

Orbitally Forced Ice Sheet Fluctuations in Snowball Earth

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1 Snowball Earth theory provides a powerful framework for understanding
2 Neoproterozoic panglaciations, although some predictions are apparently
3 contradicted by geological evidence. Snowball theory posits that the
4 panglaciations were terminated after millions of years of fridity by a positive
5 feedback, in which initial warming from rising atmospheric CO₂ was amplified by
6 reduction of ice cover and planetary albedo (1, 2). This threshold behaviour implies
7 that most of the glacial record was deposited in a brief 'melt-back' period (3), an
8 interpretation apparently inconsistent with geological evidence for glacial-
9 interglacial cycles in low palaeolatitudes (4-6). Here we use geological and
10 geochemical evidence combined with numerical modeling experiments to
11 reconcile these apparently conflicting views. New evidence from Svalbard
12 (Norwegian High Arctic) indicates oscillating glacier extent and hydrological
13 conditions within continental deposits of a Cryogenian glaciation, during a period
14 when $p\text{CO}_2$ was uniformly high. Modeling experiments show that such oscillations
15 can be explained by orbital forcing in the late stages of a 'Snowball' glaciation,
16 while $p\text{CO}_2$ was rising towards the threshold required for complete melt-back. This
17 enriched Snowball Earth theory can potentially explain complex successions
18 observed at other localities.

19 The Wilsonbreen Formation in NE Svalbard contains a detailed record of
20 environmental change during the Marinoan, the second of the major Cryogenian
21 glaciations (650-635 Ma) (7, 8). At this time, Svalbard was located in the Tropics on
22 the eastern side of Rodinia (9, 10). The <180 m thick Wilsonbreen Formation was
23 deposited within a long-lived intracratonic sedimentary basin (11). It is subdivided
24 into three members (W1, W2 and W3) based on the relative abundance of diamictite

25 and carbonate beds (7, 8; Fig. 1; Supplementary Figures 1 & 2). The occurrence
26 throughout the succession of lacustrine sediments containing both precipitated
27 carbonate and ice-rafted detritus, and intermittent evaporative carbonates and
28 fluvial deposits, indicates that the basin remained isolated from the sea, consistent
29 with eustatic sea level fall of several hundred metres and limited local isostatic
30 depression (Supplementary Information; 12). This makes it ideal for investigating
31 environmental change within a Neoproterozoic panglaciation, as it provides direct
32 evidence of subaerial environments and climatic conditions.

33 We made detailed sedimentary logs at ten known and new localities extending
34 over 60 km of strike (Fig. 1; Supplementary Figure 1; see Methods). Seven sediment
35 facies associations were identified, recording distinct depositional environments that
36 varied in spatial extent through time (Supplementary Figure 3; Supplementary
37 Information). These are: FA1: *Subglacial*, recording direct presence of glacier ice,
38 FA2: *Fluvial channels*, FA3: *Dolomitic floodplain*, recording episodic flooding,
39 evaporation and microbial communities; FA4: *Carbonate lake margin*, including
40 evidence of wave action; FA5: *Carbonate lacustrine*, including annual rhythmites and
41 intermittent ice-rafted debris; FA6: *Glacilacustrine*, consisting of ice-proximal
42 grounding-line fans (FA6-G) and ice-distal rainout deposits (FA6-D); and FA7:
43 *Periglacial*, recording cold, non-glacial conditions. Additional descriptions are
44 provided in the Supplementary Information. The vertical and horizontal distribution
45 of these facies associations (Fig. 1) allows the sequence of environmental changes to
46 be reconstructed in detail.

47 (1) The base of the Formation is a well-marked periglacially weathered horizon
48 with thin wind-blown sands (Supplementary Figure 4a-b). This surface records very
49 limited sediment cycling in cold, arid conditions.

50 (2) At all localities, the weathering horizon is overlain by fluvial channel facies
51 (FA2) and mudstones, marking the appearance of flowing water in the basin and
52 implying positive air temperatures for at least part of the time (Supplementary
53 Figure 5a).

54 (3) Glacilacustrine deposits (FA6-D) record flooding of the basin and delivery of
55 sediment by ice-rafting (Supplementary Figure 4c-d). Far-travelled clasts are
56 common, indicating transport by a large, continental ice sheet.

57 (4) Warm-based, active ice advanced into the basin, indicated by traction tills and
58 glacitectonic shearing (FA1; Supplementary Figure 4e-g). (1 – 4 make up Member
59 W1.)

