# Advances and Geographysics

# The incidence of bar-like kinematic flows in CALIFA galaxies

L. Holmes, <sup>1</sup> \* K. Spekkens, <sup>1</sup> S. F. Sánchez, <sup>2</sup> C. J. Walcher, <sup>3</sup> R. García-Benito, <sup>4</sup> D. Mast, <sup>5</sup> C. Cortijo-Ferrero, <sup>4</sup> V. Kalinova, <sup>6</sup> R. A. Marino, <sup>7</sup> J. Mendez-Abreu <sup>8</sup> and J. K. Barrera-Ballesteros <sup>9,10</sup>

Universidad Complutense de Madrid, Avda. Complutense s/n, E-28040 Madrid, Spain

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#### **ABSTRACT**

We carry out a direct search for bar-like non-circular flows in intermediate-inclination, gasrich disc galaxies with a range of morphological types and photometric bar classifications from the first data release (DR1) of the Calar Alto Legacy Integral Field Spectroscopy Area (CALIFA) survey. We use the DISKFIT algorithm to apply rotation only and bisymmetric flow models to H  $\alpha$  velocity fields for 49/100 CALIFA DR1 systems that meet our selection criteria. We find satisfactory fits for a final sample of 37 systems. DISKFIT is sensitive to the radial or tangential components of a bar-like flow with amplitudes greater than  $15\,\mathrm{km}\,\mathrm{s}^{-1}$  across at least two independent radial bins in the fit, or ~2.25 kpc at the characteristic final sample distance of  $\sim$ 75 Mpc. The velocity fields of 25/37 (67.6 $^{+6.6}_{-8.5}$  per cent) galaxies are best characterized by pure rotation, although only 17/25 (68.0 $_{-10.4}^{+7.7}$  per cent) of them have sufficient H  $\alpha$  emission near the galaxy centre to afford a search for non-circular flows. We detect non-circular flows in the remaining 12/37 ( $32.4^{+8.5}_{-6.6}$  per cent) galaxies. We conclude that the non-circular flows detected in 11/12 (91.7<sup>+2.8</sup><sub>-14.9</sub> per cent) systems stem from bars. Galaxies with intermediate (AB) bars are largely undetected, and our detection thresholds therefore represent upper limits to the amplitude of the non-circular flows therein. We find 2/23 (8.7 $^{+9.6}_{-2.9}$  per cent) galaxies that show non-circular motions consistent with a bar-like flow, yet no photometric bar is evident. This suggests that in  $\sim$ 10 per cent of galaxies either the existence of a bar may be missed completely in photometry or other processes may drive bar-like flows and thus secular galaxy evolution.

**Key words:** surveys – galaxies: kinematics and dynamics – galaxies: spiral – galaxies: structure.

#### 1 INTRODUCTION

Current estimates indicate that 30 per cent of nearby spiral galaxies are strongly barred in optical light, a number which rises to  $\sim$ 50 per cent if weak bars are included (Sellwood & Wilkinson

1993; Barazza, Jogee & Marinova 2008; Aguerri, Mendez-Abreu & Corsini 2009; Masters et al. 2011). Bars are even more prominent in NIR images where the measured bar fraction is more than ~70 per cent (Mulchaey & Regan 1997; Eskridge et al. 2000; Whyte et al. 2002; Sheth et al. 2011). The increase in bar fraction at NIR wavelengths has been attributed to a higher prevalence of weak (AB) bars, which are obscured by dust and star-forming regions in the optical (Athanassoula 1992; Marinova et al. 2009a).

<sup>&</sup>lt;sup>1</sup>Department of Physics, Royal Military College of Canada, PO Box 17000, Station Forces, Kingston, ON K7K 7B4, Canada

<sup>&</sup>lt;sup>2</sup>Instituto de Astronomía, Universidad Nacional Autonóma de Mexico, A.P. 70-264, 04510 México, D.F., Mexico

<sup>&</sup>lt;sup>3</sup>Leibniz-Institut fűr Astrophysik Potsdam (AIP), An der Sternwarte 16, D-14482 Potsdam, Germany

<sup>&</sup>lt;sup>4</sup>Instituto de Astrofísica de Andalucía (IAA/CSIC), Glorieta de la Astronomía s/n Aptdo. 3004, E-18080 Granada, Spain

<sup>&</sup>lt;sup>5</sup>Instituto de Cosmologia, Relatividade e Astrofísica ICRA, Centro Brasileiro de Pesquisas Físicas, Rua Dr. Xavier Sigaud 150, CEP 22290-180, Rio de Janeiro, RJ, Brazil

<sup>&</sup>lt;sup>6</sup>Department of Physics 4-181 CCIS, University of Alberta, Edmonton, AB T6G 2E1, Canada

<sup>&</sup>lt;sup>7</sup>CEI Campus Moncloa, UCM-UPM, Departamento de Astrofísica y CC. de la Atmósfera, Facultad de CC. Físicas,

<sup>&</sup>lt;sup>8</sup>School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews, Fife KY16 9SS, UK

<sup>&</sup>lt;sup>9</sup>Instituto de Astrofísica de Canarias, Calle Vía Lactéa s/n, E-38205 La Laguna, Tenerife, Spain

<sup>&</sup>lt;sup>10</sup>Departamento de Astrofísica, Universidad de La Laguna (ULL), E-38200 La Laguna, Tenerife, Spain

<sup>\*</sup> E-mail: lindsay.holmes@rmc.ca

Bars are therefore an essential structural component whose properties drive secular evolution (e.g. Kormendy & Kennicutt 2004, and references therein). The presence of a bar within a galaxy allows for the redistribution of both the material and angular momentum within it (Athanassoula, Machado & Rodionov 2013). Bars have a significant influence on gas flow (Weinberg & Katz 2002), they are thought to be an efficient mechanism for moving gas to central regions (Shlosman, Frank & Begelman 1989; Shlosman, Begelman & Frank 1990) adding mass to the bulge or creating secondary bars (Friedli & Martinet 1993). The incidence of barred galaxies is therefore important in understanding the secular processes that affect the basic structure of a galaxy and slowly change it over time (Kormendy & Bender 2012).

Information on the morphological, photometric and kinematic properties of bars has been obtained from many observational studies ranging from single objects to large surveys (e.g. Sheth et al. 2005; Aguerri et al. 2009; Aguerri et al. 2015; Marinova et al. 2009b; Simard et al. 2011). Because of the relative ease of obtaining images for large samples of nearby galaxies, most observational studies of bars have focused on their photometric properties. While photometric studies of bars provide important insight into the role that bars play in galaxy evolution, the relationship between the properties derived from the light associated with bars and the dynamical impact that these bars have on their host systems is not well understood. In addition, bars in different dynamical states – young, flat bars and older bars that have buckled out of the disc, for example – exhibit only subtle differences in their photometric properties (e.g. Erwin & Debattista 2013; Laurikainen et al. 2014; Mendez-Abreu et al. 2014).

A more direct measure of the dynamical importance of a bar in a disc galaxy is to measure the associated gas flows. However, studies of the kinematics of bar-like flows have been performed (e.g. Weiner, Sellwood & Williams 2001; Hernandez et al. 2005; Spekkens & Sellwood 2007; Sellwood & Sánchez 2010), and no thorough observational investigation of the correspondence between the photometric properties of a bar and their kinematic signatures exists.

The publicly released DISKFIT¹ software is specifically designed to fit for bisymmetric distortions in disc galaxy gas velocity fields. DISKFIT fits non-parametric models to images or to velocity fields as originally described by Reese et al. (2007) for images, and Spekkens & Sellwood (2007) and Sellwood & Sánchez (2010) for velocity fields. DISKFIT can fit both axisymmetric and non-axisymmetric models of disc galaxies, it can also account for symmetric outer velocity warps, and can correct for minor distortions due to seeing. Unlike other methods, DISKFIT fits a specific physically motivated model rather than parametrizing concentric rings of the velocity field (see Spekkens & Sellwood 2007; Sellwood & Sánchez 2010; Kuzio de Naray et al. 2012). DISKFIT also returns realistic estimates of the uncertainties on the best-fitting parameters using bootstrap realizations of the best-fitting model. DISKFIT is therefore ideally suited for direct searches for bar-like flows in nearby galaxies.

Large resolved spectroscopic surveys have provided a method for statistically sampling the galaxy population, allowing for a greater understanding of their formation and evolution. The large number of objects that are studied allows for a meaningful statistical analysis over a wide range of galaxy types and environmental conditions. This has led recently to the advent of several large kinematic studies using Integral Field Units (IFUs). Early IFU surveys typically

targeted ~10–100 nearby galaxies, and include SAURON (de Zeeuw et al. 2002), VENGA (Blanc et al. 2013), PINGS (Rosales-Ortega et al. 2010) and ATLAS3D (Cappellari et al. 2011). Upcoming large surveys include MaNGA (Bundy et al. 2015) as well as the ongoing SAMI (Croom et al. 2012; Bryant et al. 2015) and Calar Alto Legacy Integral Field Spectroscopy Area (CALIFA) surveys (Sánchez et al. 2012).

The CALIFA survey utilizes the PPaK mode of the Potsdam MultiAperture Spectrophotometer (PMAS) IFU on the 3.5 m telescope at the Calar Alto observatory (Roth et al. 2005; Kelz et al. 2006) and will produce spatially resolved spectral information for nearly 600 galaxies. The CALIFA mother sample consists of 939 possible target galaxies and was selected from the Sloan Digital Sky Survey (SDSS) data release 7 (DR7) photometric catalogue (Abazajian et al. 2009). Targets are drawn according to visibility from this mother sample. The fully calibrated, first data release (DR1) DR1 of 100 CALIFA targets occurred on 2012 November 1 and is the source of the data used in this paper.

Although CALIFA will produce a much smaller sample than either MaNGA or SAMI, the number of resolution elements that covers each target galaxy is much greater. The CALIFA survey is therefore unique in its combination of resolution and sample size when compared both to past (e.g. PINGS, VENGA) and future (e.g. SAMI, MaNGA) spectroscopic surveys. This resolution is particularly useful in searching for non-circular flows, where several resolution elements across both the major and minor axes are required.

Several studies of the kinematic properties of barred galaxies have now been carried out by the CALIFA collaboration. The ionized gas kinematics for a large sample of CALIFA galaxies with a wide range of morphological types were examined by Kehrig et al. (2012) and García-Lorenzo et al. (2014). The pattern speeds of barred CALIFA galaxies were examined by Aguerri et al. (2015), and the kinematic alignment of barred and unbarred systems were compared by Barrera-Ballesteros et al. (2014). However, no attempt to separate non-circular flows from the underlying disc rotation has yet been made.

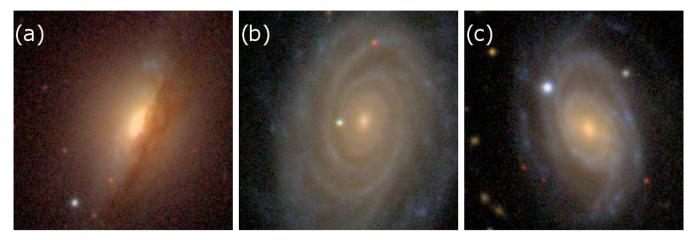
This paper carries out the first direct search for non-circular motions in the H  $\alpha$  velocity fields of an intermediate-inclination subsample of CALIFA DR1 galaxies using DISKFIT. The kinematic bar search performed in this paper provides a direct probe of the dynamical impact of the bar on the disc – and thus insight on its role in driving galaxy evolution. In addition, a systematic comparison between kinematic and photometric bar classifications is carried out, affording both a preliminary look at the relationship between these two schemes as well as a search for systems where the photometric classification belies a different kinematic structure. This paper therefore provides a first look at the relationship between photometric and kinematic indicators of bar-like flows in disc galaxies.

## 2 SAMPLE SELECTION

We attempt to model all intermediate-inclination gas-rich CALIFA DR1 galaxies. As described in Husemann et al. (2013) and Walcher et al. (2014), DR1 is a statistically representative subset of the full CALIFA sample in stellar mass, colour and morphology.

The morphological classification and barredness of all CALIFA galaxies were determined by-eye by five members of the collaboration (Walcher et al. 2014). In the sample of 100 CALIFA DR1 galaxies, 30 per cent are classified as barred (B), 21 per cent as intermediately barred (AB) and 49 per cent as unbarred (A). These values are consistent with the optical bar fractions in nearby

<sup>&</sup>lt;sup>1</sup> http://www.physics.rutgers.edu/~spekkens/diskfit/



**Figure 1.** SDSS 2 arcmin × 2 arcmin *igr* composite images of galaxies in the CALIFA mother sample illustrating the different bar classifications. (a) A: NGC 1056. (b) AB: NGC 4185. (c) B: NGC 7321.

galaxies discussed in Section 1. Fig. 1 shows SDSS 2 arcmin  $\times$  2 arcmin igr composite images of galaxies in the CALIFA mother sample illustrating the different bar classifications. We adopt these morphological and bar classifications for our analysis. The photometric inclinations,  $i_p$ , for each galaxy were computed from ellipses enclosing 50–90 per cent of the total galaxy flux in its r-band SDSS image. We attempt to model only those DR1 galaxies with  $40^{\circ} < i_p < 75^{\circ}$ . At lower inclinations, the line-of-sight component of the rotation velocity becomes harder to disentangle from the turbulent motions in the disc, and the inclination is correspondingly harder to constrain (e.g. Bershady et al. 2010). It is possible to measure rotation curves at higher inclinations, but searching for non-circular flows becomes difficult because there is limited minor axis information. 57/100 of the CALIFA DR1 galaxies meet this photometric inclination selection criterion.

