>100 au</td>
</tr>
<tr>
<td>column density power ind.</td>
<td>$\epsilon$</td>
<td>1.0</td>
</tr>
<tr>
<td>reference scale height</td>
<td>$H(100 \ au)$</td>
<td>10 au</td>
</tr>
<tr>
<td>flaring power index</td>
<td>$\beta$</td>
<td>1.15</td>
</tr>
<tr>
<td>min. dust particle radius</td>
<td>$a_{\text{min}}$</td>
<td>0.05 $\mu m$</td>
</tr>
<tr>
<td>max. dust particle radius</td>
<td>$a_{\text{max}}$</td>
<td>3 mm</td>
</tr>
<tr>
<td>dust size dist. power index</td>
<td>$a_{\text{pow}}$</td>
<td>3.5</td>
</tr>
<tr>
<td>turbulent mixing param.</td>
<td>$a_{\text{settle}}$</td>
<td>$10^{-2}$</td>
</tr>
<tr>
<td>max. hollow volume ratiob</td>
<td>$V_{\text{hollow,max}}$</td>
<td>0.8</td>
</tr>
<tr>
<td>dust composition (volume fractions)</td>
<td>$M_{\text{g}, \text{Fe}, \text{Si,Ot}}$</td>
<td>60%</td>
</tr>
<tr>
<td></td>
<td>amorph. carbon</td>
<td>15%</td>
</tr>
<tr>
<td></td>
<td>porosity</td>
<td>25%</td>
</tr>
<tr>
<td>PAH aban. rel. to ISM</td>
<td>$f_{\text{PAH}}$</td>
<td>0.01</td>
</tr>
<tr>
<td>chem. heating efficiency</td>
<td>$\chi_{\text{chem}}$</td>
<td>0.2</td>
</tr>
</tbody>
</table>

Notes. If not noted otherwise, these parameters are kept fixed for all our models presented in this work. For more details on the parameter definitions see Woitke et al. (2009, 2011, 2016). $^a$ $\chi_{\text{ISM}}$ is given in units of the Draine field (Draine & Bertoldi 1996; Woitke et al. 2009). $^b$ We use distributed hollow spheres for the dust opacity calculations (Min et al. 2005, 2016).

2.1.2. Dust structure

Our chemical network is based on the gas-phase chemical database UMIST 2012 (McElroy et al. 2013) where we only use a subset of reactions according to our selection of species. Additionally to the gas phase reactions from the UMIST database we include detailed X-ray chemistry (Meijerink et al. 2012), charge exchange chemistry of PAHs (Polycyclic aromatic hydrocarbons, Thi et al. 2014, Thi et al. 2017), excited H$_2$ chemistry, H$_2$ formation using the analytical function of Cazaux & Tielens (2002, 2004) and adsorption and thermal, photo and cosmic-ray desorption of ices (including PAHs). Dust surface chemistry is not included in our model.

The chemical network used here is described in detail in Kamp et al. (2017). We used their so called large chemical network which consists of 235 chemical species (64 of them are ices) and 3143 chemical reactions. The element abundances are listed in Kamp et al. (2017). The element abundances correspond to the group of low metal abundances (e.g Graedel et al. 1982; Lee et al. 1998). Further details concerning the chemistry of HCO$^+$ and N$_3$H$^+$ and the used binding energies are given in Rab et al. (2017b).

To solve for the chemical abundances we used the steady-state approach. In Woitke et al. (2016) and Rab et al. (2017b) comparisons of time-dependent and steady-state chemistry models are presented, which show that in our models steady-state is reached within typical lifetimes of disks in most regions of the disk. In Rab et al. (2017b) it is shown that the assumption of steady-state is well justified for HCO$^+$ and N$_3$H$^+$ (see also Aikawa et al. 2015). The resulting differences between the steady-state and time-dependent models in the radial column
density profiles of the molecular ions are not significant for our study.

2.2. Model groups

2.2.1. Dust models

For our investigations of the impact of the dust on the X-ray radiative transfer and on the molecular column densities we use three different dust size distributions. All three distributions have the same dust composition as listed in Table 1. The parameters varied are $a_{\text{min}}$, $a_{\text{max}}$ and $a_{\text{pow}}$. In all three dust models the gas density structure is the same as described in Sect. 2.1.1 and the dust to gas mass ratio is $d = 0.01$. The details of the dust models are provided in Table 2.

The small grains model (SG) includes only a single dust size with $a = 0.1 \mu m$ and no dust settling. Although such a dust model is likely not a good representation for the conditions in protoplanetary disks, it is useful as a reference and to show the impact of the dust on the X-ray radiative transfer and chemical disk structure.

The medium grain and large grain models are more appropriate in the context of grain growth and dust settling. (see Sect. 2.1.2). Although, such dust models are a simplified representation of dust evolution in disks (Birnstiel et al. 2012; Vasyunin et al. 2011; Akimkin et al. 2013; Facchini et al. 2017), they still provide insight on the role of dust for the chemistry and X-ray radiative transfer. The main difference of the medium and large grain model is the amount of small particles. In the medium grain model about 10% of the total dust mass is in grains with $a \leq 1 \mu m$ whereas in the large grain models it is only about 1.5%. Both models include dust settling as described in Sect. 2.1.2.

Most relevant for the chemistry is the total dust surface area per hydrogen nucleus (i.e. for the freeze-out of molecules). The dust surface area varies by about two orders of magnitude in our models (Table 2, see also Woitke et al. 2016; Rab et al. 2017a for details).

In Fig. 2 we show the dust density structure, the dust and gas temperature and the local UV radiation field in the disk, for the small grains and large grains model. The main difference in the dust models is the visual extinction $A_V$, which significantly affects the dust temperature structure and the local disk radiation field.

Table 2. Dust models.

<table>
<thead>
<tr>
<th>Name</th>
<th>Parameters</th>
<th>$A_V = 1^{(a)}$</th>
<th>Surface$^{(b)}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>small grains</td>
<td>single size</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SG</td>
<td>$a = 0.1 \mu m$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>no settling</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. $^{(a)}$ hydrogen column density $N_{H_2}$, where the visual extinction $A_V$ is unity. $^{(b)}$ total dust surface per hydrogen nucleus (unsettled value). $^{(c)}$ $a(b)$ means $a \times 10^b$.

Fig. 2. Large grains (left column) and small grains (right column) disk model. From top to bottom the dust density, dust temperature, gas temperature and the disk UV radiation field $\chi$ in units of the Draine field is shown. The dashed contours in each plot correspond to the levels shown in the respective colourbar. The additional contours in the UV plots (bottom row) indicate where the radial (red solid line) and vertical (black solid line) visual extinction are equal to unity. For both models the same gas density structure as shown in Fig. 1 is used.

2.2.2. Cosmic rays

There is some uncertainty about how many of the cosmic rays actually reach the disk of T Tauri stars. Similar to the Sun, the stellar wind of young stars, which might be significantly stronger compared to the Sun, can power a heliosphere-like analog which is called a “T Taurisphere”. The existence of such a T Taurisphere might reduce the cosmic-ray ionization rate in the disk by several orders of magnitude (Cleeves et al. 2013a).

To account for this, we use two different cosmic-ray input spectra, one is the canonical local ISM cosmic-ray spectrum (Webber 1998) and the second is a modulated spectrum which accounts for the suppression of cosmic-rays by a heliosphere. For the latter we use the “Solar Max” spectrum of Cleeves et al. 2013a. To calculate the cosmic-ray ionization rate we use the fitting formula of Padovani et al. (2013) and Cleeves et al. (2013a). The ISM cosmic-ray spectrum gives a cosmic-ray ionization rate per hydrogen nucleus of $\zeta_{CR} \approx 10^{-17}$ and the Solar Max spectrum gives $\zeta_{CR} \approx 10^{-19}$, which is consistent with the upper limit of the total H$_2$ ionization rate in TW Hya derived by Cleeves et al. (2015). We call these two model groups “ISM cosmic rays” and “low cosmic rays”, respectively.
2.3. X-ray radiative transfer

For the X-ray radiative transfer (RT) we extended the already available radiative transfer module of ProDiMo to the X-ray wavelength regime. The 2D radiative transfer problem including scattering is solved with a ray-based method and a simple iterative scheme (X-iteration). The radiative transfer equation is solved for a coarse grid of wavelengths bands. For each band the relevant quantities (e.g. incident intensities, opacities) are averaged over the wavelength range covered by each band. The details of this method are described in Woitke et al. (2009). For the X-ray regime we find that about 20 wavelength bands are sufficient to represent the energy range of 0.1 – 20 keV used in our models. Besides the stellar radiation also interstellar radiation fields (UV and X-rays) are considered. For the interstellar radiation fields we assume that the disk is irradiated isotropically.

The X-ray RT module provides the X-ray radiation field for each point in the disk as a function of wavelength. Those values are used in the already available X-ray chemistry module of ProDiMo to calculate the X-ray ionization rate for the various chemical species. The X-ray chemistry used in this paper is the same as presented in Aresu et al. (2011) and Meijerink et al. (2012). As the chemistry influences the gas composition which in turn determines the gas opacities, we iterate between the X-ray RT and the chemistry. For each X-ray radiative transfer step the chemical abundances are kept fixed where for each chemistry step the X-ray ionization rates are fixed. We find that typically three to five iterations are required until convergence is reached.