60 (5) Ice retreat is recorded by a second periglacial weathering surface (FA7). This is
61 overlain by fluvial channel, floodplain, lake-margin and carbonate lacustrine
62 sediments of W2 (FA2-5; Supplementary Figure 5), recording a shifting mosaic of
63 playa lakes and ephemeral streams. Lakes and river channels supported microbial
64 communities. Millimetre-scale carbonate-siliciclastic rhythmites indicate seasonal
65 cycles of photosynthesis. The environment appears to have been closely similar to
66 that of the present-day McMurdo Dry Valleys in Antarctica, though with less extreme
67 seasonality due to its low latitude (13).

68 (6) Water levels and glacier extent underwent a series of oscillations, recorded by
69 switches between glacilacustrine diamictite (FA6-D) and fluvial, lacustrine and lake-

70 margin sediments (FA2-5) in W2. Sedimentation rates inferred from annual
71 rhythmites in W2 suggest that each retreat phase may have lasted $\sim 10^4$ years.

72 (7) A second major ice advance marks the base of W3, with widespread
73 deposition of subglacial tills and glactectonism of underlying sediments. Basal tills
74 are absent from the northernmost locality, but close proximity of glacier ice is
75 recorded by grounding-line fans (FA6-G; Supplementary Figure 4h-i).

76 (8) Ice retreated while the basin remained flooded and glacial sediment
77 continued to be delivered to the lake by ice rafting. Thin laminated carbonates (FA5)
78 in W3 indicate periods of reduced glacial sedimentation, indicative of minor
79 climatic fluctuations over timescales of $\sim 10^3$ years (Supplementary Figure 5g).

80 (9) A sharp contact with overlying laminated 'cap' carbonate (Supplementary
81 Figure 2) records the transition to post-glacial conditions. At some localities, basal
82 conglomerates provide evidence of subaerial exposure followed by marine
83 transgression. The cap carbonate closely resembles basal Ediacaran carbonates
84 elsewhere, and marks global deglaciation, eustatic sea-level rise and connection of
85 the basin to the sea (1, 12, 14).

86 Environmental and atmospheric conditions during deposition of W2 and W3 can
87 be further elucidated by isotopic data from carbonate-associated sulphate in
88 lacustrine limestones (Fig. 2 and Supplementary Figure 6). These display negative to
89 extremely negative $\Delta^{17}\text{O}$ values with consistent linear co-variation with $\delta^{34}\text{S}$,
90 indicating mixing of pre-glacial sulphate and isotopically light sulphate formed in a
91 CO_2 -enriched atmosphere (15, 16). The observed values could reflect non-unique
92 combinations of $p\text{CO}_2$, $p\text{O}_2$, O_2 residence time and other factors, but a box model
93 (17) indicates $p\text{CO}_2$ was most likely ~ 10 to 100 mbar (1 mbar = 1000 ppmv).

94 These values are far too high to permit formation of low-latitude ice sheets in the
95 Neoproterozoic, but they are consistent with a late-stage Snowball Earth. For an ice-
96 free Neoproterozoic Earth, model studies indicate mean terrestrial temperatures in
97 the range 30-50°C for $p\text{CO}_2 = 10$ to 100 mbar (18). Formation of low-latitude ice
98 sheets requires much lower $p\text{CO}_2$, on the order of 0.1 - 1 mbar (2, 19, 20). Once
99 formed, however, ice sheets can persist despite rising CO_2 from volcanic outgassing,
100 due to high planetary albedo. This hysteresis in the relationship between $p\text{CO}_2$ and
101 planetary temperature is a key element of Snowball Earth theory. It implies that W2
102 and W3 were deposited relatively late in the Marinoan, after volcanic outgassing had
103 raised $p\text{CO}_2$ from 0.1 or 1 mbar to 10 or 100 mbar. Modeled silicate weathering and
104 volcanic outgassing rates indicate that this would require 10^6 to 10^7 years (21).