The H  $\alpha$  velocity fields of these 57 galaxies were examined to determine their suitability for modelling. The H  $\alpha$  emission line maps were extracted from the gas-pure cubes by fitting a single Gaussian function using the systemic velocity from the analysis of the stellar population as an initial guess using FIT3D (Sánchez 2006). The uncertainties in the velocity and velocity dispersion were determined from the inverse of the covariance map. The velocity fields used could be affected by the presence of dust by both hindering the detection of the emission lines as well as potentially perturbing the velocity distribution (Regan, Sheth & Vogel 1999). The obscuration of H  $\alpha$  emission could affect our search, if there is a significant lack of H  $\alpha$  along the major or minor axis of the galaxy, a search for noncircular flows would not be possible (see Section 4.1). Typically, the presence of strong dust lanes is associated with spiral arms or the rotational front of bars (Athanassoula 1992) and is unlikely to produce or mimic the coherent motion for which we are searching, and therefore would not significantly impact our results.

We apply spatial masks created from SDSS r-band masks reprojected to the scale, orientation and pixel size of the CALIFA cubes with foreground stars and artefacts removed. All those galaxies where less than 5 per cent of the pixels contained H  $\alpha$  were eliminated from the sample, and we attempted to model galaxies where 5–10 per cent of them contained H  $\alpha$  only if a velocity gradient was discernible in the velocity field. This criterion eliminated nearly all remaining elliptical galaxies, resulting in a sample of 49/100 CALIFA DR1 galaxies. We attempted to model each of these 49 galaxies.

The basic properties of these 49 galaxies are given in Table 1, and Fig. 2 shows their distribution of morphological types and bar classification. In Fig. 2, the dotted histogram shows the distribution of all 100 CALIFA DR1 galaxies and the blue histogram shows the 49 galaxies that we attempted to model. The modelled galaxies span a range of morphological types as well as barredness, in similar proportions to the full DR1 sample. The red histograms in Fig. 2 show the galaxies for which valid kinematic models were obtained; we describe our process for selecting valid models in Section 4.1.

# 3 KINEMATIC MODELS

We use the publicly available DISKFIT code to carry out all of our kinematic modelling. DISKFIT returns the galaxy centre, kinematic inclination  $(i_k)$ , systemic velocity  $(V_{\rm sys})$ , and position angle (PA) of the kinematic major axis. We consider three types of kinematic models within DISKFIT. The simplest model includes rotation only, and is given by

$$V_{\text{model}}(R) = V_{\text{sys}} + \bar{V}_{\text{t}}(R)\sin i_{k}\cos\theta, \tag{1}$$

where  $V_{\rm sys}$  is the systemic velocity,  $\bar{V}_{\rm t}$  is the rotation velocity,  $i_{\rm k}$  is the kinematic disk inclination, and  $\theta$  is the azimuthal angle from the major axis in the plane of the disk. Note that diskfit assumes that the disk is flat, and returns a single value for the PA, inclination, systemic velocity, and disk centre.

The bisymmetric model introduces non-circular flows produced by a bar-like, m=2 perturbation to the potential and is given by

$$V_{\text{model}}(R) = V_{\text{sys}} + \sin i_k \left[ \bar{V}_{\text{t}}(R) \cos \theta - V_{2,\text{t}}(R) \cos (2\theta_b) \cos \theta - V_{2,\text{r}}(R) \sin (2\theta_b) \sin \theta \right], \tag{2}$$

where  $V_{2,t}$  and  $V_{2,r}$  are the tangential and radial components of the non-circular flow, respectively, and the major axis of the bar is at an angle  $\theta_b$  to the projected major axis in the plane of the disk. Equation (2) describes first-order gas flows in a barred galaxy. Although higher order harmonic components are required to fully describe the kinematics of strongly barred galaxies, the m=2 component always dominates and is generally sufficient to model the physical properties of the flow.

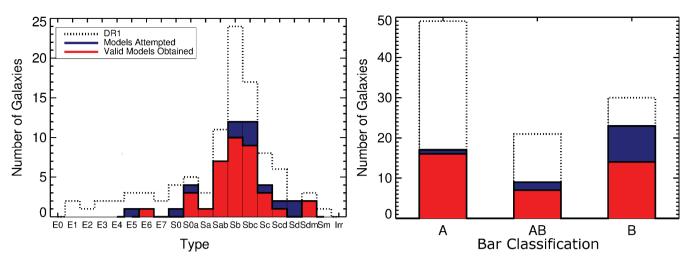
After an initial search for bar-like flows across the entire disk extent in all galaxies, an outer search radius ( $R_{\rm max}$ ) was imposed, beyond which all non-circular flows are forced to zero. For all

Table 1. Literature values for 49/100 CALIFA DR1 galaxies that were modelled with DISKFIT.