2.3.1. X-ray scattering

Compton scattering, which reduces to Thomson scattering at low energies, is the dominant scattering process in the X-ray regime. The anisotropic behaviour of Compton scattering is treated via an approximation by reducing the isotropic scattering cross-section by a factor \((1 - g)\), where \(g = \langle \cos \theta \rangle\) is the asymmetry parameter and \(\theta\) is the scattering angle (see also Laor & Draine 1993). We use this approach for both the gas and the dust scattering cross-sections. We call this reduced cross-section the pseudo anisotropic (pa) scattering cross-section. \(g\) is zero for isotropic scattering and approaches unity in case of strong forward scattering. We apply this approach because the treatment of anisotropic scattering in a ray-based radiative transfer code is expensive, in contrast to Monte Carlo radiative transfer codes. Although this method is a simple approximation it is very efficient and we find that our results concerning X-ray gas radiative transfer and the X-ray ionization rate are in reasonably good agreement with the Monte Carlo X-ray radiative transfer code MOCASSIN (see Appendix. B).

2.3.2. X-ray gas opacities

For the X-ray gas opacities we used the open source library xraylib\(^2\) (Brunetti et al. 2004; Schoonjans et al. 2011). This library provides the X-ray absorption and scattering cross-sections (Rayleigh and Compton scattering) for atomic and molecular species. Concerning the X-ray gas absorption cross-section we find that the cross-section provided by xraylib are similar to the commonly used X-ray absorption cross-section of Verner & Yakovlev (1995); Verner et al. (1996).

For the calculation of the X-ray gas opacities we used the same low-metal element abundances as are used for the chemistry (see Sect. 2.1.3). As a consequence of the strong depletion of heavy metals (Na, Mg, Si, S, Fe) by factors of 100 to 1000 compared to solar abundances, most of the absorption edges at higher energies \((E_X > 1 \text{ keV})\) disappear and the gas phase opacities in this regime are mostly dominated by hydrogen and helium (see also Bethell & Bergin 2011).

We note that we do not treat the depletion of gas-phase element abundances and the dust composition, which determines the element abundances in solids, consistently. Our approach here is to use the same dust properties (i.e. grain sizes, opacities) for the whole wavelength regime (X-ray to mm) considered in the radiative transfer modelling (see also Sect. 2.3.3 and Appendix A). The chosen dust opacities are well suited for modelling of protoplanetary disks as discussed in Woitke et al. (2016). However, for the dust compositions and the dust to gas mass ratio used in this work the sum of the gas and dust X-ray opacities are consistent within a factor of two with pure gas-phase X-ray opacities using the solar element abundances of Lodders (2003).

2.3.3. X-ray dust opacities

In the literature, only X-ray optical constants for Astronomical Silicates and carbon are available (Draine 2003). However, for protoplanetary disks often a mixture of different dust species is used.

We implemented the method of Draine (2003) to calculate X-ray optical constants for various dust compositions. This method uses the available optical constants, or more precisely the dielectric function, for the ultraviolet to the millimetre wave-
length range and additionally the atomic gas phase photo-electric cross-sections for the X-ray regime. With this, the imaginary part of the complex dielectric function can be constructed from the X-ray to the millimetre regime. Via the Kramers-Kronig relation the real part of the dielectric function can be calculated knowing the imaginary part.

To be consistent with Draine (2003) we use the photo-electric cross-sections from Verner et al. (1996) to construct the imaginary part of the dielectric function. However, in contrast to Draine (2003) we do not include any additional measured data for the K edge absorption profiles (e.g. for graphite). The details of the absorption edges are less important here, as we are mainly interested in the resulting X-ray ionization rate which is an energy-integrated quantity.

In Fig. 3 we compare the optical constants for Astronomical Silicates (MgFeSiO$_4$ composition) calculated via the above described method to the original optical constants provided by Draine (2003). The deviations of our results from the Draine (2003) data are likely a consequence of our simplified treatment of absorption edges. However, our approach is sufficient for deriving X-ray ionization rates.

By using these newly available optical constants we calculated the X-ray dust opacities with a combination of the Mie-theory, the Rayleigh-Gans approximation (Krügel 2002) and geometrical optics (Zhou et al. 2003) similar to Draine (2003) and Ercolano et al. (2008a). Also here we use the pseudo anisotropic scattering cross-sections in our calculations (see Sect. 2.3.1).

In Fig. 4 we show the dust extinction (sum of absorption and scattering cross-sections) and the scattering cross-sections per hydrogen nucleus for three examples of dust size distributions and compositions, in a similar way as presented in Draine (2003). For comparison we also show the gas cross-section for the initial elemental abundances used in our models (low metal abundances, see Kamp et al., 2017), assuming that all hydrogen is molecular and all other elements are present as neutral atoms. For all cases shown in Fig. 4 we assumed a gas to dust mass ratio of 0.01.

The first panel in Fig. 4 shows the results for an MRN (Mathis, Rumpl, Nordsieck; Mathis et al. 1977) size distribution ($a_{\text{min}} = 0.005 \mu m, a_{\text{max}} = 0.25 \mu m and a_{\text{pow}} = 3.5$) for pure Astronomical Silicates (Draine 2003). Although we do not use such a dust size distribution in our disk model the results are shown for reference. A comparison with Fig. 6 of Draine (2003) shows that our results are in good qualitative agreement with their results. However, Draine (2003) considered two individual dust populations with different dust compositions and size distributions: Astronomical Silicates and very small carbonaceous grains, the latter are not considered here. As a consequence the carbon absorption edge at around 0.3 eV is missing in our MRN dust model.

Fig. 4 clearly shows that for energies below 1 keV the gas is the main opacity source even for the case of small grains. For higher energies dust becomes the dominant opacity source in the X-ray regime. However, considering a dust size distribution more typical for protoplanetary disks ($a_{\text{min}} = 0.05 \mu m, a_{\text{max}} = 3000 \mu m and a_{\text{pow}} = 3.5$), the dust extinction becomes only important for energies $\gtrsim 4$keV. However, Fig. 4 also shows that the dust scattering cross-section is significantly reduced if the g factor approximation is applied. The scattering phase function for dust is strongly forward peaked resulting in a g factor very close to unity (i.e. small scattering angle Draine 2003). The main consequence is that dust scattering is insignificant for disks as it does not produce a diffuse radiation field as most photons are simply forward scattered (Bethell & Bergin 2011).

The gas scattering cross-section is nearly independent of energy and becomes the dominant opacity source for energies $E_X \gtrsim 5$keV. The scattering phase function of the gas is not strongly forward peaked as X-ray photons are mainly scattered by the electrons bound to hydrogen or helium. However, there is a slight decrease in the scattering cross-section with energy as Compton scattering becomes more anisotropic for higher energies, and in our simplified model this results in a reduced scattering cross-section.

We note that in our model the dust is simply an additional opacity source and we neglect actually any real interaction of X-rays with the dust, such as ionization or heating. The interaction of X-rays with solids is a very complex process (see e.g. Dwek & Smith 1996). Besides heating (e.g. Laor & Draine 1993) and ionization (Weingartner & Draine 2001), recent experiments indicate also possible dust amorphization by soft and hard X-rays (Ciavarella et al. 2016; Gavilan et al. 2016). However, we focus here on the X-ray ionization of the gas component and a detailed investigation of the impact of X-rays on the dust component is out of the scope of this paper.

Our chemical model also includes PAHs (see Sect. 2.1.3). In Appendix C we show that the expected X-ray absorption cross-
sections for PAHs are too low to play a significant role in the attenuation of X-ray radiation. As our focus here is on the X-ray ionization rates a detailed modelling of the interaction of X-rays with PAHs is not considered.

### 2.3.4. Stellar X-rays

To model the X-ray emission of T Tauri stars we assume that the origin of the emission is close to the stellar surface (see e.g. Ercolano et al. 2009) and place the source of the emission on the star. The spectral shape of the emission is modeled with an isothermal bremsstrahlung spectrum (Glassgold et al. 2009; Aresu et al. 2011) of the form

\[
I(E) \propto \frac{1}{E} \exp\left(-\frac{E}{kT_X}\right).
\]  

(4)

Where \(E\) is the energy in keV, \(I\) is the intensity, \(k\) is the Boltzman constant and \(T_X = 2 \times 10^7\) K is the plasma temperature. We considered a X-ray energy range of 0.1 – 20 keV for the stellar spectrum. The spectrum is normalized to a given total X-ray luminosity \(L_X\) in the range of 0.3 – 10 keV as such an energy range is typical for reported observed X-ray luminosities (e.g. Güdel et al. 2009).

We note that it is also possible to use a more realistic thermal line plus continuum X-ray spectrum as input in ProDiMo (see Woitke et al. 2016). However, as we do not model here a particular source we use Eq. 4, which is a reasonable approximation for the general shape of observed X-ray spectra (Glassgold et al. 2009; Woitke et al. 2016).