105 The consistent co-variation of $\Delta^{17}\text{O}$ and $\delta^{34}\text{S}$ in lacustrine limestones in both W2
106 and W3 suggests no detectable rise in atmospheric $p\text{CO}_2$, as this would alter the
107 slope of the mixing line (Fig. 2). This implies that the glacier oscillations recorded in
108 W2 and W3 occurred during a relatively short time interval ($<10^5$ years, 21) toward
109 the end of the Marinoan. In turn, this implies that the remainder of the Wilsonbreen
110 Formation (including the basal weathering horizon) represents many millions of
111 years, during which $p\text{CO}_2$ built up from the low values necessary for inception of low-
112 latitude glaciation to those indicated by the geochemical evidence. The weathering
113 horizon provides direct evidence of cold, arid conditions during this interval, prior to
114 the appearance of fluvial and glacial lacustrine sediments in the basin.

115 The evidence for ice-sheet advance/retreat cycles at low latitudes in a CO_2 -
116 enriched atmosphere motivated a series of numerical simulations to test the
117 hypothesis that these cycles were linked to Milankovitch orbital variations. We

118 employed asynchronous coupling of a 3D ice sheet model and an Atmospheric
119 General Circulation Model using the continental configuration of (22). We first ran
120 simulations with a modern orbital configuration to examine ice-sheet behaviour
121 through a large range of $p\text{CO}_2$ values from 0.1 to 100 mbar (23; Supplementary
122 Figures 7-10). Consistently with previous results (2, 20), at low $p\text{CO}_2$ (0.1 mbar),
123 global ice volume reaches $170 \times 10^6 \text{ km}^3$ but substantial tropical land areas remain
124 ice free due to sublimation exceeding snowfall (Supplementary Figure S10a). Ice
125 volume remains relatively constant for $p\text{CO}_2 = 0.1$ to 20 mbar (Supplementary Figure
126 S10b), due to an increase in accumulation that compensates for higher ablation rates
127 (Supplementary Figure 13). In contrast, above 20 mbar, ice extent in the eastern
128 Tropics significantly decreases (Supplementary Figure 10c). At $p\text{CO}_2 = 100$ mbar,
129 most of the continental ice cover disappears except for remnants over mountain
130 ranges (Supplementary Figure 10d).

131 To test the sensitivity of the tropical ice sheets to Milankovitch forcing,
132 experiments with changing orbital parameters were initialized using the steady-state
133 ice sheets for $p\text{CO}_2 = 20$ mbar. Although obliquity has been invoked as a possible
134 cause of Neoproterozoic glaciations (24), this mechanism remains problematical and
135 cannot account for significant climatic oscillations at low latitudes (25, 26). We
136 therefore focused on precession as a possible driver, and used two opposite orbital
137 configurations favoring cold and warm summers, respectively, over the northern
138 tropics (CSO: cold summer orbit and WSO: warm summer orbit) (Supplementary
139 Figure 14). Switching between these configurations causes tropical ice-sheets to
140 advance/retreat over several hundred kilometers in 10 kyr (Supplementary Movie 1),
141 with strong asymmetry between hemispheres (Fig. 3). Shifting from WSO to CSO

142 causes ice retreat in the southern hemisphere and ice sheet expansion in the
143 northern hemisphere (Supplementary Figure 14c-d). Significant ice volume changes
144 occur between 30° N and S, but are less apparent in higher latitudes. This reflects
145 higher ablation rates in the warmer low latitudes (Supplementary Figure 14e-h), and
146 higher ice-sheet sensitivity to shifting patterns of melt. Larger greenhouse forcing at
147 the end of the Snowball event implies increasing ice-sheet sensitivity to subtle
148 insolation changes. Given a strong diurnal cycle (23), our simulations also predict a
149 significant number of days above 0°C in the tropics (Supplementary Figure 15),
150 consistent with geological evidence for ice rafting, liquid water in lakes and rivers,
151 and photosynthetic microbial communities.

152 Our results show that geological evidence for glacial-interglacial cycles (5-7) is
153 consistent with an enriched Snowball Earth theory. Termination of the Marinoan
154 panglaciation was not a simple switch from icehouse to greenhouse states but was
155 characterized by a climate transition during which glacial cycles could be forced by
156 Milankovitch orbital variations. The geochemical evidence presented here implies
157 that at least the upper 60-70% of the Wilsonbreen Formation was deposited in $\sim 10^5$
158 years, on the assumption that a trend in $p\text{CO}_2$ would be evident over longer
159 timescales (21). Rates of CO_2 build-up, however, may have slowed in the later stages
160 of Snowball Earth due to silicate weathering of exposed land surfaces, so it is
161 possible that the oscillatory phase was more prolonged.