NGC 7819   Sc					α	δ	$i_{\mathrm{p}}$	$\phi_{ m p}'$	V <sub>sys</sub>		
3 NGC 7819 Sc A 00:04:24.5 31:28:19.2 59 65 49:58 ± 6 1,1 Y 7 UGC36 Sab AB 00:05:13.9 06:46:19.3 53 20 6291 ± 13 1,2 Y 14 UGC312 Sd B 00:11:22.3 06:23:21.7 49 170 60:30 ± 4 1,3 Y 14 UGC312 Sd B 00:12:23.9 08:28:00.2 72 5 43:64 ± 3 1,2 N (DF) 42 NGC 477 Sbc AB 01:21:20.5 40:29:17.3 49 120 58:76 ± 8 1,3 Y 43 IC1683 Sb AB 01:22:28.9 34:26:13.7 54 160 48:69 ± 20 1,21 N (DF) 73 NGC 776 Sb B 01:59:54.5 23:38:39.4 46 135 4921 ± 6 1,4 N (I) 100 NGC 10:56 Sa A 02:42:48.3 28:34:27.0 56 15:5 15:45 ± 10 1,4 Y 160 UGC3253 Sb B 01:59:41.9 84:03:00.4 51 65 413:0 ± 7 1,4 Y 156 NGC 2449 Sab AB 07:47:20.3 26:55:48.7 61 138 4892 ± 3 5,6 Y 177 NGC 2916 Sbc A 09:34:57.6 21:24:18.9 54 18 37:30 ± 7 5,4 Y 306 UGC3538 Sd B 09:58:47.1 11:23:19.3 74 75 2914 ± 1 5,7 N (DF) 307 UGC3559 Sb B 09:58:51.6 19:12:53.9 70 94 8472 ± 9 5,8 Y 479 NGC 4003 S0a B 11:57:59.0 23:07:29.6 67 167 65:09 ± 32 5,4 N (DD) 480 UGC771 B6 A 10:37:19.3 43:35:15.3 45 52 74:03 ± 52 5,9 Y 1515 NGC 4185 Sbc AB 12:15:12.8 05:52.7 78 10 3081 ± 1 1,10 Y 2518 NGC 4210 Sb B 12:15:15.8 65:59.07.2 43 100 2732 ± 7 5,3 Y 2528 IC776 Sdm A 12:19:03.1 08:51:22.2 56 98 2468 ± 1 4,12 Y 2548 NGC 4470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2548 NGC 470 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2549 NGC 40:40 Sc A 12:29:37.8 07:49:27.1 49 1 23:41 ± 1 5,12 Y 2540 NGC 50:40 Sc A 14:41:32.0 44:30:40 51	ID	Name	Morph	Bar	(hh:mm:ss.s)	(dd:mm:ss.s)	(deg)	(deg)	$(\text{km s}^{-1})$	Ref.	Mod.
7         UGC36         Sab         AB         0005:139         06:46:193         53         20         6291 ± 13         1,2         Y           14         UGC312         Sd         B         00:11:223         06:23:21.7         49         170         6030 ± 4         1,3         Y           42         NGC 477         Sbc         AB         01:21:20.5         40:29:17.3         49         120         5876 ± 8         1,2         N (DF)           73         NGC 776         Sb         AB         01:22:389         34:26:13.7         54         160         4869 ± 20         1,21         N (DF)           73         NGC 776         Sb         B         01:59:54.5         23:38:39.4         46         135         4921 ± 6         1,4         N (DF)           100         NGC 196.6         Sa         A         02:24:248.3         28:34:27.0         56         13:30 ± 7         1,4         Y           156         NGC 2449         Sab         AB         07:47:20.3         26:55:48.7         61         138         4892 ± 3         5,4         Y           307         UGC3538         Sd         B         09:58:47.1         11:23:19.3         74 <t></t>	(1)	(2)	(3)	(4)	(3)	(0)	(7)	(6)	(9)	(10)	(11)
10	3	NGC 7819	Sc	A	00:04:24.5	31:28:19.2	59	65		1, 1	Y
14         UGC312         Sd         B         0031239         08.2800.2         72         5         4364 ± 3         1, 2         N (DF)           42         NGC 477         Sb         AB         011220.5         4029:17.3         49         120         5876 ± 8         1, 2         N (DF)           73         NGC 776         Sb         B         01:59:54.5         23:38:39.4         46         135         4921 ± 6         1, 4         N (D)           100         NGC 1056         Sa         A         02:42:48.3         23:38:39.4         46         135         4921 ± 6         1, 4         N (D)           160         NGC 2916         Sb         AB         07:47:20.3         26:55:48.7         61         138         4892 ± 3         5, 6         Y           360         UGC5358         Sd         B         09:58:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           341         UGC5359         Sb         B         09:58:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           341         UGC5359         Sb         B         09:58:47.1         11:23:19.3	7	UGC36	Sab	AB	00:05:13.9	06:46:19.3		20			Y
42         NGC 477         Sbc         AB         01:21:20:5         40:29:17.3         49         120         5876 ± 8         1, 3         Y           43         IC1683         Sb         AB         01:22:38.9         34:26:13.7         54         160         4869 ± 20         1, 21         N (DF)           73         NGC 776         Sb         B         01:95:94.5         23:38:39.4         46         135         4921 ± 6         1, 4         N (DF)           146         UGC3253         Sb         B         05:19:41.9         84:03:09.4         51         65         155         1545 ± 10         1, 4         Y           146         UGC323         Sb         AB         07:47:20.3         26:55:48.7         61         138         4892 ± 3         5, 6         Y           177         NGC 2916         Sbc         A         09:34:57.6         21:42:18.9         54         18         373.0 ± 7         5, 8         Y           306         UGC5359         Sb         B         09:58:51.6         19:12:53.9         70         94         8472 ± 9         5, 8         Y           341         UGC5379         Sb         B         09:58:51.6	10			В	00:11:22.3						
43         IC1683         Sb         AB         01:22:38.9         34:26:13.7         54         160         4869 ± 20         1, 21         N (DF)           100         NGC 1056         Sb         B         01:59:54.5         23:38:39.4         46         135         49:21 ± 6         1, 4         Y           146         UGC3253         Sb         B         05:19:41.9         84:03:09.4         51         65         4130 ± 7         1, 4         Y           277         NGC 2916         Sbc         A         09:34:57.6         21:42:18.9         54         18         3730 ± 7         5, 4         Y           306         UGC5358         Sd         B         09:58:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           307         UGC5359         Sb         B         09:58:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           341         UGC5379         E6         A         10:37:19.3         43:35:15.3         45         52         7403 ± 52         5, 9         Y           449         NGC 4003         Soa         B         11:57:59.0         23:07:29.6				В	00:31:23.9	08:28:00.2					N (DF)
73 NGC 776 Sb B 0 1:59:54.5 23:38:39.4 46 135 4921 ± 6 1, 4 N (I) 100 NGC 1056 Sa A 0:242:48.3 28:34:27.0 56 155 154:5 ± 10 1, 4 Y 1160 NGC 1056 Sa A 0:242:48.3 28:34:27.0 56 155 154:5 ± 10 1, 4 Y 156 NGC 2449 Sab AB 0 7:47:20.3 26:55:48.7 61 138 4892 ± 3 5, 6 Y 156 NGC 2449 Sab AB 0 07:47:20.3 26:55:48.7 61 138 4892 ± 3 5, 6 Y 1360 UGC5358 Sd B 09:58:47.1 11:23:19.3 74 75 2914 ± 1 5, 7 N (DF) 1370 UGC5359 Sb B 0 99:58:51.6 19:12:53.9 70 94 8472 ± 9 5, 8 Y 1371 UGC5359 Sb B 0 99:58:51.6 19:12:53.9 70 94 8472 ± 9 5, 8 Y 1371 UGC5359 Sb B 1 1:57:59.0 23:07:29.6 67 167 6509 ± 32 5, 4 N (DD) 1381 UGC5711 E6 A 10:37:19.3 43:35:15.3 45 52 7403 ± 52 5, 9 Y 1381 UGC5712 Scd AB 12:02:03.1 29:50:52.7 58 10 3081 ± 1 1, 10 Y 1381 NGC 4210 Sb B 12:13:22.2 28:30:39.5 50 164 3904 ± 5 5, 11 Y 1518 NGC 4210 Sb B 12:15:15.8 65:59:07.2 43 100 2732 ± 7 5, 3 Y 1528 UGC5333 Sdm A 12:19:03.1 08:51:22.2 56 98 2468 ± 1 4, 12 Y 1584 NGC 4470 Sc A 12:29:37.8 07:49:27.1 49 1 2341 ± 1 5, 12 Y 1585 UGC8731 Sb B 13:56:51.0 37:49:27.1 49 1 2341 ± 1 5, 12 Y 1586 NGC 5000 Sbc B 13:50:22.7 21:32:21.7 59 175 7592 ± 15 1, 13 Y 1586 NGC 5378 Sb B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5, 6 N (DF) 1786 NGC 5378 Sb B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5, 6 N (DF) 1787 UGC8731 Sbc B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5, 16 N (DF) 1788 NGC 6061 Sbc A 14:34:32.0 44:30:46.0 51 132 32.8 ± 6 1, 4 Y 1880 NGC 5000 Sbc B 13:356:51.0 37:47:50.1 51 78 3042 ± 25 5, 14 Y 1880 NGC 5394 Sbc B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5, 6 N (DF) 1880 NGC 5000 Sbc B 13:356:51.0 37:47:50.1 51 78 3042 ± 25 5, 14 Y 1881 NGC 5720 Sbc B 14:38:33.3 50:48:54.9 49 52 7700 ± 6 5, 9 Y 1882 NGC 6061 Sbc A 16:07:13.0 07:58:44.4 53 155 2848 ± 5 5, 15 Y 1882 NGC 6061 Sbc A 16:07:13.0 07:58:44.4 53 155 2848 ± 5 5, 15 Y 1883 NGC 6154 Sab B 16:10:34.3 10:02:25.3 67 159 4731 ± 44 5, 9 Y 1886 NGC 6061 Sbc A 16:12:56.9 09:52:01.6 64 129 5176 ± 31 5, 9 Y 1886 NGC 6061 Sbc A 16:12:56.9 09:52:01.6 64 129 5176 ± 31 5, 9 Y 1887 NGC 6314 Sab A 17:13:36.7 36:06.02 80 211.5 54 90 4730 ± 10 1, 4 Y	42			AB	01:21:20.5	40:29:17.3	49	120		1, 3	
100   NGC 1056   Sa	43	IC1683	Sb	AB			54	160	$4869 \pm 20$	1, 21	N (DF)
146	73		Sb	В		23:38:39.4	46	135			
156         NGC 2419         Sab         AB         07:47:20.3         26:55:48.7         61         138         4892 ± 3         5, 6         Y           277         NGC 2916         Sbc         A         09:34:57.6         21:42:18.9         54         18         3730 ± 7         5, 4         Y           306         UGC5358         Sd         B         09:38:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           307         UGC5359         Sb         B         09:58:47.1         11:23:19.3         70         94         8472 ± 9         5, 8         Y           341         UGC5771         E6         A         10:37:19.3         43:35:15.3         45         52         7403 ± 52         5, 9         Y           479         NGC 4003         Soa         B         11:57:59.0         23:07:29.6         67         167         6509 ± 32         5, 4         N (DD)           486         UGC7012         Sed         AB         12:13:22.2         28:30:39.5         50         164         3904 ± 5         5, 11         Y           518         NGC 4210         Sb         B         12:15:15.8         65:59:90.7	100		Sa	Α	02:42:48.3	28:34:27.0	56	155	$1545 \pm 10$	1, 4	Y
277         NGC 2916         Sbc         A         09:34:57.6         21:42:18.9         54         18         3730 ± 7         5, 4         Y           306         UGC5358         Sd         B         09:58:51.6         19:12:3:19.3         74         75         2914 ± 1         5, 7         N (DF)           341         UGC5771         E6         A         10:37:19.3         43:35:15.3         45         52         7403 ± 52         5, 9         Y           479         NGC 4003         S0a         B         11:57:59.0         23:07:29.6         67         167         6509 ± 32         5, 4         N (DD)           486         UGC7012         Sed         AB         12:02:03.1         29:50:52.7         58         10         3081 ± 1         1, 10         Y           515         NGC 4185         Sbc         AB         12:13:22.2         28:30:39.5         50         164         3904 ± 5         5, 11         Y           518         NGC 4210         Sb         B         12:13:22.2         28:30:39.5         50         164         3904 ± 5         5, 11         Y           548         NGC 4210         Sb         B         12:13:22.2         28:30:39.5	146	UGC3253	Sb	В	05:19:41.9	84:03:09.4	51	65	$4130 \pm 7$	1, 4	
306         UGC5358         Sd         B         09:58:47.1         11:23:19.3         74         75         2914 ± 1         5, 7         N (DF)           307         UGC53589         Sb         B         09:58:51.6         19:12:53.9         70         94         8472 ± 9         5, 8         Y           479         NGC 4003         S0a         B         11:57:59.0         23:07:29.6         67         167         6509 ± 32         5, 4         N (DD)           486         UGC7012         Scd         AB         12:02:03.1         29:50:52.7         58         10         3081 ± 1         1, 10         Y           515         NGC 4185         Sb         AB         12:13:22.2         28:30:39.5         50         164         3094 ± 5         5, 11         Y           518         NGC 4210         Sb         B         12:13:22.2         28:30:39.5         50         164         3094 ± 5         5, 11         Y           528         IC76         Sdm         A         12:19:19.31         08:51:22.2         56         98         2468 ± 1         4, 12         Y           668         UGC8733         Sdm         B         13:09:47.5         28:54:25.0	156	NGC 2449	Sab	AB	07:47:20.3	26:55:48.7	61	138	$4892 \pm 3$	5, 6	Y
307 UGC5359 Sb B 09:58:51.6 19:12:53.9 70 94 8472 ± 9 5,8 Y   341 UGC5771 E6 A 10:37:19.3 45:35:15.3 45 52 7403 ± 52 5,9 Y   7479 NGC 4003 Soa B 11:57:59.0 23:07:29.6 67 167 6509 ± 32 5,4 N (DD)  486 UGC7012 Scd AB 12:02:03.1 29:50:52.7 58 10 3081 ± 1 1,10 Y   515 NGC 4185 Sbc AB 12:13:22.2 28:30:39.5 50 164 3904 ± 5 5,11 Y   518 NGC 4210 Sb B 12:15:15.8 65:59:07.2 43 100 27:32 ± 7 5,3 Y   528 IC776 Sdm A 12:19:03.1 08:51:22.2 56 98 2468 ± 1 4,12 Y   548 NGC 4470 Sc A 12:29:37.8 07:49:27.1 49 1 2341 ± 1 5,12 Y   548 NGC 6470 Sc A 12:29:37.8 07:49:27.1 49 1 2341 ± 1 5,12 Y   665 UGC8731 Sb B 13:59:22.7 21:32:21.7 59 175 7592 ± 15 1,13 Y   665 UGC8781 Sb B 13:55:22.2 7 21:32:21.7 59 175 7592 ± 15 1,13 Y   666 NGC 5378 Sb B 13:55:51.0 37:47:50.1 51 78 3042 ± 25 5,14 Y   676 NGC 5378 Sb B 13:56:51.0 37:47:50.1 51 78 3042 ± 25 5,14 Y   676 NGC 5378 Sbc B 14:38:33.3 50:48:54.9 49 52 7790 ± 6 5,9 Y   676 UGC9476 Sbc A 14:41:32.0 44:30:46.0 51 132 3262 ± 8 5,3 Y   823 NGC 6063 Sbc A 16:10:34.3 10:02:25.3 67 159 4731 ± 44 5,9 Y   824 IC1199 Sb AB 16:10:34.3 10:02:25.3 67 159 4731 ± 44 5,9 Y   825 NGC 6063 Sbc A 16:12:56.9 09:52:01.6 64 129 5176 ± 31 5,9 Y   826 NGC 6341 Sab B 17:16:47.7 61:55:12.4 62 62 3079 ± 11 5,5 N   677 NGC 641 Sab B 17:18:43.7 58:08:06.4 67 92 8746 ± 26 5,17 Y   826 NGC 6341 Sab B 17:18:43.7 58:08:06.4 67 92 8746 ± 26 5,17 Y   827 NGC 102128 S0 B 18:24:46.3 41:29:33.8 56 165 5771 ± 23 1,23 N   827 NGC 6405 Sbc A 17:10:34.7 58:08:06.4 67 92 8746 ± 26 5,17 Y   828 NGC 6407 Sab A 17:12:38.7 23:16:12.3 60 174 6633 ± 4 5,16 Y   828 NGC 6407 Sab B 17:38:46.3 41:29:33.8 56 165 5771 ± 23 1,23 N   829 NGC 6407 Sab A 17:12:38.7 23:16:12.3 60 174 6633 ± 4 5,16 Y   836 NGC 6497 Sab B 17:38:46.3 41:29:33.8 56 165 5771 ± 23 1,23 N   847 NGC 7025 S0a A 17:34:06.4 59:20:33.8 50 166 649 ± 10 1,4 Y   848 NGC 6762 Sab A 19:05:371 63:20:24.7 63 150 468 ± 5 1,19 Y   849 NGC 7025 S0a A 21:07:47.3 16:20:09.2 44 50 468 ± 5 1,19 Y   849 NGC 7025 S0a A 21:07:47.3 16:20:09.2 44 50 468 ± 5 1,19 Y   849 NGC 7591 Sbc B 23:18:	277	NGC 2916	Sbc	A	09:34:57.6	21:42:18.9	54	18	$3730 \pm 7$	5, 4	Y
341 UGC5771 E6 A 10:37:19.3 43:35:15.3 45 52 7403 ± 52 5,9 Y A (79 NGC 4003 S0a B 11:57:59.0 23:07:29.6 67 167 6509 ± 32 5,4 N (DD)   486 UGC7012 Scd AB 12:02:03.1 29:50:52.7 58 10 3081 ± 1 1,10 Y   515 NGC 4185 Sbc AB 12:15:15.8 65:59:07.2 43 100 2732 ± 7 5,3 Y   518 NGC 4210 Sb B 12:15:15.8 65:59:07.2 43 100 2732 ± 7 5,3 Y   528 IC776 Sdm A 12:19:03.1 08:51:22.2 56 98 2468 ± 1 4,12 Y   548 NGC 4470 Sc A 12:29:37.8 07:49:27.1 49 1 2341 ± 1 5,12 Y   608 NGC 5000 Sbc B 13:09:47.5 28:54:25.0 53 6 5608 ± 4 5,4 N (I)   657 UGC8733 Sdm B 13:48:39.0 43:24:44.8 61 140 2338 ± 6 1,4 Y   665 UGC8781 Sb B 13:55:51.0 37:47:50.1 51 78 3042 ± 25 5,14 Y   680 NGC 5394 Sbc B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5,6 N (DF)   660 UGC9476 Sbc A 14:43:32.0 44:30:46.0 51 132 3262 ± 8 5,3 Y   676 UGC9476 Sbc A 16:07:13.0 07:58:44.4 53 155 2848 ± 5 5,15 Y   824 IC1199 Sb AB 16:10:34.3 10:02:25.3 49:50:24.9 50 166 6015 ± 40 5,4 Y   826 NGC 6081 S0a A 16:12:56.9 09:52:01.6 64 129 5176 ± 31 5,9 Y   833 NGC 6154 Sab B 17:16:47.7 61:55:12.4 67 14 633 ± 4 5,16 Y   852 UGC10796 Scd AB 17:18:43.7 58:08:06.4 67 92 8746 ± 6 5,9 Y   854 UGC10811 Sb B 17:18:43.7 58:08:06.4 67 92 8746 ± 6 5,9 Y   855 UGC10796 Scd AB 17:23:47.3 26:29:11.5 54 90 07:43:43 ± 31 1,18 Y   866 NGC 6061 Soa A 17:34:06.4 25:20:38 56 115 522.3 ± 7 1,18 Y   877 UGC10171 Sab A 17:18:43.7 58:08:06.4 67 92 8746 ± 26 5,17 Y   878 NGC 6062 Sab A 10:00:35.7 42:41:33.7 58:08:06.4 67 92 8746 ± 26 5,17 Y   879 UGC10796 Scd AB 17:23:47.3 26:29:11.5 54 90 07:43:43 ± 31 1,18 Y   866 UGC11228 S0 B 13:35:35.7 42:41:33.7 63:36:02.2 44 50 4968 ± 5 1,19 Y   877 UGC11717 Sab A 21:07:47.3 16:20:09.2 44 50 4968 ± 5 1,19 Y   878 NGC 7321 Sbc B 22:36:28.0 21:37:18.4 46 55 770 ± 23 1,23 N (DF)   879 UGC12185 Sb B 22:47:25.1 31:22:47.7 63 150 6649 ± 10 1,4 Y   870 UGC12185 Sb B 23:18:16.3 06:35:08.9 54 70 4966 ± 4 1,4 Y   870 UGC12185 Sb B 23:18:16.3 06:35:08.9 54 70 4966 ± 4 1,4 Y   870 UGC12185 Sb B 23:18:16.3 06:35:08.9 54 70 4966 ± 4 1,4 Y   870 UGC12185 Sb B 23:18:16.3 06:35:08.9 54 70 4966 ±	306	UGC5358	Sd	В	09:58:47.1	11:23:19.3	74	75	$2914 \pm 1$	5, 7	N (DF)