### 2.3.5. X-ray background field

A star embedded in a young cluster likely receives X-ray radiation from the other cluster members. In Adams et al. (2012) typical flux values for such a cluster X-ray background field (XBGF) are derived, where the values depend on the cluster properties (e.g. number of cluster members) and the position of the considered target within the cluster. Such a cluster background field is probably one to two orders of magnitude stronger than the diffuse extragalactic background field (Adams et al. 2012).

In Adams et al. (2012) only the total flux or energy averaged values of the XBGF are considered and now detailed X-ray radiative transfer method is applied. Here we included the XBGF in the energy dependent X-ray radiative transfer module. To do this we modelled the spectrum of the background field in the same way as the stellar X-ray spectrum. We used an isothermal bremsstrahlung spectrum (Eq. (4)) with \(T_X = 2 \times 10^7\) K (\(kT_X \approx 1.7\) keV) and normalized the spectrum to the given total flux in the energy range of 0.1 – 20 keV. We assumed that the disk is irradiated isotropically by the XBGF.

Adams et al. (2012) estimated a characteristic flux level for a cluster X-ray background field (XBGF) of \(F_{XBGF} = 1 - 6 \times 10^{-5}\) erg cm\(^{-2}\) s\(^{-1}\). As discussed by Adams et al. (2012) variations from cluster to cluster and also between single cluster members (i.e. location within the cluster) can be significant. Therefore we consider here flux levels for the XBGF in the range of \(F_X = 2 \times 10^{-6} - 2 \times 10^{-4}\) erg cm\(^{-2}\) s\(^{-1}\), including the benchmark value of \(2 \times 10^{-5}\) from Adams et al. (2012). These values roughly cover the width of the X-ray background flux distributions derived by Adams et al. (2012). We note that we considered here a slightly wider X-ray energy range as Adams et al. (2012), who used 0.2 – 15 keV. Therefore the given total flux levels differ slightly, for example \(F_X(0.1 - 20\) keV) = \(2 \times 10^{-5}\) erg cm\(^{-2}\) s\(^{-1}\) corresponds to \(F_X(0.2 - 15\) keV) = \(1.4 \times 10^{-5}\) erg cm\(^{-2}\) s\(^{-1}\).

Adams et al. (2012) assumes that there is no absorption of X-rays within the cluster. However, absorption of soft X-rays (\(E \leq 1\) keV) is possible, either by material between the star and the disk (see Ercolano et al. 2009) or the interstellar medium itself. To account for such a scenario in a simple way we also used input spectra with low-energy cut-offs of 0.3 and 1 keV, respectively (see Sect. 3.2.2).

In Fig. 5 we show our XBGF spectra and additionally the spectrum measured for the diffuse extragalactic X-ray background field (Fabian & Barcons 1992) and a “hot gas” spectrum (e.g. produced by supernova remnants see Tielens 2005 chap. 1, Slavin & Frisch 2008). This figure shows that typically the cluster XBGF will dominate the X-ray background flux impinging on the disk.

### 3. Results

Our results are presented in the following way. In Sect. 3.1 we show the impact of scattering, dust opacities and X-ray background fields on the X-ray disk ionization rate \(\zeta_X\). In Sect. 3.2 we present the molecular column densities of HCO\(^+\) and N\(_2\)H\(^+\) for our three different dust models and for models with and without X-ray background fields.

#### 3.1. X-ray disk ionization rates

In ProDiMo the X-ray ionization rate is calculated individually for the single atoms and molecules (see Meijerink et al. 2012 for details). \(\zeta_X\) used in the following is simply the sum of the ionization rates of atomic and molecular hydrogen (we use a similar definition as Adámkovics et al. 2011). We note that we define \(\zeta_X\) per hydrogen nucleus, which is a factor of two lower compared to the ionization rate per molecular hydrogen. For all models discussed in this section \(L_X = 10^{30}\) erg s\(^{-1}\), if not noted otherwise.
source is located $12 R_\odot$ above and below the star. Compared to our model where the X-ray source is the star itself, the scattering surface moves to deeper layers in the disk as the radial column density seen by stellar X-rays is reduced (see also Appendix B). This can cause differences in $\xi_X$ by about an order of magnitude in vertical layers close to the scattering surface (Igea & Glassgold 1999). In terms of vertical column density the scattering surface is located at $N(b,\text{ver}) \approx 2 \times 10^{22} \text{ cm}^{-2}$ for $r \lesssim 50$ au, but drops rapidly to lower vertical column densities due to the disk structure (see Fig. 6).

An X-ray background field irradiates the disk isotropically. In Fig. 6 we also mark $N(b,\text{ver}) \approx 2 \times 10^{22} \text{ cm}^{-2}$ which roughly corresponds to the scattering surface for X-ray radiation entering the disk vertically (perpendicular to the midplane). This indicates that scattering is of less importance for X-ray background fields, as only in the region with $N(b,\text{ver}) \gtrsim 2 \times 10^{24} \text{ cm}^{-2}$ (i.e. $r \lesssim 10$ au) scattering can become significant. However, in that region stellar X-rays will dominate the disk radiation field anyway (see Sect. 3.1.3). Test models with and without X-ray scattering indeed showed that scattering is negligible for the case of an isotropic X-ray background radiation source.

In Fig. 7, $\xi_X$ is also shown for models with and without scattering. This figure shows that at high column densities, $\xi_X$ is dominated by X-ray scattering, whereas at low column densities, $\xi_X$ is not significantly affected by scattering and is dominated by direct stellar X-rays. The reason is that the scattering cross-section becomes only comparable to the absorption cross-section for X-ray energies $E \gtrsim 5$ keV (see Fig. 4). This means that mainly the energetic X-ray photons are scattered towards the midplane of the disk, where above the scattering surface $\xi_X$ is dominated by the softer X-rays which are not efficiently scattered. This is consistent with other X-ray radiative transfer models (e.g. Igea & Glassgold 1999; Ercolano & Glassgold 2013; Cleeves et al. 2013b).

### 3.1.1. Impact of X-ray scattering

X-ray scattering is already a quite common ingredient in protoplanetary disk modelling codes (e.g. Igea & Glassgold 1999; Nomura et al. 2007; Ercolano et al. 2008a; Ercolano & Glassgold 2013; Cleeves et al. 2013a). In this section we want to compare our results concerning scattering to some of those models. We also briefly discuss the importance of X-ray scattering for the location of the scattering surface.

In Fig. 6 we show $\xi_X$ for the whole 2D disk structure for a model with X-ray gas absorption only and a model including scattering. In these models dust is not considered as an X-ray opacity source. The same models are also included in Fig. 7 where $\xi_X$ is plotted as a function of vertical hydrogen column density $N(b,\text{ver})$ at radii of 1 and 100 au distance from the central star.

As discussed already in Igea & Glassgold (1999) and Ercolano & Glassgold (2013) it is possible to define a single scattering surface in the disk, because the scattering cross-section of the gas component is nearly constant over the whole X-ray energy range (see Fig. 4). A scattering optical depth of unity is reached at a hydrogen column density of $N(b) \approx 2 \times 10^{24} \text{ cm}^{-2}$ (see Fig. 4 and Igea & Glassgold 1999). For stellar X-rays the radial column density defines the location of the scattering surface in the disk (see Fig. 6). Below the scattering surface the X-ray ionization rate is dominated by scattered X-rays. We want to note that the location of the scattering surface depends on the location of the X-ray source. For example in the models of Igea & Glassgold (1999) and Ercolano & Glassgold (2013) the central X-ray scattering surface is located 12 $R_\odot$ above and below the star. Compared to our model where the X-ray source is the star itself, the scattering surface moves to deeper layers in the disk as the radial column density seen by stellar X-rays is reduced (see also Appendix B). This can cause differences in $\xi_X$ by about an order of magnitude in vertical layers close to the scattering surface (Igea & Glassgold 1999). In terms of vertical column density the scattering surface is located at $N(b,\text{ver}) \approx 2 \times 10^{22} \text{ cm}^{-2}$ for $r \lesssim 50$ au, but drops rapidly to lower vertical column densities due to the disk structure (see Fig. 6).

In Fig. 6 we show $\xi_X$ for the whole 2D disk structure for a model with X-ray gas absorption only and a model including scattering. In these models dust is not considered as an X-ray opacity source. The white and red dashed lines show $N(b,\text{ver}) = 2 \times 10^{22} \text{ cm}^{-2}$ and $N(b,\text{ver}) = 2 \times 10^{24} \text{ cm}^{-2}$, respectively.

**Fig. 6.** X-ray ionization rate $\xi_X$ for the 2D disk structure. The top panel shows a model with only gas absorption the bottom panel a model with gas absorption and scattering. The white solid contour line shows $N(b) = 2 \times 10^{24} \text{ cm}^{-2}$, which corresponds roughly to the X-ray scattering surface. Below this surface $\xi_X$ starts to be dominated by scattered X-ray photons. The white and red dashed lines show $N(b,\text{ver}) = 2 \times 10^{22} \text{ cm}^{-2}$ and $N(b,\text{ver}) = 2 \times 10^{24} \text{ cm}^{-2}$, respectively.