162 Initiation of low latitude glaciation in the Neoproterozoic requires low $p\text{CO}_2$ (0.1 -
163 1 mbar, 2, 19, 20), implying that the oscillatory phase was preceded by a prolonged
164 colder period ($\sim 10^6$ to 10^7 years) during which $p\text{CO}_2$ gradually increased by volcanic
165 outgassing (21). This timescale is in agreement with recent dates indicating the

166 Marinoan lasted ~15 million years (27). The basal weathering horizon is consistent
167 with a period of low temperatures and limited hydrological cycle prior to the
168 oscillatory phase (2, 19).

169 Additional work is needed to refine the upper and lower limits of $p\text{CO}_2$ conducive
170 to climate and ice-sheet oscillations in Snowball Earth. Factors not included in the
171 present model, such as supraglacial dust or areas of ice-free tropical ocean (28-30),
172 can be expected to make the Earth system more sensitive to orbital forcing. While
173 many details remain to be investigated, our overall conclusions remain robust.

174 The Neoproterozoic Snowball Earth was nuanced, varied and rich. We anticipate
175 that detailed studies of the rock record in other parts of the world, in conjunction
176 with numerical modeling studies, will continue to yield insight into the temporal and
177 regional diversity of this pivotal period in Earth history.

178

179

180 **Methods**

181

182 **Sedimentology.** Lithofacies were classified based on grain size, internal sedimentary
183 structures and deformation structures, and bounding surfaces. Detailed stratigraphic
184 logs were made in the field, supplemented by drawings and photographs of key
185 features. Samples were taken for polishing and thin sectioning, to allow detailed
186 examination of microstructures in the laboratory. In addition, data were collected on
187 clast lithology, shape, surface features and fabric. Diamictites of the Wilsonbreen
188 Formation are commonly very friable, allowing included clasts to be removed intact
189 from the surrounding matrix, allowing measurement of both clast morphology and

190 orientation, using methods developed for unlithified sediments. Clast morphology
191 (shape, roundness and surface texture) was measured for samples of 50 clasts to
192 determine transport pathways. Clast fabric analysis was performed by measuring a-
193 axis orientations of samples of 50 clasts with a compass-clinometer, and data were
194 summarized using the eigenvalue or orientation tensor method. Orientated samples
195 for measurement of Anisotropy of Magnetic Susceptibility (AMS) were collected
196 using a combination of field-drilling and block sampling. AMS was measured using an
197 AGICO KLY-3 Kappabridge operating at 875 Hz with a 300 A/m applied field at the
198 University of Birmingham and an AGICO MFK-1A Kappabridge operating at 976 Hz
199 with a 200 A/m applied field at New Mexico Highlands University.

200

201 **Geochemistry.** Laboratory procedures for extracting, purifying, and measuring the
202 triple oxygen ($\delta^{18}\text{O}$ and $\Delta^{17}\text{O}$) and sulfur ($\delta^{34}\text{S}$) isotope composition of CAS in bulk
203 carbonates are detailed in ref 16. Briefly, fresh carbonate-bearing rock chips were
204 crushed into fine grains and powders using mortar and pestle. Rinsing the fines with
205 18 M Ω water revealed little water-leachable sulphate in all the Wilsonbreen
206 carbonates. Subsequently, ca. 10 to 30 g carbonates were slowly digested in 1-3 M
207 HCl solutions. The solution was then centrifuged, filtered through a 0.2 μm filter, and
208 acidified before saturated BaCl_2 droplets were added. BaSO_4 precipitates were
209 collected after >12 hours and purified using the DDARP method (see Supporting
210 Information). The purified BaSO_4 was then analyzed for three different isotope
211 parameters: 1) $\Delta^{17}\text{O}$, by converting to O_2 using a CO_2 -laser fluorination method; 2)
212 $\delta^{18}\text{O}$, by converting to CO through a Thermal Conversion Elemental Analyzer (TCEA)
213 at 1450 $^\circ\text{C}$; and 3) $\delta^{34}\text{S}$, by converting to SO_2 by combustion in tin capsules in the