479         NGC 4003         S0a         B         11:57:59.0         23:07:29.6         67         167         6509 ± 32         5, 4         N (DD)           486         UGC7012         Scd         AB         12:02:03.1         29:50:52.7         58         10         3081 ± 1         1,10         Y           515         NGC 4210         Sb         B         12:15:15.8         65:59:07.2         43         100         2732 ± 7         5,3         Y           518         NGC 4210         Sb         B         12:15:15.8         65:59:07.2         43         100         2732 ± 7         5,3         Y           528         IC776         Sdm         A         12:19:03.1         08:51:22.2         56         98         2468 ± 1         4,12         Y           608         NGC 5000         Sbc         B         13:09:47.5         28:54:25.0         53         6         5608 ± 4         5,4         N(D           665         UGC8731         Sb         B         13:55:22.7         21:32:21.7         59         175         7592 ± 15         1,13         Y           665         UGC8781         Sb         B         13:56:51.0         37:47:50.1         <	307	UGC5359	Sb	В		19:12:53.9	70	94	$8472 \pm 9$	5, 8	Y
486         UGC7012         Scd         AB         12:02:03.1         29:50:52.7         58         10         3081 ± 1         1, 10         Y           515         NGC 4185         Sbc         AB         12:13:22.2         28:30:39.5         50         164         3904 ± 5         5, 11         Y           518         NGC 4210         Sb         B         12:15:15.8         65:59:07.2         43         100         2732 ± 7         5, 3         Y           528         IC776         Sdm         A         12:19:03.1         08:51:22.2         56         98         2468 ± 1         4, 12         Y           548         NGC 5000         Sbc         A         12:29:37.8         07:49:27.1         49         1         2341 ± 1         5, 12         Y           668         NGC 5000         Sbc         B         13:59:22.7         28:54:25.0         53         6         5668 ± 4         5, 4         N (D           665         UGC8733         Sdm         B         13:55:22.7         21:32:21.7         59         175         7592 ± 15         1, 13         Y           676         NGC 5378         Sb         B         13:56:51.0         37:27:13.1	341	UGC5771	E6	A	10:37:19.3	43:35:15.3	45	52	$7403 \pm 52$	5, 9	Y
515         NGC 4185         Sbc         AB         12:13:22.2         28:30:39.5         50         164         3904 ± 5         5, 11         Y           518         NGC 4210         Sb         B         12:15:15.8         65:59:07.2         43         100         2732 ± 7         5, 3         Y           528         IC776         Sdm         A         12:19:03.1         08:51:22.2         56         98         2468 ± 1         4, 12         Y           548         NGC 5000         Sbc         B         13:09:47.5         28:54:25.0         53         6         5608 ± 4         5, 4         N (I)           657         UGC8733         Sdm         B         13:59:22.7         21:32:21.7         59         175         7592 ± 15         1, 13         Y           665         UGC8781         Sb         B         13:55:33.2         37:27:13.1         51         78         3042 ± 25         5, 14         Y           665         UGC93476         Sbc         B         13:55:33.2         37:27:13.1         41         60         3448 ± 2         5, 6         N (DF)           764         NGC 5720         Sbc         B         14:38:33.3         50:48:54.9 <td>479</td> <td>NGC 4003</td> <td>S0a</td> <td>В</td> <td>11:57:59.0</td> <td>23:07:29.6</td> <td>67</td> <td>167</td> <td><math>6509 \pm 32</math></td> <td>5, 4</td> <td>N (DD)</td>	479	NGC 4003	S0a	В	11:57:59.0	23:07:29.6	67	167	$6509 \pm 32$	5, 4	N (DD)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	486	UGC7012	Scd	AB	12:02:03.1	29:50:52.7	58	10	$3081 \pm 1$	1, 10	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	515	NGC 4185	Sbc	AB	12:13:22.2	28:30:39.5	50	164	$3904 \pm 5$	5, 11	Y
548         NGC 4470         Sc         A         12:29:37.8         07:49:27.1         49         1         2341 ± 1         5, 12         Y           608         NGC 5000         Sbc         B         13:09:47.5         28:54:25.0         53         6         5608 ± 4         5, 4         N (I)           657         UGC8733         Sdm         B         13:48:39.0         43:24:44.8         61         140         2338 ± 6         1, 4         Y           665         UGC8781         Sb         B         13:48:39.0         43:24:44.8         61         140         2338 ± 6         1, 4         Y           665         UGC8731         Sb         B         13:55:21.7         21:32:21.7         59         175         7592 ± 15         1, 13         Y           666         NGC 5378         Sb         B         13:55:33.2         37:27:13.1         41         60         3448 ± 2         5, 6         N (DF)           764         NGC 5720         Sbc         B         14:38:33.3         50:48:54.9         49         52         7790 ± 6         5, 9         Y           823         NGC 60631         Sbc         A         16:07:13.0         07:58:44.4	518	NGC 4210	Sb	В	12:15:15.8	65:59:07.2	43	100	$2732 \pm 7$	5, 3	Y
608         NGC 5000         Sbc         B         13:09:47.5         28:54:25.0         53         6         5608 ± 4         5, 4         N (I)           657         UGC8733         Sdm         B         13:48:39.0         43:24:44.8         61         140         2338 ± 6         1, 4         Y           665         UGC8781         Sb         B         13:52:22.7         21:32:21.7         59         175         7592 ± 15         1, 13         Y           666         UGC97878         Sb         B         13:56:51.0         37:47:50.1         51         78         3042 ± 25         5, 14         Y           680         NGC 5394         Sbc         B         13:56:51.0         37:47:50.1         51         78         3042 ± 25         5, 14         Y           769         UGC9476         Sbc         A         14:31:32.0         44:30:46.0         51         132         3262 ± 8         5, 3         Y           823         NGC 6063         Sbc         A         16:07:13.0         07:58:44.4         53         155         2848 ± 5         5, 15         Y           824         IC1199         Sb         AB         16:10:34.3         10:02:25.3	528	IC776	Sdm	A	12:19:03.1	08:51:22.2	56	98	$2468 \pm 1$	4, 12	Y
657 UGC8733 Sdm B 13:48:39.0 43:24:44.8 61 140 2338 ± 6 1, 4 Y 665 UGC8781 Sb B 13:55:22.7 21:32:21.7 59 175 7592 ± 15 1, 13 Y 676 NGC 5378 Sb B 13:56:51.0 37:47:50.1 51 78 3042 ± 25 5, 14 Y 680 NGC 5394 Sbc B 13:58:33.2 37:27:13.1 41 60 3448 ± 2 5, 6 N (DF) 764 NGC 5720 Sbc B 14:38:33.3 50:48:54.9 49 52 7790 ± 6 5, 9 Y 769 UGC9476 Sbc A 14:41:32.0 44:30:46.0 51 132 3262 ± 8 5, 3 Y 823 NGC 6063 Sbc A 16:07:13.0 07:58:44.4 53 155 2848 ± 5 5, 15 Y 824 IC1199 Sb AB 16:10:34.3 10:02:25.3 67 159 4731 ± 44 5, 9 Y 826 NGC 6081 S0a A 16:12:56.9 09:52:01.6 64 129 5176 ± 31 5, 9 Y 846 UGC10695 E5 A 17:05:05.6 43:02:35.4 47 117 8328 ± 34 5, 22 N (DD) 850 NGC 6314 Sab B 16:25:30.5 49:50:24.9 50 166 6015 ± 40 5, 4 Y 852 UGC10796 Scd AB 17:16:47.7 61:55:12.4 62 62 3079 ± 11 5, 5 N (DF) 854 UGC10811 Sb B 17:18:43.7 58:08:06.4 67 92 8746 ± 26 5, 17 Y 858 UGC10905 S0a A 17:34:06.4 25:20:38.3 59 0 7843 ± 34 1, 18 Y 863 NGC 6497 Sab B 17:51:18.0 59:28:15.2 50 116 6162 ± 64 5, 9 Y 874 NGC 6762 Sab A 19:05:37.1 63:56:02.8 62 115 923 ± 47 1, 9 Y 875 UGC11717 Sab A 21:18:35.4 19:43:07.4 63 35 6303 ± 36 1, 9 Y 877 UGC11717 Sab A 21:18:35.4 19:43:07.4 63 35 6303 ± 36 1, 9 Y 877 UGC11717 Sab A 21:18:35.4 19:43:07.4 63 35 6303 ± 36 1, 9 Y 878 NGC 7321 Sbc B 22:36:28.0 21:37:18.4 46 25 7145 ± 5 1, 19 Y 879 UGC11818 Sb B 22:36:28.0 21:37:18.4 46 25 7145 ± 5 1, 19 Y 870 UGC11218 Sb B 22:36:28.0 21:37:18.4 46 25 7145 ± 5 1, 19 Y 877 UGC11717 Sab A 21:18:35.4 19:43:07.4 63 35 6303 ± 36 1, 9 Y 870 UGC12185 Sb B 22:36:28.0 21:37:18.4 46 25 7145 ± 5 1, 19 Y 870 UGC12185 Sb B 22:36:28.0 21:37:18.4 46 25 7145 ± 5 1, 19 Y 870 UGC12185 Sb B 23:15:17.3 19:02:30.4 41 110 4736 ± 3 1, 24 N (DF) 904 NGC 7591 Sbc B 23:18:16.3 06:35:08.9 54 170 4956 ± 4 1, 4 Y	548	NGC 4470	Sc	A	12:29:37.8	07:49:27.1	49	1	$2341 \pm 1$	5, 12	Y
665	608	NGC 5000	Sbc	В	13:09:47.5	28:54:25.0	53	6	$5608 \pm 4$	5, 4	N (I)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	657	UGC8733	Sdm	В	13:48:39.0	43:24:44.8	61	140	$2338 \pm 6$	1, 4	Y
680         NGC 5394         Sbc         B         13:58:33.2         37:27:13.1         41         60         3448 ± 2         5, 6         N (DF)           764         NGC 5720         Sbc         B         14:38:33.3         50:48:54.9         49         52         7790 ± 6         5, 9         Y           769         UGC9476         Sbc         A         14:41:32.0         44:30:46.0         51         132         3262 ± 8         5, 3         Y           823         NGC 6063         Sbc         A         16:07:13.0         07:58:44.4         53         155         2848 ± 5         5, 15         Y           824         IC1199         Sb         AB         16:10:34.3         10:02:25.3         67         159         4731 ± 44         5, 9         Y           826         NGC 6081         Soa         A         16:12:56.9         09:52:01.6         64         129         5176 ± 31         5, 9         Y           846         UGC10695         E5         A         17:05:05.6         43:02:35.4         47         117         8328 ± 34         5, 22         N (DD)           850         NGC 6314         Sab         A         17:16:47.7         61:55:12.	665	UGC8781	Sb	В	13:52:22.7	21:32:21.7	59	175	$7592 \pm 15$	1, 13	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	676	NGC 5378	Sb	В	13:56:51.0	37:47:50.1	51	78	$3042 \pm 25$	5, 14	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	680	NGC 5394	Sbc	В	13:58:33.2	37:27:13.1	41	60	$3448 \pm 2$	5, 6	N (DF)
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824         IC1199         Sb         AB         16:10:34.3         10:02:25.3         67         159         4731 ± 44         5, 9         Y           826         NGC 6081         S0a         A         16:12:56.9         09:52:01.6         64         129         5176 ± 31         5, 9         Y           833         NGC 6154         Sab         B         16:25:30.5         49:50:24.9         50         166         6015 ± 40         5, 4         Y           846         UGC10695         E5         A         17:05:05.6         43:02:35.4         47         117         8328 ± 34         5, 22         N (DD)           850         NGC 6314         Sab         A         17:12:38.7         23:16:12.3         60         174         6633 ± 4         5, 16         Y           852         UGC10796         Scd         AB         17:16:47.7         61:55:12.4         62         62         3079 ± 11         5, 5         N (DF)           854         UGC10811         Sb         B         17:18:43.7         58:08:06.4         67         92         8746 ± 26         5, 17         Y           856         IC1256         Sb         AB         17:51:18.0         59:28:	769	UGC9476	Sbc	A	14:41:32.0	44:30:46.0	51	132	$3262 \pm 8$	5, 3	Y
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833         NGC 6154         Sab         B         16:25:30.5         49:50:24.9         50         166         6015 ± 40         5, 4         Y           846         UGC10695         E5         A         17:05:05.6         43:02:35.4         47         117         8328 ± 34         5, 22         N (DD)           850         NGC 6314         Sab         A         17:12:38.7         23:16:12.3         60         174         6633 ± 4         5, 16         Y           852         UGC10796         Scd         AB         17:16:47.7         61:55:12.4         62         62         3079 ± 11         5, 5         N (DF)           854         UGC10811         Sb         B         17:18:43.7         58:08:06.4         67         92         8746 ± 26         5, 17         Y           856         IC1256         Sb         AB         17:23:47.3         26:29:11.5         54         90         4730 ± 10         1, 4         Y           858         UGC10905         S0a         A         17:34:06.4         25:20:38.3         59         0         7843 ± 34         1, 18         Y           863         NGC 6497         Sab         B         17:51:18.0         59:28:	824	IC1199	Sb	AB	16:10:34.3	10:02:25.3	67	159	$4731 \pm 44$	5, 9	Y
846         UGC10695         E5         A         17:05:05.6         43:02:35.4         47         117         8328 ± 34         5, 22         N (DD)           850         NGC 6314         Sab         A         17:12:38.7         23:16:12.3         60         174         6633 ± 4         5, 16         Y           852         UGC10796         Scd         AB         17:16:47.7         61:55:12.4         62         62         3079 ± 11         5, 5         N (DF)           854         UGC10811         Sb         B         17:18:43.7         58:08:06.4         67         92         8746 ± 26         5, 17         Y           856         IC1256         Sb         AB         17:23:47.3         26:29:11.5         54         90         4730 ± 10         1, 4         Y           858         UGC10905         S0a         A         17:34:06.4         25:20:38.3         59         0         7843 ± 34         1, 18         Y           863         NGC 6497         Sab         B         17:51:18.0         59:28:15.2         50         116         6162 ± 64         5, 9         Y           865         UGC11228         S0         B         18:24:46.3         41:29:3	826	NGC 6081	S0a	A	16:12:56.9	09:52:01.6	64	129	$5176 \pm 31$	5, 9	Y
850         NGC 6314         Sab         A         17:12:38.7         23:16:12.3         60         174         6633 ± 4         5, 16         Y           852         UGC10796         Scd         AB         17:16:47.7         61:55:12.4         62         62         3079 ± 11         5, 5         N (DF)           854         UGC10811         Sb         B         17:18:43.7         58:08:06.4         67         92         8746 ± 26         5, 17         Y           856         IC1256         Sb         AB         17:23:47.3         26:29:11.5         54         90         4730 ± 10         1, 4         Y           858         UGC10905         S0a         A         17:34:06.4         25:20:38.3         59         0         7843 ± 34         1, 18         Y           863         NGC 6497         Sab         B         17:51:18.0         59:28:15.2         50         116         6162 ± 64         5, 9         Y           865         UGC11228         S0         B         18:24:46.3         41:29:33.8         56         165         5771 ± 23         1, 23         N (DF)           866         UGC11262         Sc         A         18:30:35.7         42:41:3	833	NGC 6154	Sab	В	16:25:30.5	49:50:24.9	50	166	$6015 \pm 40$	5, 4	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	846	UGC10695	E5	A	17:05:05.6	43:02:35.4	47	117	$8328 \pm 34$	5, 22	N (DD)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	850	NGC 6314	Sab	A	17:12:38.7	23:16:12.3	60	174	$6633 \pm 4$	5, 16	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	852	UGC10796	Scd	AB	17:16:47.7	61:55:12.4	62	62	$3079 \pm 11$	5, 5	N (DF)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	854	UGC10811	Sb	В	17:18:43.7	58:08:06.4	67	92	$8746 \pm 26$	5, 17	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	856	IC1256	Sb	AB	17:23:47.3	26:29:11.5	54	90	$4730 \pm 10$	1, 4	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	858	UGC10905	S0a	Α		25:20:38.3	59	0	$7843 \pm 34$	1, 18	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	863	NGC 6497	Sab	В	17:51:18.0	59:28:15.2	50	116	$6162 \pm 64$	5, 9	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	865	UGC11228	S0	В	18:24:46.3	41:29:33.8	56	165	$5771 \pm 23$	1, 23	N (DF)
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	866	UGC11262	Sc	A	18:30:35.7	42:41:33.7	69	48	$5606 \pm 36$	4, 18	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	867	NGC 6762	Sab	Α	19:05:37.1	63:56:02.8	62	115	$2923 \pm 47$	1, 9	Y
$\begin{array}{cccccccccccccccccccccccccccccccccccc$											
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896 NGC 7466 Sbc A 23:02:03.5 27:03:09.3 59 25 $7508 \pm 3$ 1, 20 Y 901 NGC 7549 Sbc B 23:15:17.3 19:02:30.4 41 110 $4736 \pm 3$ 1, 24 N (DF) 904 NGC 7591 Sbc B 23:18:16.3 06:35:08.9 54 170 4956 $\pm 4$ 1, 4 Y											
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904 NGC 7591 Sbc B 23:18:16.3 06:35:08.9 54 170 4956 $\pm$ 4 1, 4 Y											
											N (DF)