### 3.1.2. Impact of dust opacities

In Fig. 8 we show the X-ray ionization rate for models with three different dust size distributions: small grains, medium grains and large grains (see Sect. 2.2.1). In these models both the gas and X-ray absorption are the same in all three dust models. To compare $\xi_X$ to models without X-ray dust opacity they are also included in Fig. 7.

As already mentioned, scattering of X-rays by dust can be neglected due to the strongly forward peaked scattering phase function (see Sect. 2.3.3). As the dust acts only as an additional absorption agent, $\xi_X$ is reduced wherever the dust opacity becomes similar or larger than the gas opacity. This is in particular the case for high X-ray energies (see Fig. 4) but depends on the chosen dust properties. In the case of the small grains, dust absorption dominates the X-ray opacity for X-ray energies $E_X \gtrsim 1$ keV. As a consequence $\xi_X$ drops by about an order of magnitude and more, compared to the model with gas opacities only (see Fig. 7). For the medium and large grain models the impact of dust is much less severe. For the medium grains dust extinction becomes relevant for $E_X \gtrsim 3$ keV and for the large grains only for $E_X \gtrsim 10$ keV, but in the large grains model, gas extinction remains always higher than dust absorption (see Fig. 4).

Our results imply that dust extinction plays an important role for young disks, whereas for evolved disks with large grains, X-rays can penetrate deeper. In evolved disks only the most energetic X-rays are affected as the gas opacity drops rapidly with
energy. Therefore the impact on $\zeta_X$ is the largest in the deep, high density, layers of the disk where $\zeta_X$ is dominated by high energy X-rays. In young objects, where the disk is still embedded in an envelope, small grains can be important and should be included in X-ray radiative transfer models. We will investigate such a scenario based on the Class I PdDiMO model presented in Rab et al. (2017a) in a future study.

3.1.3. Impact of X-ray background fields

The importance of X-ray background fields for disks was estimated analytically by Adams et al. (2012). They find that the X-ray background flux can be larger than the stellar X-ray flux for disk radii $r \gtrsim 14$ au, assuming a geometrically flat disk and a typical disk impact angle for the stellar radiation. Their estimated radius corresponds to the radius where the stellar and interstellar X-ray flux becomes equal. However, attenuation by the disk itself was not taken into account (i.e. they compared the stellar and background X-ray fluxes at the disk surface).

In Fig. 9 we show $\zeta_X$ for our full 2D disk model using $L_X = 10^{29}$ erg s$^{-1}$ and an X-ray background flux of $F_{XBGF} = 2 \times 10^{-5}$ erg cm$^{-2}$ s$^{-1}$ (these are the values used by Adams et al. 2012 for their benchmark case). We mark the region of the disk where the X-ray background field dominates $\zeta_X$ (i.e. $\zeta_X, XBGF \geq \zeta_X$).

In the midplane of the disk ($z = 0$) the XBGF dominates for $r \gtrsim 20$ au. Assuming a geometrically flat disk, the XBGF dominates in our model for $r \gtrsim 15$ au (we simply projected the small-
Fig. 10. X-ray ionization rate in the midplane (left panel) and for a vertical cut at $r = 150$ au (right panel) for models with fixed stellar X-ray luminosity ($L_X = 10^{30}$ erg s$^{-1}$) but varying X-ray background fields with fluxes of $2 \times 10^{-4}$ (blue), $2 \times 10^{-5}$ (brown) and $2 \times 10^{-6}$ erg cm$^{-2}$ s$^{-1}$ (red); the black lines are for the model without an XBGF. The solid lines are for the full X-ray spectra (0.1 – 20 keV); the dotted and dashed lines correspond to models with a low-energy cut-off at 0.3 keV and 1 keV, respectively. The horizontal lines mark the cosmic-ray ionization rates for the ISM ($\zeta_{CR} \approx 10^{-17}$), and low cosmic-ray case ($\zeta_{CR} \approx 10^{-19}$ s$^{-1}$). In the right panel the vertical grey solid line indicates the scattering surface at $N_{H(\text{tot})} = 2 \times 10^{24}$ cm$^{-2}$ (see also Fig. 7).

In Fig. 10 we show $\zeta_X$ in the midplane and for a vertical cut at $r = 150$ au for models with different XBGF fluxes and a fixed stellar X-ray luminosity of $L_X = 10^{30}$ erg s$^{-1}$. Additionally we show models with a low energy cut-off for the stellar and XBGF spectrum at 0.3 and 1 keV, respectively. With this low energy cut-off we simulate (in a simple way) a possible absorption of the X-rays before they actually impinge on the disk. Such an absorption can happen by material close to the star (e.g. accretion columns Grady et al. 2010) for the stellar X-rays and in case of the X-ray background field additional extinction due to the interstellar medium is also possible. The corresponding absorption columns required for those cut-offs are $N_{H(\text{tot})} \approx 10^{21}$ cm$^{-2}$ for 0.3 keV and $N_{H(\text{tot})} \approx 10^{22}$ cm$^{-2}$ for 1 keV (see Fig. 4 and Ercolano et al. 2009).

As seen from the left panel of Fig. 10, $\zeta_X$ at the outer radius of the disk can be as high as $10^{-14}$ s$^{-1}$ but strongly depends on the assumed low energy cut-off. Adams et al. (2012) also estimated $\zeta_X$ for their benchmark X-ray background field ($F_{\text{XBGF}} = 2 \times 10^{-5}$ erg cm$^{-2}$ s$^{-1}$) assuming an average X-ray photon energy of $E_X = 1$ keV, they find $\zeta_X = 8 \times 10^{-17}$ s$^{-1}$. This is similar to our model with the 0.3 keV low energy cut-off.

The low energy cut-off has no significant impact on the radius down to which the XBGF dominates $\zeta_X$. For this high density regions only the most energetic X-rays, which are not affected by the low energy cut-off, are of relevance. However, as seen from Fig. 10 a possible absorption of the XBGF photons before they reach the disk has a significant impact for radii $r \approx 200$ au and at higher layers of the disk. For the 1 keV-cut-off $\zeta_X$ can be lower by more than an order of magnitude compared to the reference model with a minimum X-ray energy of 0.1 keV.

More important than the value of $\zeta_X$ at the outer disk radius is the value at higher densities where the actual emission from molecular ions originates. From Fig. 10 we can see that $\zeta_X$ drops already below the ISM cosmic-ray ionization rate at $r \approx 200$ au even for the strongest XBGF considered. However, for the low cosmic-ray case the XBGF can be the dominant high energy ionization source in the midplane for radii as small as $r \approx 50$ au. This is also seen in the right panel of Fig. 10, depending on the XBGF flux $\zeta_X$ can reach values around $5 \times 10^{-18}$ s$^{-1}$ close to the midplane of the disk at $r = 150$ au.

3.2. Molecular ion column densities

In this Section we show results for the radial column density profiles of the disk ionization tracers HCO$^+$ and N$_2$H$^+$. We use these two molecules because they are the most commonly detected molecular ions in disks (e.g. Thi et al. 2004; Dutrey et al. 2007; Öberg et al. 2011a; Guilloteau et al. 2016) and because they trace different regions in the disk.

HCO$^+$ and N$_2$H$^+$ are mainly formed via proton exchange of H$_3^+$ with CO and N$_2$, respectively. The main destruction pathway is dissociative recombination with free electrons, where the metals (e.g. sulphur) play a significant role as additional electron donors (e.g. Graedel et al. 1982; Teague et al. 2015; Kamp et al. 2013; Rab et al. 2017b). HCO$^+$ and N$_2$H$^+$ are sensitive to high energy ionization sources such as X-rays and cosmic-rays, because the formation of H$_3^+$ involves the ionization of H$_2$ (15.4 eV ionization potential).

Besides free electrons another efficient destruction pathway for N$_2$H$^+$ and HCO$^+$ are ion-neutral reactions. N$_2$H$^+$ is efficiently destroyed by CO and therefore resides mainly in regions where gas phase CO is depleted (e.g. frozen-out). This makes it a good observational tracer of the CO ice line in disks (e.g. Qi et al. 2013; Aikawa et al. 2015; van’t Hoff et al. 2017). In case of HCO$^+$, gas phase water is the destructive reaction partner. Observations of protostellar envelopes indicate that HCO$^+$ is indeed sensitive to the water gas phase abundances (e.g. Jørgensen et al. 2013; Bjerkeli et al. 2016; van Dishoeck et al. 2014). In disks this is more difficult to observe, due to the more complex structure and because the water snow line in disks is located at much smaller radii ($r \approx 1$ au for a T Tauri star) compared to CO ($r \approx 20$ au). However, HCO$^+$ follows mainly the distribution of gas phase CO in the disks, whereas N$_2$H$^+$ traces regions where CO is frozen-out (i.e. where the temperature is $\leq 25$ K).
For the abundance of the molecular ions also the so called sink-effect for CO and N$_2$ is of relevance. The main mechanism of the sink-effect is the conversion of CO and N$_2$ to less volatile species which freeze-out at higher temperatures or remain on the dust grains. This can happen via surface chemistry and/or via dissociation of neutral molecules by He$^+$ (e.g. Aikawa et al. 1996; Bergin et al. 2014; Cleeves et al. 2015; Helling et al. 2014; Furuya & Aikawa 2014; Rebousin et al. 2015; Aikawa et al. 2015). The main consequence of the sink-effect is the depletion of gas phase CO and N$_2$ in regions with temperatures above their respective sublimation temperatures. However, the efficiency of the sink-effect is not very well understood as it depends on various chemical parameters (see Aikawa et al. 2015 for more details). In our model only the He$^+$ sink-effect is considered.