214 presence of V₂O₅ through an Elementar Pyrocube elemental analyzer at 1050 °C. The
215 $\Delta^{17}\text{O}$ was run in dual-inlet mode while the $\delta^{18}\text{O}$ and $\delta^{34}\text{S}$ in continuous-flow mode.
216 Both the $\Delta^{17}\text{O}$ and $\delta^{18}\text{O}$ were run on a MAT 253 at Louisiana State University whilst
217 the $\delta^{34}\text{S}$ was determined on an Isoprime 100 continuous flow mass spectrometer at
218 the University of Lancaster, UK. The $\Delta^{17}\text{O}$ was calculated as $\Delta^{17}\text{O} \equiv \delta'^{17}\text{O} - 0.52 \times \delta'^{18}\text{O}$
219 in which $\delta' \equiv 1000 \ln (R_{\text{sample}}/R_{\text{standard}})$ and R is the molar ratio of $^{18}\text{O}/^{16}\text{O}$ or $^{34}\text{S}/^{32}\text{S}$.
220 All δ values are in VSMOW and VCDT for sulphate oxygen and sulfur respectively.
221 The analytical standard deviation (1σ) for replicate analysis associated with the $\Delta^{17}\text{O}$,
222 $\delta^{18}\text{O}$, and $\delta^{34}\text{S}$ are $\pm 0.05\text{‰}$, $\pm 0.5\text{‰}$, and $\pm 0.2\text{‰}$, respectively. Since the CAS is
223 heterogeneous in hand-specimen, the standard deviation is for laboratory
224 procedures. $\delta^{34}\text{S}$ values were corrected against VCDT using within run analyses of
225 international standard NBS-127 (assuming $\delta^{34}\text{S}$ values of +21.1 ‰). Within-run
226 standard replication (1 SD) was $< 0.3 \text{‰}$. All geochemical data are included in
227 Supplementary Table 1.

228

229 **Numerical modeling.** Model runs were conducted with a coupled atmospheric
230 general circulation model (LMDz) and ice-sheet model (GRISLI: GRenoble Ice Shelf
231 and Land Ice model). LMDz (spatial resolution 4° in latitude x 5° in longitude with 38
232 vertical levels) was run with prescribed continental ice to climatic equilibrium. GRISLI
233 has a 40km grid size and is driven with downscaled climatic fields of surface air
234 temperature, precipitation and evaporation. To capture ice sheet – climate
235 feedbacks, LMDz is rerun using the new ice sheet distribution and topography. This
236 procedure was repeated each 10 kyr to investigate orbital forcing.

237

238 Surface mass balance (accumulation minus sublimation and melting) was computed
239 from monthly mean temperature, precipitation and evaporation rate. Melt rate is
240 calculated using the Positive Degree Day method.

241

242 No sea ice dynamics treatment is specified, the sea ice cover is prescribed and a
243 thickness of 10 meters is imposed. Ice albedo is fixed at 0.6, while snow albedo
244 varies from 0.9 from 0.55 as a function of the zenith, and ageing process. Land
245 ice/snow free surface has the characteristic of a bare soil (rocky regolith) with an
246 albedo of 0.3.

247

248 Code availability. Code for the GCM LMDz can be accessed at:
249 <http://lmdz.lmd.jussieu.fr>. Code for the ISM GRISLI (GRenoble Ice Shelf and Land Ice
250 model) is not available.

251

252 Additional details of the methods and modeling procedures are provided in the
253 Supplementary Information in the online version of the paper.

254

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Author contributions

Field data were collected and analyzed by IJF, DIB, EJP, MJH, EAMcM, MSP, PMW and CTES. Geochemical analyses were conducted by HB and PMW. Model experiments were designed and conducted by GLeH, YD, CD and GR. The manuscript and figures were drafted by DIB, IJF and GLeH, with contributions from the other authors.

Competing financial interests

The authors declare no competing financial interests.

Figures:

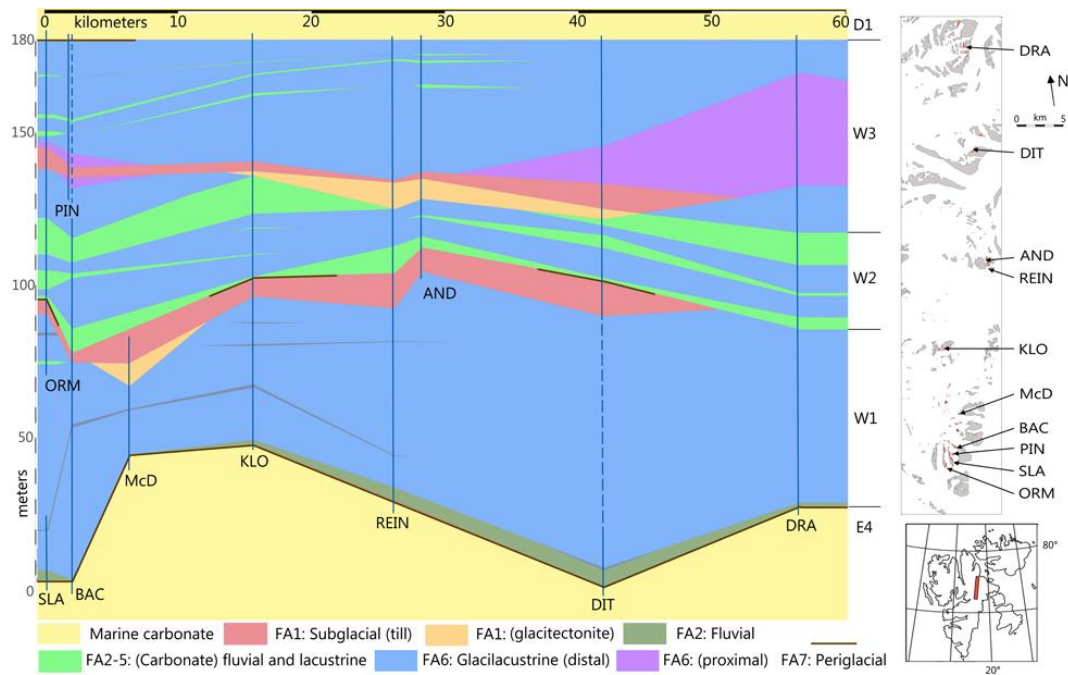


Figure 1: Sedimentary architecture and palaeoenvironments of the Wilsonbreen

Formation. Regional correlation of facies associations and members W1, W2 and W3

across NE Svalbard. From north to south, study locations are: DRA: Dracoisen; DIT:

Ditlovtoppen; AND: East Andromedafjellet; REIN: Reinsryggen (informal name); KLO:

Klofjellet; McD: MacDonaldryggen; BAC: Backlundtoppen - Kvitfjellet ridge; PIN:

Pinnsvinryggen (informal name); SLA: Slangen and ORM: Ormen.

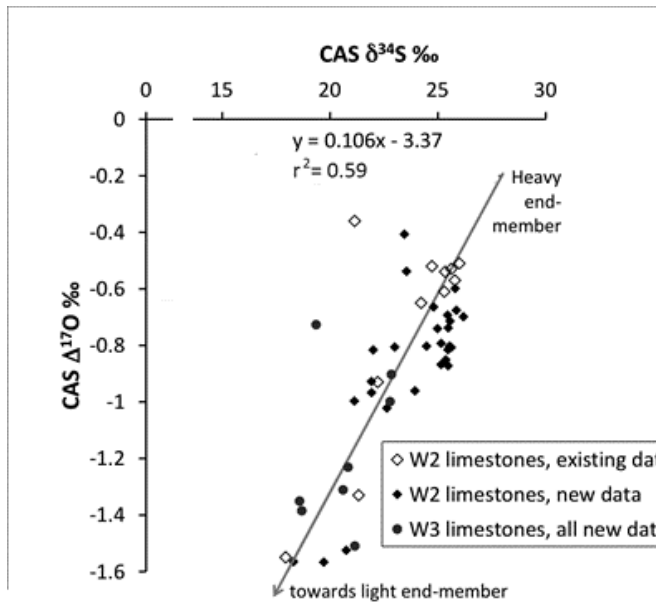


Figure 2: Co-variation of $\Delta^{17}\text{O}$ and $\delta^{34}\text{S}$ from carbonate-associated sulphate in W2 and W3. Existing data (ref. 16) and new data define a mixing line between pre-glacial sulphate (top) and an isotopically light sulphate formed by oxidation of pyrite including incorporation of a light- $\Delta^{17}\text{O}$ signature from a CO_2 -enriched atmosphere. Data from W2 and W3 lie on closely similar trend lines, indicating no detectable change in pCO_2 between deposition of the two members.