Notes. Column (1): CALIFA ID. Column (2): Galaxy name. Column (3): morphological type, as classified by CALIFA. Column (4): CALIFA bar classification. Column (5): photometric right ascension as provided by NED. Column (6): photometric declination as provided by NED. Column (7): photometric inclination. Column (8): photometric disc PA. Column (9): systemic heliocentric velocity. Column (10): reference key for  $\phi'_p$ , and  $V_{sys}$ . Column (11): Y: successfully modelled. N: unable to model, not included in final sample (DD: distorted inner disk. I: inclination out of range. DF: not in dynamical equilibrium).

References. (1): Skrutskie et al. (2006). (2): Lu et al. (1993). (3): Theureau et al. (1998). (4): de Vaucouleurs et al. (1991). (5): Adelman-McCarthy et al. (2008). (6): Epinat et al. (2008a). (7): O'Neil (2004). (8): Theureau et al. (2007). (9): Falco et al. (1999). (10): Nordgren et al. (1997). (11): Ramella et al. (1995). (12): Kent et al. (2008). (13): dell'Antonio, Bothun & Geller (1996). (14): Huchra, Geller & Corwin (1995). (15): Freudling, Haynes & Giovanelli (1992). (16): Haynes et al. (1997). (17): Abazajian et al. (2003). (18): Marzke, Huchra & Geller (1996). (19): Giovanelli & Haynes (1993). (20): Saintonge et al. (2008). (21): Wegner, Haynes & Giovanelli (1993). (22): Davoust & Considere (1995). (23): Wegner et al. (2003). (24): Nishiura et al. (2000).



**Figure 2.** Distribution of morphological type (left) and photometric bar strength (right) for the galaxies modelled with DISKFIT. In both panels, the dotted line shows the distribution of all 100 CALIFA DR1 galaxies, the blue histogram shows the distribution for the subset of 49 intermediate-inclination, gas-rich galaxies that we attempted to model with DISKFIT (see Section 2) and the red histogram shows the distribution of our final sample of 37 galaxies for which valid kinematic models were obtained (see Section 4). The modelled galaxies span a range of morphological type and barredness.

galaxies with bar classification A or AB, this radius is one half that of the disk. For those galaxies with bar classification B,  $R_{\rm max}$  is the larger of either one half the galaxy radius or the estimated bar radius plus 20 per cent to ensure that the entire bar is included.

We also applied a model with radial flows that is also available in DISKFIT and assumes an m = 0 perturbation in the disc plane:

$$V_{\text{model}}(R) = V_{\text{sys}}(R) + \sin i \left[ \bar{V}_{\text{t}}(R) \cos \theta + \bar{V}_{\text{r}}(R) \sin \theta \right], \tag{3}$$

where  $\bar{V}_{\rm r}$  is the radial velocity. Since quiescent disc galaxies are unlikely to exhibit large radial flows, we focus our analysis on the rotation only and bisymmetric DISKFIT models.

DISKFIT can also fit for a warp in the outer disc. The disc is assumed to be flat out to some radius  $r_w$  after which the ellipticity and PA vary quadratically with increasing radius. There are degeneracies between fitting for a warp and bisymmetric flows since both can cause variations in the ellipticity and PA of the flow pattern, and therefore both of these components cannot be fit simultaneously. We apply a warp model in only a few cases where non-circular flows are evident but not well parametrized by other models.

Multiple DISKFIT models were attempted for the 49/100 DR1 galaxies selected using the criteria in Section 2. DISKFIT was applied to each galaxy automatically using a series of scripts to drive the publicly available executable. We adopt  $i_p$  described in Section 2 as an initial guess for  $i_k$  and use the literature  $V_{\rm sys}$  values from Table 1 as an initial guess for that parameter. The PA and  $R_{\rm max}$  were visually estimated from contour plots of the input velocity field, and the centre position was initially chosen as the central pixel of the PMAS IFU. Although the atmospheric seeing in the CALIFA observations is typically  $\sim$ 1 arcsec (Sánchez et al. 2012) the spatial resolution of the velocity field is  $\sim$ 3.5 arcsec. The ring radii at which the velocity components were sampled by DISKFIT were spaced by 3 arcsec.

Initially rotation only (equation 1), bisymmetric (equation 2) and radial (equation 3) models were applied to the velocity fields for each of the 49/100 galaxies selected as described in Section 2. We generate 100 bootstrap realizations of each velocity field to determine uncertainties on each model parameter as described in Sellwood & Sánchez 2010. The parameter  $\Delta$ ISM (interstellar medium) is added in quadrature to the uncertainties in the emission line centroids during the fit which allows for turbulence in the ISM

(Spekkens & Sellwood 2007). A value of  $\Delta$ ISM=5 km s<sup>-1</sup> was used for all models. For all successfully modelled galaxies (see Section 4), uncertainties on all parameters were derived from 1000 bootstrap realizations of the best-fitting model.

#### 4 RESULTS

In the following sections, we detail the process by which an optimal DISKFIT model was selected for each of the modelled galaxies (Section 4.1), provide an in-depth case study for two representative systems (NGC 1056 and NGC 7321, Section 4.2), and present the results from the DISKFIT models for the sample as a whole (Section 4.3).

#### 4.1 Model selection

Each of the DISKFIT models described in Section 3 was applied to the 49/100 DR1 galaxies that satisfy the criteria described in Section 2. We then proceeded to determine which model provided the best characterization of the data. The overall fit quality was assessed by examining the model, (data – model) residuals, disc geometries and rotation curves for the rotation only, bisymmetric and radial models. Since the radial model was used primarily for diagnostic purposes, we focused on determining whether the rotation only or bisymmetric model provided the best description of each system. We illustrate the details of this process for two representative sample galaxies in Section 4.2.

In addition to examining the DISKFIT outputs described above, a chi-square test was used to determine the statistical significance of any non-circular flows returned by the bisymmetric and radial model fits. The  $\chi^2$  statistic for the null hypothesis that the non-circular flows are consistent with zero is given by

$$\chi_{\text{NC}}^2 = \sum_{i=1}^N \frac{(x_i - \mu_i)^2}{\sigma_i^2} = \sum_{i=1}^N \frac{x_i^2}{\sigma_i^2},\tag{4}$$

where  $x_i$  is the velocity ( $V_{2,t}$  or  $V_{2,r}$  for the bisymmetric model),  $\sigma_i$  is its uncertainty, N is the number of radial bins in which the flow is measured and  $\mu_i = 0$ . We deem that values of  $\chi^2_{NC} > 5\sigma$  for the bisymmetric model, where  $\sigma$  is the standard deviation of the  $\chi^2$ 

distribution with N degrees of freedom, signal statistically significant flows, values  $3\sigma < \chi^2_{\rm NC} < 5\sigma$  represent marginally significant flows, and insignificant flows have  $\chi^2_{\rm NC} < 3\sigma$ . The chi-square test was found to be useful in determining the best physical model but was not always accurate. Specifically, the significance threshold of  $5\sigma$  was too stringent in four cases (NGC 477, UGC 3253, NGC 5720 and UGC 12185) where the uncertainties are large for the bisymmetric model. Of these, in two cases (NGC 5720 and UGC 12185)  $\chi^2_{\rm NC} > 5\sigma$  if the centre position is fixed, and all four had  $\chi^2_{\rm NC} > 5\sigma$  if the radial model was examined. The chi-square test is therefore a good indicator of significant non-circular flows, but it was still necessary to examine by-eye the residuals, disc geometry and kinematic components for each model to determine which was optimal.

The optimal physical model for each galaxy fell into one of two possible categories: *Rotation Only* (25/37 or 67.6 $^{+6.6}_{-8.5}$  per cent galaxies), and *Non-Circular Flows* (12/37 or 32.4 $^{+8.5}_{-6.6}$  per cent galaxies). Note that the uncertainties on derived fractions correspond to the  $1\sigma$  confidence intervals obtained using the Bayesian approach of Cameron (2011). The *Rotation Only* category includes all galaxies where either a rotation only model was deemed to be optimal (17/25 or  $68.0^{+7.7}_{-10.4}$  per cent galaxies), or where a search for bisymmetric flows was not possible (8/25 or  $32.0^{+10.4}_{-7.7}$  per cent galaxies). This *Can't Tell* subcategory contains galaxies with velocity fields lacking significant H  $\alpha$  emission or containing masked pixels near the galaxy centre. The majority of the galaxies that fell into the *Non-Circular Flows* category have significant non-circular flows in the bisymmetric model that are consistent with bar-like flows. We return to this issue in Section 5.

Out of the 49/100 galaxies that we attempted to model, 10 galaxies were eliminated from further consideration because they did not meet the assumptions inherent in the DISKFIT models. Two galaxies (NGC 4003 and UGC 10695) had model residuals that suggested they have strongly distorted inner discs, and eight were determined to be disturbed and unlikely to be in dynamical equilibrium as implicitly assumed by any model that fits for a rotating disc. Although fixing parameters during kinematic model fitting is common in the literature (e.g. de Blok et al. 2008), it was decided that if DISKFIT could not find the inclination of the galaxy, even in the simplest rotation only model, that it was unlikely that the galaxy could be well modelled as an equilibrium flat disc. There are therefore 39/100 CALIFA DR1 galaxies for which valid models were determined. Table 1 indicates which of the 49/100 galaxies were successfully modelled and those that were eliminated for these reasons. For consistency with the photometric selection criteria in Section 2, we eliminated an additional two systems for which  $i_k < 40^\circ$ . Our final sample therefore consists of 37/100 CALIFA DR1 galaxies, whose distribution in morphological type and barredness is shown by the red histograms in Fig. 2.