Our model also includes excited H$_2$ chemistry that opens up another formation pathway for HCO$^+$. This formation pathway can be important close to the C$^+$/C transition (see Greenwood et al. 2017 and Appendix D). The relevance of this pathway will be discussed later on.

The typical abundance structure for HCO$^+$ and N$_2$H$^+$ in our reference model is presented in Rab et al. (2017b). Here we focus on the radial column densities because they can be more easily compared to observations and other thermo-chemical disk models.

### 3.2.1. Impact of dust grain size distributions on chemistry

In Fig. 11 we show the molecular ion column densities $N_{\text{HCO}^+}$ and $N_{\text{N}_2\text{H}^+}$ for the three different dust models, small grains (SG), medium grains (MG) and large grains (LG) described in Sect. 2.2.1. For each dust model also both cases of cosmic-ray ionization rates, low and ISM cosmic rays are shown (Sect. 2.2.2). Further we show models with and without X-ray dust opacities. All models shown in Fig. 11 have $L_X = 10^{30}$ erg s$^{-1}$ and no X-ray background field.

It is clearly seen in Fig. 11 that neither for the medium grains nor for large grains the inclusion of X-ray dust opacities has a significant impact on the molecular ion column densities. Only for N$_2$H$^+$ a slight decrease on the column density can be seen in the models with low cosmic rays (e.g. compare model MG gas with MG gas+dust). The column densities are not significantly affected by including X-ray dust opacities as the strongest impact of the dust on $X$ is limited to regions close to the midplane (see Fig. 7). There CRs mostly dominate the molecular ion abundances as the X-ray ionization is typically $\zeta_X \ll 10^{-19}$ s$^{-1}$, even if dust opacities are not included. Further the contribution to the molecular ion column densities from regions close to the midplane is limited as the parent molecules of the ions are frozen out anyway. The situation is different for the SG model, where $\zeta_X$ is affected by the dust at all disk layers (see Fig. 7) and $N_{\text{HCO}^+}$ and $N_{\text{N}_2\text{H}^+}$ can drop by factors of three to ten. This shows that it is justified, in case of HCO$^+$ and N$_2$H$^+$, to neglect X-ray dust opacities for evolved disk dust populations but not necessarily for ISM like dust.

Fig. 11 also shows that, independent of the X-ray dust opacities, the dust grain size distributions themselves have a significant impact on the molecular column densities. In the SG model the gas disk is more efficiently shielded from the stellar and interstellar UV radiation field but also the total dust surface per hydrogen nucleus increases significantly (see Table 2). This has mainly two consequences:

- Firstly, the ionization of metals such as carbon and sulphur is significantly reduced. This causes a decrease in the number of free electrons available for the dissociative recombination with...
molecular ions. On the other hand the impact of the dust opacities on the X-ray disk radiation field (and on $\zeta_X$) is less significant (SG model), or not significant at all (MG and LG model) compared to the impact of the dust on the UV radiation field. Consequently the abundance of the molecular ions increases in regions which are efficiently shielded from the UV radiation fields by the presence of small grains.

Secondly, the freeze-out and the sink-effect become more important if the total dust surface increases. This reduces the abundance of molecular ions in high density regions that are efficiently shielded from UV radiation (i.e. no photo-desorption).

These effects are best seen for $N_{N_2H^+}$. Compared to the LG model, in the SG model the abundance of $N_2H^+$ is reduced close to the midplane of the disk due to the sink-effect and freeze-out (i.e. lower gas phase abundance of the parent molecule $N_2$) but increases in the outer and upper layers of the disk due to the shielding of the UV radiation by small grains (i.e. lower abundance of metal ions). This results in a shift of the $N_{N_2H^+}$ peak to larger radii ($r \approx 150 - 200$ au), and the peak is not tracing the radial CO ice line anymore (which is at $r \approx 45$ au in the SG model). For radii $r \leq 150$ au, $N_{N_2H^+}$ is now dominated by the $N_2H^+$ layer just below the C$^+$/C/CO transition where the X-ray ionization rate is high enough so that $N_2H^+$ survives also in layers with gas phase CO (see Aikawa et al. 2015; van’t Hoff et al. 2017; Rab et al. 2017b). In contrast to the LG grain model, $N_{N_2H^+}$ in the SG model can reach comparable or even higher values in the inner disk ($r \leq 100$ au) compared to the peak value around $r = 150 - 200$ au.

Aikawa et al. (2015) also used two different dust size distributions (ISM like and large grains) for their detailed study on $N_2H^+$ in protoplanetary disks. Their resulting column density profiles are very similar to what is shown in Fig. 11. In the the chemical models of Dutrey et al. (2007) for DM Tau and LkCa 15 the peak in their $N_{N_2H^+}$ profiles are at very large radii ($r \geq 400$ au), which is likely due to their assumed single grain size of 0.1 $\mu$m. Cleeves et al. (2015) used a reduced dust surface area, compared to 0.1 $\mu$m grains, to model $N_{N_2H^+}$ for TW Hya, however they also required a lower cosmic-ray ionization rate ($\zeta_{CR} \approx 10^{-19}$ s$^{-1}$) to match the observed sharp peak in $N_{N_2H^+}$, located close to the CO ice line. A lower cosmic-ray ionization rate decreases the efficiency of the He$^+$ sink-effect. A strong impact of the low-cosmic ray ionization rate on the $N_{N_2H^+}$ peak is not really seen in our models or in the models of Aikawa et al. (2015). This might be caused by differences in the timescales for the sink-effect (Bergin et al. 2014). In our LG model, steady-state for $N_{N_2H^+}$ is already reached at a chemical age of approximately 1 Myr (see Rab et al. 2017b). For the SG models a time-dependent test run with ISM cosmic rays showed that steady-state is only reached after 2 – 3 Myr in regions around the radial CO ice line, whereas at $\approx 1$ Myr the $N_{N_2H^+}$ peak is still tracing the radial CO ice line.

Despite the differences in the various chemical models, they all indicate that the sink-effect plays a crucial role for the shape of the $N_2H^+$ radial column density profile. Further, only models accounting for dust growth are able to reproduce a sharp peak in the $N_{N_2H^+}$ profile near the radial CO ice line as is observed for TW Hya (Qi et al. 2013, but see also Aikawa et al. 2015; van’t Hoff et al. 2017 for a discussion on the robustness of $N_{N_2H^+}$ as a CO ice line tracer). This is consistent with dust observations clearly indicating grain growth and dust settling in disks (e.g. Andrews & Williams 2005; Pinte et al. 2016). In any case the chemical modelling results for $N_{N_2H^+}$ indicate that $N_2H^+$ is not only a tracer of the radial CO ice line but also for dust evolution in disks.

3.2.2. Impact of X-ray background fields on chemistry

To show the impact of X-ray background fields (XBF) on the molecular column densities we compare in Fig. 12 models with $L_X \approx 10^{19}$ erg s$^{-1}$ but varying XBF fluxes. We also include models with a low-energy cut-off at 1 keV to show the impact of the possible absorption of soft X-rays before they reach the disk (see also Sect. 3.1.3). For each of these models the results for low and ISM cosmic rays are shown. For all models the large grains dust model is used.

For the case of the ISM cosmic-ray ionization rate the impact of the XBF on the column densities is limited. Only for models with the highest XBF flux of $2 \times 10^{-5}$ erg cm$^{-2}$ s$^{-1}$ the column densities increase by more than a factor of three for radii $r \geq 200$ au. Although the XBF dominates the X-ray ionization rate down to $r \approx 20$ au, $\zeta_X > \zeta_{CR}$ is true only for $r \geq 200$ au, and only for the case of the strongest XBF (see Fig. 10).

The impact of the XBF is much larger in the case of a low CR ionization rate. In that case the molecular ion column densities are generally lower compared to ISM CRs and the relative impact of the XBF increases. However, the impact on $N_{HCO^+}$ remains limited; only for the strongest XBF, $N_{HCO^+}$ increases by about a factor of five at most. For $N_{N_2H^+}$ the picture is quite different. Due to the low CRs the column densities for $r \approx 200$ au are reduced by more than an order of magnitude compared to the ISM CR models. In these regions the XBF is now most effective and consequently $N_{N_2H^+}$ increases significantly. For the strongest XBF $N_{N_2H^+}$ increases by up to two orders of magnitude for $r \approx 200$ au and reaches levels similar to the ISM CR models. The reason why $N_2H^+$ is more sensitive to the high energy ionization sources is its location in the disk. Compared to HCO$^+$, $N_2H^+$ is mainly located in deeper layers of the disk; below the CO ice line. In those layers, the ionization balance is mostly dominated by molecular ions, as the ionization of atomic metals by UV becomes less important.