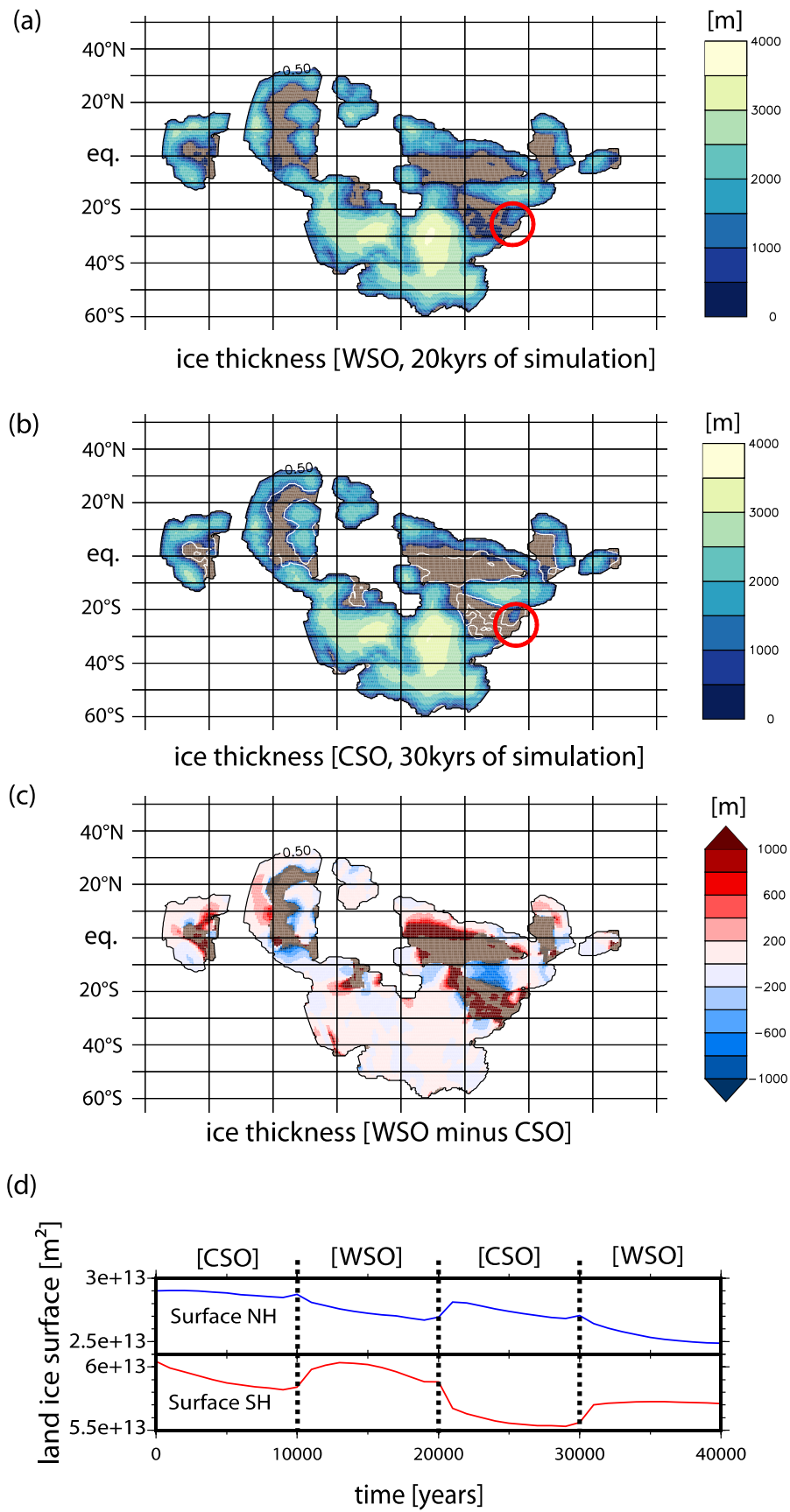


Figure 3: Modelled ice sheet oscillations in response to orbital forcing. (a), (b) Land

ice thickness obtained with 20 mbar of carbon dioxide in response to changes of orbital forcing (WSO and CSO, warm/cold summer orbit for the northern hemisphere) over the course of two precession cycles (40 ky of simulation).

Continental areas without ice are light brown, the white line is used to represent the old ice-sheet extension (WSO case). The Svalbard area is indicated by a red circle. (c)

ice thickness variation in 10 ky (WSO case after 20 ky minus CSO case after 30 ky of simulation) (d) area covered by ice (m^2) in each hemisphere through time ([WSO] and [CSO] indicate which orbital configuration is used).