The results of the best-fitting models for the final sample galaxies are shown in Table 2. The velocity field, velocity uncertainties, best-fitting model and residuals for each galaxy can be found online in Appendix A. The H  $\alpha$  velocity fields for the 12 galaxies where fits were attempted but then rejected can be found online in Appendix B. Detailed notes on all of the 49/100 galaxies are online in Appendix C.

#### 4.2 Model selection for representative galaxies

In this section, we illustrate the optimal DISKFIT model selection process outlined in Section 4.1 for the representative galaxies NGC

1056, a galaxy that we classify as having rotation only flows, and NGC 7321, which we classify as having non-circular flows. For both galaxies, the best-fitting disk parameters for the rotation only and bisymmetric models are given in Table 3.

#### 4.2.1 NGC 1056

NGC 1056 is at a distance of 18.7 Mpc (Theureau et al. 2007). It is classified as having morphological-type Sa with photometric bar classification A (Walcher et al. 2014) and is a typical example of a galaxy whose H  $\alpha$  velocity field is best described by a rotation only model. Panel (a) of Fig. 1 shows the SDSS 2 arcmin  $\times$  2 arcmin igr composite image of this galaxy. Fig. 3 shows the H  $\alpha$  velocity field and corresponding uncertainties, as well as the best-fitting rotation only and bisymmetric models and their residuals. There is H  $\alpha$  emission throughout the disk and the velocity field is well determined, with uncertainties  $\Delta v_{\rm obs} < 7 \ {\rm km \, s^{-1}}$  throughout most of the inner disk. The residuals for the rotation only model show no apparent coherent patterns, and the bisymmetric model does not significantly reduce the residuals despite the additional free parameters in the fit and lower reduced  $\chi^2_R$  relative to the rotation only fit. As shown in Table 3, there is good agreement between the derived kinematic parameters for both models. Note that the relatively high values of  $\chi_R^2$  for both models suggested that  $\Delta ISM=5 \, \mathrm{km \, s^{-1}}$  is too low for this galaxy.

The rotation only model was chosen for NGC 1056 because there is no evidence for non-circular flows in the model residuals. A chi-square test run on the components of the bisymmetric flow (equation 2) supports this assessment, which returned  $\chi^2_{NC} < 3\sigma$  and therefore no evidence against the null hypothesis of a purely rotating disc.

NGC 1056 is one of few sample galaxies where a published rotation curve derived from an independent H  $\alpha$  velocity field is available for comparison. Fig. 4 shows the DISKFIT rotation curve for the rotation only model (blue curve) compared to that published by Epinat, Amram & Marcelin (2008b) from the GHASP survey (solid red and green curves for the approaching and receding sides, respectively). The published rotation curve has an amplitude of  $\bar{V}_{\rm t} \sim 160 \, \rm km \, s^{-1}$  which is significantly greater than that found with DISKFIT of  $\bar{V}_{\rm t} \sim 130 \, \rm km \, s^{-1}$ . This difference arises primarily due to the difference in kinematic inclination found by DISKFIT ( $i_k = 58^{\circ} \pm 2^{\circ}$ ) and by Epinat et al. (2008b,  $i_k = 41^{\circ} \pm 10^{\circ}$ ). The rotation curve from Epinat et al. (2008b) was therefore reprojected using the DISKFIT inclination, and shown as the dashed red and green curves in Fig. 4. There is reasonable agreement between the results from Epinat et al. (2008b) and DISKFIT's rotation only model when the same disc inclination is adopted in both models in the inner 5 arcsec (receding) and beyond 15 arcsec (approaching), considering that Epinat et al. modelled different data using a different algorithm, and considered only half the disc at a time. Epinat et al. (2008b) also used adaptive binning techniques to generate the velocity field from which their rotation curve was derived, which may explain the discrepancies between their results and ours for 5 arcsec < r < 15 arcsec. In general, the disc parameters found by DISKFIT (Table 3) agree well with those from the literature (Table 1; Barrera-Ballesteros et al. 2014; García-Lorenzo et al. 2014).

#### 4.2.2 NGC 7321

NGC 7321 is at a distance of 97.5 Mpc (Theureau et al. 2007). It is classified as having morphological-type Sbc with photometric bar

Table 2. DISKFIT minimization results for final sample of 37 galaxies.

			Sig	X	У	$\phi_{k,d}'$	$i_{ m k}$	$V_{ m sys}$	$\phi_b$	$\phi_b'$
ID	Name	Model	(σ)	(arcsec)	(arcsec)	(deg)	(deg)	$(\text{km s}^{-1})$	(deg)	(deg)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
3	NGC 7819	m2	5.5	$1.1 \pm 0.1$	$-1.2 \pm 0.1$	$80 \pm 2$	$45 \pm 4$	$4955 \pm 1$	$110 \pm 6$	18, 95
7	UGC36	R	0.2	$1.0 \pm 0.1$	$-1.8 \pm 0.1$	$20 \pm 1$	$65 \pm 2$	$6303 \pm 2$		
10	NGC 36	W	0.8	$0.9 \pm 0.3$	$-1.8 \pm 0.6$	$200 \pm 1$	$51 \pm 2$	$5992 \pm 5$		
42	NGC 477	m2	1.8	$5.1 \pm 0.4$	$10.0 \pm 0.3$	$311 \pm 2$	$38 \pm 5$	$5875 \pm 3$	$19 \pm 38$	326, 244
100	NGC 1056	R	1.3	$1.4 \pm 0.2$	$-1.9 \pm 0.2$	$161 \pm 1$	$58 \pm 2$	$1559 \pm 1$		
146	UGC3253	m2	1.8	$0.9 \pm 0.2$	$-1.7 \pm 0.3$	$84 \pm 1$	$52 \pm 3$	$4119 \pm 1$	$59 \pm 11$	64
156	NGC 2449	CT	1.7	$1.4 \pm 0.2$	$-1.3 \pm 0.2$	$136 \pm 1$	$58 \pm 1$	$4903 \pm 2$		
277	NGC 2916	CT	1.9	$0.4 \pm 0.2$	$0.2 \pm 0.7$	$16 \pm 1$	$51 \pm 1$	$3698 \pm 5$		
307	UGC5359	R	1.6	$1.2 \pm 0.1$	$-1.0 \pm 0.1$	$273 \pm 1$	$69 \pm 1$	$8465 \pm 1$		
341	UGC5771	CT	0.1	$1.0 \pm 0.2$	$-1.1 \pm 0.2$	$54 \pm 1$	$34 \pm 8$	$7417 \pm 4$		
486	UGC7012	R	0.5	$1.5 \pm 0.2$	$-0.3 \pm 0.6$	$6. \pm 1$	$52 \pm 4$	$3088 \pm 3$		
515	NGC 4185	R	0.0	$1.0 \pm 0.2$	$-1.4 \pm 0.2$	$168 \pm 1$	$48 \pm 1$	$3873 \pm 1$		
518	NGC 4210	CT	0.0	$0.9 \pm 0.7$	$-0.9 \pm 0.3$	$97 \pm 1$	$41 \pm 1$	$2712 \pm 3$		
528	IC776	R	0.8	$1.9 \pm 0.5$	$0.5 \pm 0.6$	$281 \pm 1$	$46 \pm 4$	$2470 \pm 1$		
548	NGC 4470	R	0.0	$0.5 \pm 0.7$	$0.2 \pm 0.4$	$171 \pm 1$	$47 \pm 2$	$2344 \pm 1$		
657	UGC8733	CT	1.5	$8.1 \pm 1.3$	$0.7 \pm 1.2$	$218 \pm 3$	$63 \pm 5$	$2335 \pm 5$		
665	UGC8781	CT	4.1	$1.2 \pm 0.2$	$-1.3 \pm 0.5$	$160 \pm 1$	$58 \pm 2$	$7571 \pm 4$		
676	NGC 5378	CT	0.1	$-0.2 \pm 0.3$	$-0.9 \pm 0.3$	$84 \pm 2$	$39 \pm 5$	$2960 \pm 2$		
764	NGC 5720	m2	8.3	1.2*	-1.0*	$309 \pm 1$	$51 \pm 1$	$7785 \pm 1$	$47 \pm 4$	278
769	UGC9476	Rad	0.0	$2.1 \pm 0.4$	$-1.2 \pm 0.3$	$117 \pm 3$	$43 \pm 2$	$3247 \pm 2$		
823	NGC 6063	R	0.1	$1.1 \pm 0.2$	$-0.9 \pm 0.1$	$152 \pm 1$	$57 \pm 1$	$2841 \pm 1$		
824	IC1199	R	0.7	$0.8 \pm 0.1$	$-1.6 \pm 0.2$	$158 \pm 1$	$61 \pm 2$	$4708 \pm 2$		
826	NGC 6081	R	0.1	$1.7 \pm 0.4$	$-1.5 \pm 0.3$	$129 \pm 1$	$68 \pm 3$	$5050 \pm 5$		
833	NGC 6154	CT	0.1	$0.4 \pm 0.3$	$0.1 \pm 0.3$	$202 \pm 3$	$70 \pm 6$	$5983 \pm 2$		
850	NGC 6314	R	1.9	$1.6 \pm 0.1$	$-0.5 \pm 0.2$	$176 \pm 1$	$62 \pm 1$	$6614 \pm 4$		
854	UGC10811	m2	6.9	$0.7 \pm 0.2$	$-1.6 \pm 0.1$	$90 \pm 1$	$69 \pm 1$	$8739 \pm 3$	$64 \pm 5$	125
856	IC1256	R	0.0	$1.4 \pm 0.2$	$-0.8 \pm 0.1$	$270 \pm 1$	$52 \pm 1$	$4717 \pm 1$		
858	UGC10905	R	0.1	$1.1 \pm 0.1$	$-0.5 \pm 0.2$	$175 \pm 1$	$60 \pm 1$	$7750 \pm 3$		
863	NGC 6497	m2	6.6	$1.2 \pm 0.2$	$-1.0 \pm 0.2$	$114 \pm 1$	$57 \pm 1$	$6053 \pm 1$	$60 \pm 8$	157
866	UGC11262	R	0.0	$0.7 \pm 0.1$	$-0.9 \pm 0.1$	$54 \pm 1$	$68 \pm 1$	$5546 \pm 1$		
867	NGC 6762	R	5.2	$1.7 \pm 0.2$	$-1.2 \pm 0.2$	$299 \pm 2$	$64 \pm 4$	$2939 \pm 3$		
874	NGC 7025	m2	14.0	$1.0 \pm 0.1$	$-1.0 \pm 0.1$	$40 \pm 1$	$62 \pm 1$	$4925 \pm 2$	$68 \pm 2$	89, 29
877	UGC11717	R	0.4	$0.7 \pm 0.4$	$-1.2 \pm 0.4$	$224 \pm 1$	$59 \pm 2$	$6272 \pm 8$		
887	NGC 7321	m2	9.7	$1.6 \pm 0.2$	$-1.4 \pm 0.3$	$12 \pm 1$	$46 \pm 2$	$7123 \pm 3$	$47 \pm 6$	48
890	UGC12185	m2	7.1	0.6*	-0.9*	$337 \pm 1$	$59 \pm 1$	$6586 \pm 1$	$44 \pm 5$	310
896	NGC 7466	R	1.2	$0.6 \pm 0.2$	$-1.2 \pm 0.3$	$25 \pm 1$	$62 \pm 2$	$7489 \pm 3$		
904	NGC 7591	m2	13.0	$0.6 \pm 0.1$	$-1.1 \pm 0.1$	$145 \pm 1$	$60 \pm 2$	$4929 \pm 1$	$64 \pm 4$	190

Notes. Column (1): CALIFA ID. Column (2): Galaxy name. Column (3): optimal DISKFIT model: R (rotation only); CT (rotation only, can't tell); m2 (bisymmetric); Rad (radial); W (warp). Column (4): maximum  $\sigma$  value from chi-square test on significance of non-circular flows ( $V_{2,t}$  or  $V_{2,r}$ ) in bisymmetric model. Column (5): right ascension of disc centre, relative to photometric centre from Table 1, \* = centre was fixed. Column (6): declination of disc centre, relative to photometric centre from Table 1, \* = centre was fixed. Column (7): disc PA. Column (8): disc inclination. Column (9): disc systemic velocity. Column (10): bisymmetric distortion PA in the disc plane. Column (11): bisymmetric distortion PA in the sky plane. If no photometric bar is evident in the galaxy image, possible values for either the major or minor axis are listed.

classification B (Walcher et al. 2014) and is a typical example of a galaxy whose H  $\alpha$  velocity field is best described by a bisymmetric model. Panel (c) of Fig. 1 shows the SDSS 2 arcmin  $\times$  2 arcmin igr composite image of this galaxy. Fig. 5 shows the H  $\alpha$  velocity field and corresponding uncertainties, as well as the best-fitting rotation only and bisymmetric models and their residuals. Uncertainties in the disc are all relatively small with  $\Delta v_{\rm obs} < 7~{\rm km~s^{-1}}$  across most of the disc, with only small regions of higher uncertainties, up to  $\Delta v_{\rm obs} \sim 25~{\rm km~s^{-1}}$ . Note that while there is a large area masked in the top left of the velocity field due to a foreground star, it does not strongly affect the fit because of its location with respect to the major and minor axes.