In the models with a low-energy cut-off at 1 keV for the X-ray spectra, HCO$^+$ is not affected by the XBF even in the low CR model. Also the impact on $N_{N_2H^+}$ is now weaker. $N_{N_2H^+}$ is typically a factor of a few up to an order of magnitude lower compared to the models with a cut-off at 0.1 keV. Although we use the low-energy cut-off also for the stellar X-rays, such a drop in the column densities is not seen in the models without XBF's. The reasons are the geometrical dilution of the stellar X-ray radiation and that the stellar X-rays have to penetrate the high radial and vertical column densities in the inner disk. The XBF irradiates the disk isotropically and only has to penetrate the low column densities of the outer disk. Therefore also the low-energy X-rays can penetrate larger areas of the disk and have more impact on $\zeta_X$ in disk regions relevant for the molecular ions.

For HCO$^+$ we actually also see a drop in the column density for $r \approx 400$ au for the strongest XBF. The reason for this is a lower CO abundance caused by X-ray photo-dissociation which is also included in our chemistry model. The CO abundance at $r \approx 450$ au drops by factors of approximately three to five down to heights of $z \approx 20$ au, which results in a drop of the HCO$^+$ abundance by nearly an order of magnitude. The situation is similar for $N_2$ and $N_2H^+$, however the abundance of $N_2H^+$ is already below $10^{-12}$. As noted (Sect.3.2) our model includes also chemistry of excited molecular hydrogen $H_2^*$. This opens up a formation channel for HCO$^+$ via the ion-neutral reaction of $H_2^*$ with $C^+$ (see Appendix D for details). In the inner disk this reaction is only effective in a very thin layer at the $C^+/C$/CO transition. However, in the outer disk for $r \geq 300$ au this reaction becomes significant, as
the C*/C/CO transition is not as sharp as in the inner disk. If this reaction is deactivated, we find that for such a model the slope of \( N_{\text{HCO}^+} \) for \( r > 300 \text{ au} \) becomes steeper. However, our findings concerning the impact of XBGFs are not significantly affected, \( N_{\text{HCO}^+} \) becomes slightly more sensitive to XBGFs for \( r \gtrsim 300 \text{ au} \) and X-ray photo-dissociation becomes less significant for \( N_{\text{HCO}^+} \) at large radii where \( N_{\text{HCO}^+} \) drops below \( 10^{10} \text{ cm}^{-2} \) (\( r \approx 400 \text{ au} \)). The results for \( N_{\text{H}_2^+} \) are not affected by \( \text{H}_3^+ \) chemistry.

4. Discussion

4.1. Observational implications of X-ray background fields

Our results indicate that the molecular ion column densities in the outer disk are sensitive to X-ray background fields. At least for \( \text{H}_2^+ \) the effect on the column density can be strong enough to be observable with modern (sub)millimetre telescopes like ALMA (Atacama Large Millimeter Array), NOEMA (NOrthern Extended Millimeter Array) and SMA (Submillimeter Array). However, our results also show that certain conditions such as a strong XBGF and low CR ionization rates are required.

The typical value for the X-ray background flux in young embedded clusters of \( 2 \times 10^{-5} \text{ erg cm}^{-2} \text{ s}^{-1} \) corresponds to cluster member sizes with \( N < 3000 \), typical for clusters in the solar vicinity (Adams et al. 2012). However, this value drops to \( \lesssim 10^{-5} \text{ erg cm}^{-2} \text{ s}^{-1} \) for smaller clusters with \( N \approx 100 \), which is more typical for the Taurus star formation region; the X-ray XEST survey detected 136 X-ray sources (Güdel et al. 2007a). A typical disk in Taurus would only be affected by an XBGF if it is shielded efficiently from cosmic-rays (see Fig. 12). However, even in a small cluster some of the sources might experience a higher X-ray background flux depending on their location within the cluster (e.g. closer to the cluster center, see Adams et al. 2012). To identify such sources a large sample of spatially resolved \( \text{N}_2\text{H}^+ \) observations (see below) would be required. The current number of \( \text{N}_2\text{H}^+ \) detections in protoplanetary disk is less than ten (Dutrey et al. 2014) and it is therefore not surprising that signatures of XBGF have not been found yet.

Due to the rather poor knowledge concerning the impact of individual high-energy ionization sources on disk chemistry (see e.g. Rab et al. 2017b) and as can only the stellar X-ray luminosity can be measured, it will be certainly challenging to discriminate the influence of XBGFs from the stellar high-energy ionization sources (X-rays and stellar energetic particles), cosmic-rays and radionuclide ionization. However, all these ionization sources are different in the way they irradiate the disk.

The stellar high energy ionization sources have less impact on the outer disk; they need to penetrate the high densities in the inner disk and also experience geometric dilution as they irradiate the disk as a point source (see also Rab et al. 2017b). Cosmic rays irradiate the disk isotropically and therefore have an impact on the whole disk. Due to their high energies, CRs are only significantly absorbed in the inner disk (\( r \lesssim 10 \text{ au} \)) and provide therefore a nearly constant \( \text{H}_3^+ \) ionization rate for the bulk of the disk material (this is similar for radionuclide ionization). In contrast to CRs, the XBGF experiences significant absorption by the disk material even in the outer disk. Those differences result in different shapes of the \( \text{N}_2\text{H}^+ \) radial column density profiles as is seen in Fig. 12. XBGFs make the profile shallower as the impact on the molecular column densities decreases for smaller disk radii (measured from the star). In contrast, a change in the CR ionization rate affects the radial column density profile at all radii.

In any case modelling of spatially resolved \( \text{N}_2\text{H}^+ \) observations of disks are required to discriminate the contribution of XBGF to disk ionization. Such observations for T Tauri disks...
are still rare (Dutrey et al. 2007; Qi et al. 2013) but certainly will become more common in the near future due to the significant advances, in particular in terms of spatial resolution, of modern (sub)mm interferometers.

4.2. UV background fields and external photo-evaporation

For all models presented here we assumed the canonical value for the interstellar UV radiation of $\chi_{\text{ISM}} = 1$ (in units of the Draine field). This is a reasonable assumption for low-mass star formation regions as an enhanced UV background field would be mostly produced by massive stars with spectral type O, B and A. In contrast to the UV field, the X-ray background field is mainly produced by X-ray emission of solar-like low mass stars (see Adams et al. 2012). However, a presence of an enhanced UV background field certainly has an impact on the outer disk due to photo-dissociation of molecules, photo-desorption of ices and photo-ionization of metals (see e.g. Teague et al. 2015). These processes will reduce the abundances of molecular ions in the outer disk as their parent molecules are dissociated and metals like carbon and sulphur are ionized and will therefore dominate the ionization balance. Consequently, the presence of an enhanced UV background field will lower the impact of the XBGF on the outer disk molecular abundances. In high-mass star formation regions like Orion with UV background fields up to $\chi_{\text{ISM}} \approx 10^3$, most likely the UV field will completely dominate the chemistry in the outer disk (Walsh et al. 2013; Antonelli et al. 2015).

There is evidence that already weak UV background fields $\chi_{\text{ISM}} \gtrsim 4$ can drive photo-evaporation of the outer disk (Haworth et al. 2017, but see also Adams 2010; Williams & Cieza 2011). Such a process is not included in our model. However, we do not expect a huge impact of photo-evaporation on our results. For the X-ray RT mainly the column density matters that photons have to penetrate until they reach the regions of the disk where the molecular ions become abundant. These column densities are not significantly affected if parts of the outer disk material would slowly drift radially outwards.

On the other hand XBGFs can act as an additional heating source for the outer disk and therefore could contribute to external disk photo-evaporation. We find that only the strongest X-ray background field with $F_{\text{XBGF}} \approx 2 \times 10^{-4}$ erg cm$^{-2}$ s$^{-1}$ has a significant impact on the gas temperature in our models. In the midplane of the disk at $r \approx 500$ au ($n(H) \approx 4 \times 10^3$ cm$^{-3}$), the gas temperature increases from about $T_g \approx 24$ K to $T_g \approx 36$ K, where for the canonical XBGF we find only an increase of about 2 K (always $\chi_{\text{ISM}} = 1$ is used). Those gas temperatures are lower than the typical temperatures reported by Facchini et al. (2016) derived from hydrodynamical disk photo-evaporation models with $\chi_{\text{ISM}} \gtrsim 30$. This indicates that in the presence of a modestly enhanced UV background field, XBGFs would play a rather minor role for external disk photo-evaporation. However, a more detailed investigation of the possible importance of XBGFs for external disk photo-evaporation is required to be more quantitative.

4.3. The role of dust evolution

The properties of the dust and its evolution has a significant impact on the chemical structure of the disk (e.g. Vasyunin et al. 2011; Akimkin et al. 2013; Woitke et al. 2016). Important dust evolution processes are dust growth, dust settling and radial migration of (sub)mm sized grains. Individual disks likely will show different dust properties as dust evolution proceeds over time and also depends on various parameters such as the turbulence in the disk (see Birnstiel et al. 2016 for a recent review). It is, therefore, crucial to have good knowledge of the dust disk (e.g. from continuum observations) for modelling of molecular line emission of individual protoplanetary disks. In the following, we briefly discuss the impact of dust evolution on our results and possible shortcomings of our dust model.