Although the rotation only model (Fig. 5c) fits the data reasonably well, the velocity field exhibits 'S-shaped' isovelocity contours along the minor axis that (by definition) are not replicated in

this model. As a result, a coherent feature (residuals negative for 0 arcsec < x < 10 arcsec east of the galaxy centre, and positive residuals 0 arcsec < x < 10 arcsec to the west) is present near the centre of the residual map. The bisymmetric model and residuals are shown in the bottom row of Fig. 5. The model appears to be a good fit, similar to the rotation only model, except it now accounts for the 'S-shaped' feature along the minor axis. A significant difference is noted when comparing the residuals of the rotation only and the bisymmetric models: the coherent rotation only model residual pattern is not present in the bisymmetric model residuals. The kinematic components for the bisymmetric model for NGC 7321 are shown in Fig. 6 where the blue curve is  $\bar{V}_{t}$ , the red curve is  $V_{2,t}$  and the green curve is  $V_{2,t}$ . The disc geometry parameters agree for both the rotation only and bisymmetric models (see Table 3). This is one example where forcing the bisymmetric velocity components ( $V_{2,t}$ 

Table 3. DISKFIT minimization results for representative galaxies NGC 1056 and NGC 7321.

ID (1)	Galaxy (2)	x (arcsec) (3)	y (arcsec) (4)	$\phi'_{k,d}$ (deg) (5)	<i>i</i> <sub>k</sub> (deg) (6)	$V_{\text{sys}} \\ (\text{km s}^{-1}) \\ (7)$	N (8)	χ <sub>R</sub> <sup>2</sup> (9)
100	NGC 1056							
	<b>Rotation Only</b>	$0.1\pm0.2$	$\textbf{-1.9} \pm \textbf{0.2}$	$161\pm1$	$58 \pm 2$	$\textbf{1559} \pm \textbf{1}$	2781	3.8
	Bisymmetric	$0.1 \pm 0.2$	$-1.9 \pm 0.2$	$161 \pm 1$	$59 \pm 1$	$1559\pm1$	2776	3.5
887	NGC 7321							
	Rotation Only	$0.1 \pm 0.1$	$-1.3 \pm 0.3$	$10 \pm 1$	$45 \pm 3$	$7122 \pm 3$	2837	1.5
	Bisymmetric	$\textbf{0.1} \pm \textbf{0.2}$	$-1.4\pm0.3$	$12\pm1$	$\textbf{46} \pm \textbf{2}$	$\textbf{7123} \pm \textbf{3}$	2822	0.9

Notes. Column (1): CALIFA ID. Column (2): Galaxy name and models. Col. (3): right ascension of disc centre, relative to photometric centre from Table 1. Column (4): declination of disc centre, relative to photometric centre from Table 1. Column (5): disc PA. Column (6): disc inclination. Column (7): disc systemic velocity. Column (8): number of degrees of freedom. Column (9): model reduced chi-square. The optimal model for each galaxy is shown in bold.

and  $V_{2,r}$ ) to zero for r>20 arcsec improved the fit by reducing uncertainties in the resulting velocities. Given the lack of coherence in the model residuals, it was determined that the bisymmetric model is optimal for this galaxy. This is corroborated by  $\chi^2_{\rm NC}>5\sigma$  for the bisymmetric flows in Fig. 6.

The bisymmetric model inclination found by DISKFIT is  $i_k =$  $46^{\circ} \pm 2^{\circ}$  which agrees well with the photometric value derived within the CALIFA collaboration of  $i_p = 47^{\circ} \pm 1^{\circ}$  (see Table 1) and is higher than the value from 2MASS of  $i_p = 39^{\circ}$  (Skrutskie et al. 2006). The PA,  $\phi'_{k,d} = 12^{\circ} \pm 1^{\circ}$  is lower than the value of  $\phi'_{p,d} = 25^{\circ}$  estimated from 2MASS data (Skrutskie et al. 2006) but agrees well with other kinematic works such as Barrera-Ballesteros et al. (2014) and García-Lorenzo et al. (2014,  $\phi'_{k,d} = 15^{\circ}$  and  $\phi_{k_d}' = 14^{\circ}.4 \pm 2^{\circ}.8$ , respectively). The morphological PA however, can be easily shifted by the edges of the spiral arms, which lie outside the CALIFA FOV. The systemic velocity found is  $V_{\rm svs} = 7123 \pm 3 \, {\rm km \, s^{-1}}$  (Table 3) which is comparable, although not consistent with, the value from Giovanelli & Haynes (1993) of  $V_{\rm sys} = 7145 \pm 5 \, {\rm km \, s^{-1}}$  (Table 1). This could be because the Giovanelli & Haynes (1993) V<sub>sys</sub> stems from single-dish H I observations rather than detailed modelling of the velocity field: one therefore expects the DISKFIT value to be more accurate. The resulting value for the PA of the bar was determined to be  $\phi_b' = 48^{\circ} \pm 6^{\circ}$ in the sky plane, which seems plausible given the orientation of the optical bar in Fig. 1(c).

#### 4.3 Sample results

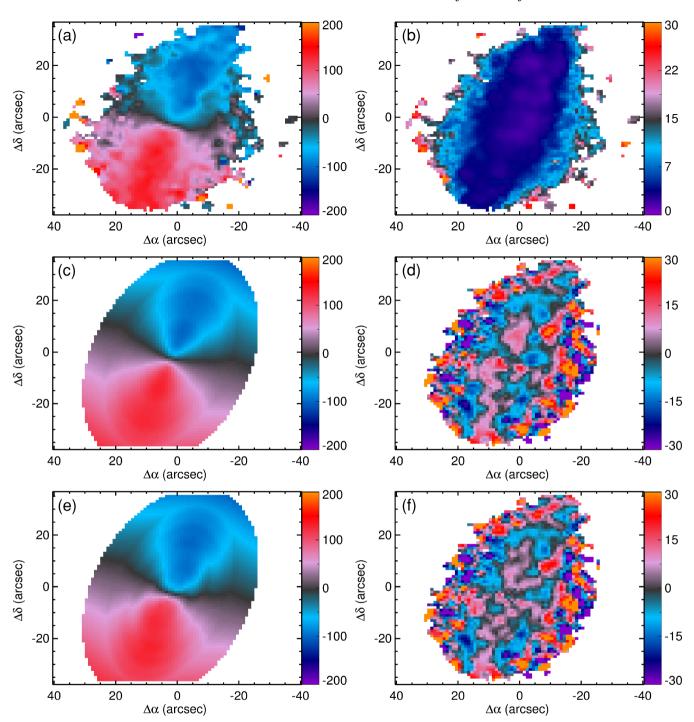
We use the method outlined in Section 4.1 and demonstrated in Section 4.2 to identify the optimal DISKFIT model for each of the 37/100 CALIFA DR1 galaxies that meet the selection criteria of Section 2 for which valid models were obtained. We henceforth restrict our analysis to these 37 systems, and discuss the modelling results from this final sample as a whole in this section.

The model classifications in Table 2 show that the H  $\alpha$  velocity fields of 25/37 (67.6 $^{+6.6}_{-8.5}$  per cent) galaxies are best characterized as *Rotation Only*. Of these, 17/25 (68.0 $^{+7.7}_{-10.4}$  per cent) had an optimal model of rotation only, whereas 8/25 (32.0 $^{+10.4}_{-7.7}$  per cent) galaxies had insufficient H  $\alpha$  or suffered from spatial masking near the galaxy centre that prevented a robust search for non-circular flows and were placed in the *Can't Tell* subcategory. The remaining 12/37 (32.4 $^{+8.5}_{-6.6}$  per cent) galaxies were found to contain *Non-Circular Flows*, such that 10 galaxies were best fit with a bisymmet-

ric model, one galaxy with a warped disc model (NGC 36) and one galaxy with a radial model (UGC 9476). We address these special cases in Section 5.1.

Fig. 7 compares the disc geometry obtained from the rotation only and bisymmetric DISKFIT models of the same galaxy. In all panels, blue symbols represent galaxies in the Rotation Only category including those classified as Can't Tell, while red symbols show galaxies in the Non-Circular Flows category. There are two galaxies for which significant discrepancies exist between the bestfitting rotation only and bisymmetric model disc geometries. First, the linear feature 1 arcsec west of the optical centre in UGC 8733 (see Fig. A16) was fit differently by various DISKFIT models, producing outliers in Fig. 7. Second, the kinematic inclination of the bisymmetric model for UGC 11717 corresponds to the minimum value allowed by DISKFIT, implying an unreliable fit for this galaxy (note that the rotation only model for this galaxy is reliable). Fig. 7 shows that in general, the disc geometry of a given system is consistently determined for all the different models: in most cases, it is the amplitude of the non-circular flows and residual pattern that determines the optimal model, not the disc geometry. This was explicitly shown for the case studies in Section 4.2. This result is also broadly consistent with the conclusions of Barrera-Ballesteros et al. (2014), who find no significant deviation in the PA of the line of nodes in barred galaxies relative to unbarred systems.

Fig. 8 compares the disc geometry of the optimal DISKFIT model for each galaxy to the photometric literature values from Table 1. The colour coding in Fig. 8 is the same as that in Fig. 7. With the exception of UGC 8733 discussed above whose difference in the relative kinematic centre lies beyond the limits of the plot, all of the scatter lies within a single 2.7 arcsec-diameter PPaK fibre. There is good agreement between the kinematic and photometric PA (Fig. 8b). In a few cases, the kinematic PA differs by  $\sim 20^{\circ}$  from the photometric PA, however the corresponding discs are at the low end of the sample inclination range. Fig. 8(c) shows a scatter of the photometric inclination derived by the CALIFA collaboration compared to the kinematic inclination from DISKFIT. There is good agreement between the values within uncertainties with the exception of NGC 6154 and NGC 7025 (Figs A24 and A32, respectively), for which the kinematic inclination is much higher than that returned from the photometry. In general, there is good agreement between the literature and DISKFIT  $V_{
m sys}$ . There are some cases where the DISKFIT  $V_{\rm sys}$  differs by  $\sim 100 \; {\rm km \, s^{-1}}$  from the literature value, however the latter are highly uncertain in these cases (see Table 1).

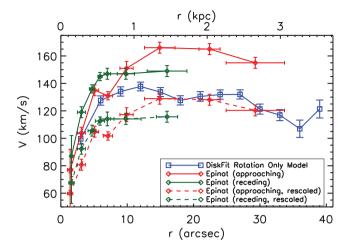


**Figure 3.** DISKFIT model results for NGC 1056, a galaxy that is representative of the *Rotation Only* category. (a) H  $\alpha$  velocity field. (b) Uncertainties in the velocity. (c) Best-fitting rotation only model. (d) Rotation only model residuals. (e) Best-fitting bisymmetric model. (f) Bisymmetric model residuals. In all panels, the colourbar is in km s<sup>-1</sup>.

Fig. 9 shows the weighted mean value of  $V_{2,t}$  (stars) and  $V_{2,r}$  (triangles) as a function of the number of independent radial bins (bottom) or arcsec from the centre (top) over which the non-circular flow was detected for those final sample galaxies where the bisymmetric model was deemed optimal. The mean value of  $V_{2,t}$  or  $V_{2,r}$  exceeds 15 km s<sup>-1</sup> over two independent radial rings in each galaxy, as illustrated by the horizontal and vertical dashed lines in Fig. 9. We adopt this pair of values as DISKFIT's detectability threshold for

non-circular flows in the final sample, and discuss its implications in Section 5.2.

Fig. 10 shows the distribution of modelled galaxies as a function of morphological type (left) and photometric bar classification (right). It illustrates that the photometric bar classification agrees with the model selected in  $86.2^{+4.1}_{-8.8}$  per cent (25/29) of the galaxies that contained enough H  $\alpha$  to search for non-circular flows. Of the 16/37 galaxies photometrically classified as unbarred,



**Figure 4.** Comparison between DISKFIT rotation curve for NGC 1056 and that from the GHASP survey (Epinat et al. 2008b). The blue curve is the rotation curve from the rotation only model shown in Fig. 3. The red and green solid curves are velocities from Epinat et al. (2008b) for the approaching and receding sides, respectively. The dashed red and green curves are the approaching and receding velocities from Epinat et al. (2008b) rescaled from their kinematic inclination of  $i_k = 41^{\circ}$  to the DISKFIT-derived  $i_k = 58^{\circ}$ .

 $81.2^{+6.2}_{-13.1}$  per cent (13/16) were found to be best fit with the rotation only model. Of the 14/37 galaxies that were photometrically classified as barred,  $57.1^{+11.5}_{-13.3}$  per cent (8/14) were found to have significant non-circular flows and an additional  $35.7^{+13.9}_{-10.2}$  per cent (5/14) of these galaxies were placed into the *Can't Tell* subcategory due to the lack of H  $\alpha$  or spatial masking near the galaxy centre. Thus while there is a good correspondence between the photometric and kinematic bar classifications in the final sample, there are exceptions. We discuss these statistics in light of the kinematic bar detectability implied by Fig. 9 in Section 5.3.

# 5 DISCUSSION

In this section, we interpret the DISKFIT results for the final sample of 37/100 DR1 galaxies presented in Section 4.3. A discussion of the origin of detected non-circular flows is presented in Section 5.1, DISKFIT's sensitivity to non-circular flows is addressed in Section 5.2 and a comparison of the photometric and kinematic classifications of the final sample galaxies is given in Section 5.3.