In our modelling approach, we do include methods to simulate dust growth and dust settling (see Sections 2.1.2 and 2.2.1). The models with varying grain size distributions indicate a significant impact of the assumed grain size on the radial column densities of HCO$^+$ and N$_2$H$^+$ (see Sect. 3.2.1). We also did run disk models using the large grains dust model but varied the degree of settling (i.e. no settling at all and strong settling with $\alpha_{\text{sett}} \approx 10^{-4}$). For the case of strong settling, the HCO$^+$ and N$_2$H$^+$ column densities change at most by a factor of three where HCO$^+$ is more sensitive than N$_2$H$^+$. In the non-settled disk model, only N$_2$H$^+$ is affected where the column density drops by about an order of magnitude around $r = 100$ au. However, the relative impact of X-ray background fields on the molecular column densities is similar to the models presented in Sect. 3.2.2 and consequently our conclusions concerning the impact of X-ray background fields are not affected. Nevertheless, for modelling of molecular observations of individual disks, it is also necessary to consistently model the dust component. The model presented here is well suited for such modelling, as the same dust model is used for the radiative transfer (X-ray to mm), the chemistry and also for the calculation of synthetic observables such as spectral energy distributions and spectral line emission (see Woitke et al. 2016).

Not included in our model is the inward radial migration of large dust grains. Spatially resolved (sub)mm observations indicate that the radial extent of dust emission is significantly smaller than the molecular gas emission (for CO see e.g. de Gregorio-Monsalvo et al. 2013; Cleeves et al. 2016). However, models indicate that the difference in the extent of the dust and gas emitting areas might be an optical depth effect (Woitke et al. 2016; Facchini et al. 2017). Nevertheless, radial migration of large dust particles can have an impact on the molecular abundances in the outer disk as shown by Cleeves (2016) for CO. The models of Cleeves (2016) show that the depletion of large dust grains in the outer disk can increase the CO gas phase column density by about a factor of two, compared to models without radial migration. This will also likely also have an impact on the HCO$^+$ and N$_2$H$^+$ column densities.

We do not expect that radial migration affects our general conclusions on the impact of X-ray background fields. The changes in the molecular ion abundances in the outer disk are purely driven by an increase of the X-ray ionization rate. It is unlikely that the X-ray ionization rate is strongly affected by the depletion of large dust grains in the outer disk, as in that case the X-ray opacities are dominated by the gas, similar to our large dust grains model (see Fig. 4). The impact of radial migration on the molecular ion abundances is an interesting aspect which certainly deserves more detailed investigations. However, such a study is out of the scope of this paper.

Recent ALMA observations have shown azimuthally symmetric gap- and ring structures in the disk emission of (sub)mm sized dust grains (e.g. ALMA Partnership et al. 2015; Andrews et al. 2016; Isella et al. 2016). Although the dust depletion in the gaps has an impact on the molecular gas phase abundances (e.g. Teague et al. 2017), those rings are rather narrow (width $\leq 10$au, Pinte et al. 2016) and the global radial distribution of the molec-
ular column densities remains intact. Therefore our main conclud-
sions concerning the impact of X-ray background fields are not
significantly affected by the presence of gaps.

5. Summary and conclusions

We introduced a new X-ray radiative transfer module for the ra-
diation thermo-chemical disk code PtoDiMo. This new mod-
ule includes X-ray scattering and a detailed treatment of X-ray
dust opacities, which can be applied to different dust composi-
tions and dust size distributions. We investigated the import-
ance of X-ray scattering, X-ray dust opacities and X-ray back-
ground fields of embedded young clusters for the X-ray ionization rates
by means of a representative T Tauri protoplanetary disk model.
Further, we studied the impact of X-ray background fields on the
disk chemistry, where we used the observed disk ionization
tracers HCO⁺ and N₂H⁺. Our main conclusions are:

- For evolved dust size distributions (e.g. including grain
growth) X-ray opacities are mostly dominated by the gas,
only for energies $E_X \gtrsim 5 \to 10 \text{keV}$ dust opacities become re-
levant. Consequently the disk X-ray ionization rates are only
reduced in high density regions close to the midplane if dust
opacities are included in the X-ray RT. For ISM like dust size
distributions (i.e. maximum grain size $\lesssim 0.1 \mu m$) the X-ray
ionization rate is affected throughout the disk and is reduced
by more than an order of magnitude due to efficient absorp-
tion of X-rays by the dust.

- For a typical X-ray background flux, as expected for embed-
yed young clusters in the solar vicinity, the XBGF dominates
disk ionization processes including cosmic rays, radionuclide
ionization (not presented in this study), stellar energetic particles
(Rab et al. 2017b) and X-rays (stellar and interstellar). How-
ever, further observational constraints are required to constrain
the disk ionization fraction and to better understand molecu-
lar ion chemistry. Next to a good knowledge of the stellar (i.e. UV
and X-ray radiation) and disk properties, spatially resolved ob-
servations of molecular ions such as N₂H⁺ and HCO⁺ are most
crucial. Such observations are still rare but will likely be quite
common in the near future due to the modern (sub)millimetre
interferometers like ALMA, NOEMA and SMA.

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Fig. A.1. Comparison of X-ray photoelectric (absorption) cross-sections per hydrogen nucleus as a function of photon energy. The red line shows the gas absorption cross-section from Igea & Glassgold (1999). The brown lines show the cross-sections derived by Bethell & Bergin (2011). The black lines show the PRODiMO results for the large grains dust model.

Appendix A: Comparison of X-ray photoelectric cross-sections

In Fig. A.1, we compare the X-ray photoelectric cross-sections as used in PRODiMO to the cross-sections derived by Igea & Glassgold (1999) and Bethell & Bergin (2011). For the PRODiMO case we used the depleted element abundances (Kamp et al. 2017) assuming all hydrogen is in H$_2$ and all other elements are present as neutral atoms. For the dust, we use the large grains dust model (see Table 1) and the opacity calculations as described in Sect. 2.3.3.

For the Igea & Glassgold (1999) cross-sections, we used their Eq. 10 for the case of heavy element depletion. Igea & Glassgold (1999) did not include a treatment of the absorption edges and also neglected the dust component. For the Bethell & Bergin (2011) cross-sections we used their Eq. 1 with the corresponding fitting coefficients for their “Gas” case (their Table 2); for the dust we used the coefficients for their dust size distribution with $a_{\text{min}} = 0.01 \mu m$, $a_{\text{max}} = 1000 \mu m$ and $a_{\text{pow}} = 3.5$ (their Table 3). We note that Bethell & Bergin (2011) did not use Mie theory for the opacity calculations but rather used directly the photo-electric cross-sections for the atoms and assumed that all heavy metals (except noble gases) and a certain fraction of C and O are in solid form. To account for different dust sizes they used self-blanketing factors.

The deviations between Igea & Glassgold (1999) and PRODiMO cross-sections are on average $\approx 20\%$ with a maximum of $\approx 30\%$. For the Bethell & Bergin (2011) cross-sections we find deviations of $\approx 10\%$ with a maximum of $\approx 50\%$, relative to PRODiMO. The agreement for the gas cross-section is remarkably good considering that we did not adapt the exact same element abundances (although in all three cases some form of depleted abundances are used).

The Bethell & Bergin (2011) dust cross-sections are about a factor of 1.2 -- 2 higher than the PRODiMO cross-sections. The differences are probably caused by the different dust properties (e.g. in the PRODiMO case $a_{\text{max}} = 3000 \mu m$). However, considering the general uncertainties connected to X-ray dust opacities the agreement is quite good.

Appendix B: Comparison to the Monte Carlo X-ray radiative transfer code MOCASSIN

Ercolano & Glassgold (2013) presented a comparison of the 3D Monte Carlo radiative transfer and photoionization code MOCASSIN (Ercolano et al. 2008b) to the Monte Carlo X-ray radiative transfer model of Igea & Glassgold (1999). For the comparison a minimum mass solar nebula disk model is used (see Igea & Glassgold 1999 for details). The X-ray emitting source is modelled via two rings with radius 5 $R_\odot$ located at a height of 5 $R_\odot$ above and below the star. Dust absorption and scattering is not considered in those models. Ercolano & Glassgold (2013) found a good agreement for the resulting X-ray ionization rates per hydrogen nucleus between the two codes.

In Fig. B.1 we show a comparison of our X-ray radiative transfer model to the results from MOCASSIN. For this comparison we used the same physical disk parameters and the same initial element abundances (the “IG99 depleted”) as given in Ercolano & Glassgold (2013). The X-ray luminosity is $L_X(1 - 20 \text{ keV}) = 10^{29} \text{ erg s}^{-1}$ and the spectrum has a single temperature of $k T_X = 5 \text{ keV}$. In contrast to the models presented in Ercolano & Glassgold (2013) we assume that the X-rays are emitted at the stellar surface. The X-ray ionization rate $\zeta_X$ is simply calculated for the given initial abundances (i.e. all species are neutral and all hydrogen is in molecular form) without solving for the chemistry.

As seen from Fig. B.1, the agreement of the two codes is quite good but there are also some significant differences. We want to emphasize that the radiative transfer methods used are very different. MOCASSIN uses the Monte Carlo approach with a proper treatment of anisotropic scattering. In PRODiMO, we apply a ray-base method (discrete-ordinates) with a simple approximation for the anisotropic scattering. Scattering dominates $\zeta_X$ for $N_{\text{H$_2$}} \gtrsim 10^{25} \text{ cm}^{-2}$ (scattering shoulder Igea & Glassgold 1999). In this region the results of both codes are within a factor of three, indicating that our simplified treatment of anisotropic scattering is a reasonable approximation.

Fig. B.1. Comparison of the X-ray ionization rate $\zeta_X$ as a function of vertical hydrogen column density $N_{\text{H$_2$},\text{ver}}$ at radii of 1 au (solid lines), 5 au (dashed lines) and 10 au (dotted line). The red lines are the results from MOCASSIN, the black lines are the results from PRODiMO. The 10 au result from MOCASSIN were not available for this test case. The 10 au results have been scaled down by a factor of 10 for better visibility. The gray shaded area indicates a factor of three deviation relative to the PRODiMO results. An isothermal X-ray spectrum with $k T_X = 5 \text{ keV}$ and $L_X = 10^{29} \text{ erg s}^{-1}$ is used.
The largest differences are actually at low column densities of \(N_{\text{H},\text{ver}} \leq 10^{23} \text{ cm}^{-2}\) where \(\zeta_X\) is solely dominated by absorption of low energy X-ray photons (here \(E_X \approx 1 \text{ keV}\)). Those deviations might be caused by the exact treatment of the low energy-cut off for the X-ray spectrum. We did run a test with a cut-off at 1.1 keV in that case \(\zeta_X\) drops by a factor of a few at low column densities but is not affected at high column densities. However, we also performed a test with twice as much energy bands in our X-ray RT to more accurately treat the low energy cut-off, but we did not find significant differences. So, the origin of these deviations remains rather unclear. Although \(\zeta_X\) at low columns is relevant for photo-evaporative winds (e.g. Ercolano et al. 2008a) it is of less relevance for our here presented models as we are mainly interested in the impact of X-ray ionization on the chemistry.

The deviations around \(N_{\text{H},\text{ver}} = 10^{23} \text{ cm}^{-2}\) are likely caused by the different locations of the X-ray emitting source. Compared to a pure stellar X-ray source, the X-ray photons emitted by an elevated ring source have encountered a lower column of material when they reach a certain height of the disk (see also Igea & Glassgold 1999). At larger distances the geometrical effects (e.g. incident angle on the disk surface) are less severe. The actual location of the X-ray source in T Tauri stars is not well known which is a general uncertainty in the models. However, as discussed by Ercolano et al. (2009) there are observational indications for a location of the X-ray source at or very close (\(\leq 1 R_S\)) to the stellar surface.

In Fig. B.2, we present a similar comparison as in Fig. B.1 but for a flared X-ray spectrum with \(L_X(1 - 20 \text{ keV}) = 2 \times 10^{31} \text{ erg s}^{-1}\) and \(kT_X = 12 \text{ keV}\) (the COUP flared spectrum in Ercolano & Glassgold 2013).

Appendix C: X-ray photoelectric cross-sections for PAHs

In Fig. C.1 we show the photo-electric (absorption) cross-section of PAHs (Polycyclic aromatic hydrocarbons) in comparison to the X-ray gas and dust cross-sections used in our reference model (i.e. large grains dust model; see Fig. 4). The PAH absorption cross-sections are from Li & Draine (2001)\(^1\). They provide absorption cross-sections for various PAH sizes in the X-ray energy domain up to 2 keV, assuming graphite-like optical properties. We used neutral PAH particles with 54 carbon and 18 hydrogen atoms and a radius of \(\approx 4.87 \times 10^{-4} \mu\text{m}\) (the same PAH properties as are used for our chemical model) and considered an ISM like PAH abundance of \(\approx 2.8 \times 10^{-7}\) (Tielens 2008). Further details on the treatment of PAHs in our model can be found in Woitke et al. (2016).

It is clear from Fig. C.1 that, compared to the gas, PAHs play an insignificant role in the X-ray radiative transfer and for the disk X-ray radiation field. Furthermore, the PAH abundance in disks around T Tauri stars is likely significantly lower than in the ISM (e.g. Geers et al. 2006), which further reduces the importance of PAHs as an opacity source (similar to the far-UV wavelength regime, see Woitke et al. 2016). For all models presented in this paper, we assumed a PAH abundance reduced by an elevated ring source have encountered a lower column of material when they reach a certain height of the disk (see also Igea & Glassgold 1999). At larger distances the geometrical effects (e.g. incident angle on the disk surface) are less severe. The actual location of the X-ray source in T Tauri stars is not well known which is a general uncertainty in the models. However, as discussed by Ercolano et al. (2009) there are observational indications for a location of the X-ray source at or very close (\(\leq 1 R_S\)) to the stellar surface.

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\(\zeta_X\) is solely dominated by absorption of low energy X-ray photons (here \(E_X \approx 1 \text{ keV}\)). Those deviations might be caused by the exact treatment of the low energy-cut off for the X-ray spectrum. We did run a test with a cut-off at 1.1 keV in that case \(\zeta_X\) drops by a factor of a few at low column densities but is not affected at high column densities. However, we also performed a test with twice as much energy bands in our X-ray RT to more accurately treat the low energy cut-off, but we did not find significant differences. So, the origin of these deviations remains rather unclear. Although \(\zeta_X\) at low columns is relevant for photo-evaporative winds (e.g. Ercolano et al. 2008a) it is of less relevance for our here presented models as we are mainly interested in the impact of X-ray ionization on the chemistry.

The deviations around \(N_{\text{H},\text{ver}} = 10^{23} \text{ cm}^{-2}\) are likely caused by the different locations of the X-ray emitting source. Compared to a pure stellar X-ray source, the X-ray photons emitted by an elevated ring source have encountered a lower column of material when they reach a certain height of the disk (see also Igea & Glassgold 1999). At larger distances the geometrical effects (e.g. incident angle on the disk surface) are less severe. The actual location of the X-ray source in T Tauri stars is not well known which is a general uncertainty in the models. However, as discussed by Ercolano et al. (2009) there are observational indications for a location of the X-ray source at or very close (\(\leq 1 R_S\)) to the stellar surface.

In Fig. B.2, we present a similar comparison as in Fig. B.1 but for a flared X-ray spectrum with \(L_X(1 - 20 \text{ keV}) = 2 \times 10^{31} \text{ erg s}^{-1}\) and \(kT_X = 12 \text{ keV}\) (the COUP flared spectrum in Ercolano & Glassgold 2013). The deviations between the models are similar to the first test case. However, now the impact of the X-ray source location is better visible. In the MOCASSIN models the scattering is located at slightly deeper layers than in the ProDiMo models. Due to the elevated location of the X-ray source the photons experience a lower radial column of material and can penetrate to deeper layers of the disk. The differences for \(N_{\text{H},\text{ver}} > 10^{25} \text{ cm}^{-2}\) are likely of technical nature. As noted by Ercolano & Glassgold (2013) the sudden drop in \(\zeta_X\) is caused by the low number of photons reaching those layers. In the ProDiMo model
by a factor of 100 compared to the ISM. Nevertheless, X-rays might play an essential role for the destruction of PAHs in disks. Due to their high energies, X-ray photons can efficiently destroy PAHs on timescales significantly shorter than typical disk lifetimes (Siebenmorgen & Krügel 2010; Siebenmorgen & Heymann 2012). However, here we are mainly interested in the overall X-ray disk radiation field and the resulting X-ray ionization rates and therefore do not include PAHs in the X-ray radiative transfer.

Appendix D: HCO$^+$ formation pathway via excited molecular hydrogen

The formation pathway for HCO$^+$ via excited molecular hydrogen $H_2^*$ works in the following

$$H_2^* + C^+ \rightarrow CH^+ + H_2 \quad \text{(D.1)}$$
$$CH^+ + H_2 \rightarrow CH_2^+ + H \quad \text{(D.2)}$$
$$CH_2^+ + H_2 \rightarrow CH_3^+ + H \quad \text{(D.3)}$$
$$CH_3^+ + O \rightarrow HCO^+ + H_2 \quad \text{(D.4)}$$

Key here is the reaction $H_2^* + C^+ \rightarrow CH^+ + H_2$, where we use the measured rate of Hierl et al. (1997) with an extrapolation to lower temperatures. However, in particular the rate at low temperatures ($T < 100$ K) is uncertain, and theoretical models indicate significantly lower rates (by orders of magnitude, Zanchet et al. 2013). A more detailed discussion and a comparison of different rates for $H_2^* + C^+$ is presented in Kamp et al. (2017).