#### 5.1 Origin of detected non-circular flows

By definition (equation 2), DISKFIT's bisymmetric model is sensitive to a bisymmetric flow with constant phase. As discussed in Section 2, this model is therefore well suited to detecting bar-like flows in disc galaxies. Fig. 10 shows that we detect bisymmetric flows in most of the photometrically barred galaxies in the final sample that have sufficient H  $\alpha$  to afford a search. Moreover, a visual inspection shows that the kinematic bar angle returned by DISKFIT in those galaxies (Table 2) as well as the extent of the non-circular flow regions agree well with the photometric bar properties observed in the SDSS igr images. We therefore conclude that the bisymmetric flows detected by DISKFIT do indeed represent physical bar-like flows, and interpret the main results in Section 4 in this context.

There are, however, 2/37 (5.4 $^{+6.4}_{-1.8}$  per cent) sample galaxies for which another non-circular flow model is preferred to the bisymmetric model: a radial flow model was deemed optimal in UGC

9476 (Fig. A20), whereas a warped disc was invoked for NGC 36 (Fig. A3). We discuss these special cases here.

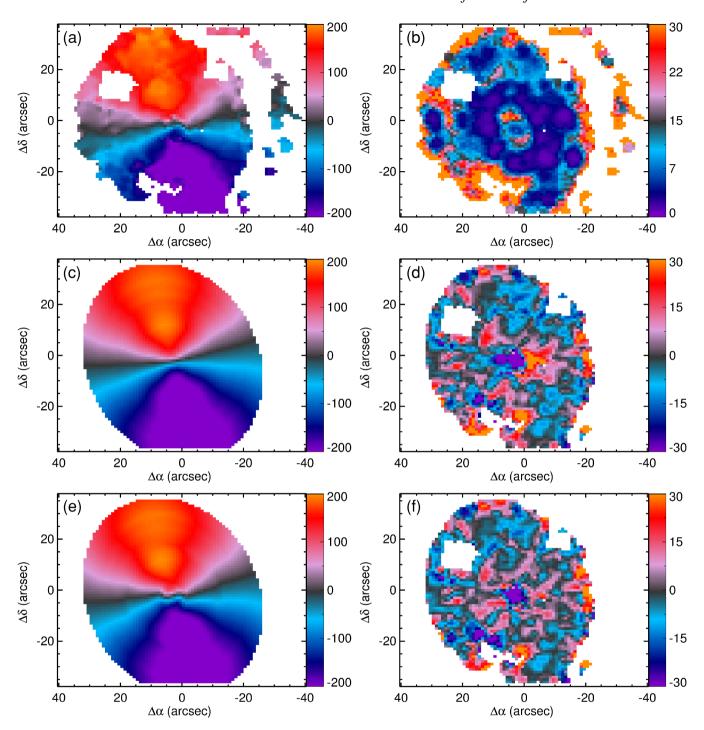
Pure radial flows have not been observed (e.g. Wong, Blitz & Bosma 2004) and are not physically well motivated. It seems unlikely that the radial flows detected in UGC 9476 are indeed pure radial flows, but that DISKFIT has rather misidentified a bar-like flow. This is possible when the bar is aligned along either the major or minor axis of the disc ( $\theta_b \to 0^\circ$  and  $\theta_b \to 90^\circ$  in equation 2), since the non-circular flow components in the bisymmetric model become degenerate with rotation at these bar orientations (Sellwood & Sánchez 2010). The radial model (equation 3) does not have this same degeneracy and is more reliable in these circumstances (recall that both m = 0 and m = 2 flows in the disc plane project to m = 1flows in the sky plane; Schoenmakers, Franx & de Zeeuw 1997). Utilizing the radial model in cases where the bar angle approaches the major or minor axis allows for the continued detection of noncircular flows for these bar geometries. We propose that there is a kinematic bar signature in UGC 9476 along its major axis, which has been detected by the radial model. Despite its classification as photometrically unbarred (Table 1), a linear feature appears to be visible along the major axis in the SDSS igr composite image (see Fig. A20) that approximately matches the extent of the radial flows detected. A more detailed analysis of this galaxy will be performed using DISKFIT's photometric branch as part of future work.

We find that the kinematics of NGC 36 are best described by a warped disc model instead of non-circular flows in a flat disc. This galaxy is photometrically classified as barred however, we find significant uncertainties in the derived velocities for the bisymmetric model. There are hints of a radial change in PA in the velocity field thus indicating that a warp may be present. It is also possible that NGC 36 hosts an oval disc instead of a warp, which would have a similar kinematic signature (e.g. Kormendy 2013). If NGC 36 has an inner warp, the frequency of 1/37 (2.7 $^{+5.7}_{-0.8}$  per cent) galaxies seems high compared to other studies (e.g. Briggs 1990; García-Ruiz, Sancisi & Kuijken 2002; de Blok et al. 2008); however, none of these studies selected statistically representative samples.

The discussion above suggests that the warped flow that we detect in NGC 36 is not a misidentified bar-like flow, but results from different physical processes in the disc. This suggests that 1/12 (8.3 $^{+14.9}_{-2.8}$  per cent) of the coherent non-circular flows in intermediate-late-type CALIFA galaxies do not stem from bars, with the important caveat that the sample studied here is relatively small. Since our discussion in the sections below pertains to bar-like non-circular flows, we omit NGC 36 from further consideration.

## 5.2 Sensitivity to bar-like flows

Fig. 9 illustrates that the detected non-circular flows in the final sample have at least one component with an amplitude that exceeds  $15 \, \mathrm{km \, s^{-1}}$  over at least two independent radial bins. As discussed in Section 5.1, the physical implication of this threshold for bar-like flows in galaxies depends on the bar angle: equation (2) becomes degenerate for bars close to either the major or minor axis of the disc, making them more difficult to reliably detect. A thorough simulation of the effect for the CALIFA sample is beyond the scope of this work, and is not justified given the relatively small sample studied here. Our experience suggests, however, that DISKFIT's sensitivity to bar-like flows is unaffected by bar angle when the latter is more than  $\sim 10^{\circ}$  from the disc major or minor axis in intermediate-inclination galaxies. The bar-like flows detected by DISKFIT for the 10 galaxies in Fig. 9 are at least  $\sim 20^{\circ}$  from either the major or minor axis,



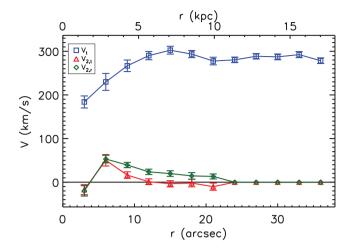
**Figure 5.** DISKFIT model results for NGC 7321, a galaxy that is representative of the *Non-Circular Flows* category. (a) H  $\alpha$  velocity field. (b) Uncertainties in the velocity. (c) Best-fitting rotation only model. (d) Rotation only model residuals. (e) Best-fitting bisymmetric model. (f) Bisymmetric model residuals. In all panels, the colourbar is in km s<sup>-1</sup>.

suggesting that bar angle is not influencing the flow detectability therein.

Of the 8/37 (21.6 $^{+8.2}_{-5.2}$  per cent) gas-rich galaxies photometrically classified as barred for which the bisymmetric model is optimal, the average detected flow amplitude is  $V_{2,t,avg} = 9 \text{ km s}^{-1}$  over  $\sim 3.5 \text{ kpc}$  and  $V_{2,t,avg} = 28 \text{ km s}^{-1}$  over  $\sim 5.5 \text{ kpc}$ . Small-number statistics preclude us from correcting those numbers for the CALIFA selection function (Walcher et al. 2014). However, the fact that we detect such flows in most (8/9 or  $88.9^{+3.9}_{-18.3}$  per cent) of the photometri-

cally barred galaxies with sufficient H  $\alpha$  to afford a search suggests that this flow amplitude is characteristic of barred galaxies with the masses probed by CALIFA. We conclude that non-circular flows due to bars in CALIFA galaxies are detectable by DISKFIT, provided that they are at intermediate angles to the disc major and minor axes.

On the other hand, we detect non-circular flows in only 1/7 ( $14.3^{+21.4}_{-5.3}$  per cent) galaxies of photometric classification AB. This galaxy (NGC 477; Fig. A4) has non-circular flows as high as



**Figure 6.** Kinematic components for NGC 7321, whose optimal kinematic model is the bisymmetric model. The blue curve is  $\bar{V}_t$  (the rotation curve) for the bisymmetric model shown in Fig. 5, the red curve is  $V_{2,t}$  and green curve is  $V_{2,r}$ .

 $70\,\mathrm{km\,s^{-1}}$ , extending  $\sim 4\,\mathrm{kpc}$  from the centre. There is a masked star near the minor axis of the velocity field that could have interfered with the fit, raising the possibility that the non-circular flows in this system are overestimated. Regardless, our non-detection of most AB galaxies suggests that the non-circular flows associated with their weaker/intermediate bars fall below our detection threshold. At the characteristic distance of these galaxies in our sample, this implies that these flows are weaker than  $15\,\mathrm{km\,s^{-1}}$  and/or do not extend more than  $2.25\,\mathrm{kpc}$  in radius.

# 5.3 Galaxies with different kinematic and photometric bar classifications

Fig. 10 illustrates that for the majority of the galaxies in the final sample, the kinematic classification obtained from our DISKFIT models matches the photometric classification in Table 1. By and large, we find bar-like flows in photometrically barred galaxies with sufficient H  $\alpha$  to afford a search, and that the rotation only model best describes the velocity fields of photometrically unbarred galaxies. There are exceptions, however: we find no evidence of bar-like flows in the barred galaxy UGC 5359 (Fig. A9), and significant non-

circular flows in the photometrically unbarred galaxies NGC 7819, UGC 9476 and NGC 7025 (Figs A1, A20 and A32, respectively). In this section, we investigate the origin of these discrepancies to estimate the incidence of systems where the photometric bar classification is different from that inferred kinematically.

We find no evidence for bar-like flows in the photometrically barred galaxy UGC 5359 (Fig. A9). However, an examination of the SDSS image reveals that the bar angle approaches the disc major axis, making bar-like flows difficult to detect (see Sections 5.1 and 5.2). It is therefore plausible that the amplitude of the bar-like flows in UGC 5359 resemble those of other barred galaxies in the sample, but that the bar angle precludes detecting these flows with DISKFIT's bisymmetric model. We see some evidence for non-circular flows in the radial model for this galaxy, although they are not as convincing as those for UGC 9476 in Section 5.1.

On the other hand, we do detect non-circular flows in the photometrically unbarred galaxies NGC 7819, UGC 9476 and NGC 7025 (Figs A1, A20 and A32, respectively). We discussed UGC 9476 in Section 5.1, suggesting that it contains a major axis bar and is therefore photometrically misclassified. For NGC 7819 and NGC 7025, the average non-circular flows detected are  $V_{2,t,avg} = 85 \,\mathrm{km}\,\mathrm{s}^{-1}$ over  $\sim 8.3$  arcsec rings ( $\sim 9$  kpc) and  $V_{2,\text{r,avg}} = 48 \text{ km s}^{-1}$  over  $\sim 6$ 3 arcsec rings ( $\sim$ 6.5 kpc): Fig. 9 shows that they are well above our detection threshold. We re-examined the SDSS images for these two systems and find no evidence for a bar that was missed during the photometric classification. It is possible that the non-circular flows that we detect are being driven by another mechanism, such as an interaction with a nearby galaxy. Mahtessian (1998) classify NGC 7819 as a member of a group by searching for neighbours with similar radial velocities. NGC 7025 is isolated (Karachentseva 1973), however, and we see no obvious photometric feature that could drive the non-circular flows that we detect. It is possible that a bar-like feature in NGC 7025 is present in the NIR but not in the optical. This possibility is unlikely, however, since the amplitude of the non-circular flows implies a relatively strong bar, and weak bars are the ones that are typically obscured in the optical (Marinova et al. 2009a).

Considering the above discussion, and excluding intermediate (AB) bars, we conservatively conclude that the photometric classification of the final sample galaxies with sufficient H  $\alpha$  to enable a search for non-circular flows belies a different kinematic classification in at least 2/23 (8.7 $^{+9.6}_{-2.9}$  per cent) systems (UGC 9476 and NGC 7025). Systematic searches for bar-like flows thus not only characterize the kinematic properties of galaxy bars, but may also

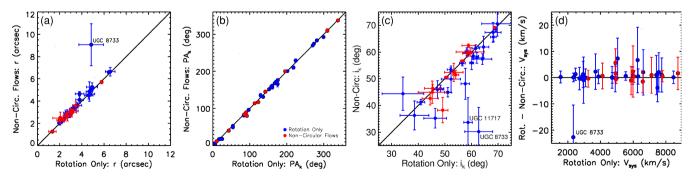


Figure 7. Comparison of DISKFIT disc geometry for best-fitting rotation only versus non-circular flow models for each final sample galaxy. In all panels, blue dots represent galaxies in the *Rotation Only* category including those classified as *Can't Tell*, while red dots represent galaxies in the *Non-Circular Flows* category. (a) Position  $r = \sqrt{x^2 + y^2}$  of the kinematic centre relative to centre pixel. (b) PA. The uncertainties are smaller than the symbol size for many systems. (c) Kinematic inclination,  $i_k$ . (d) Difference between  $V_{sys}$  returned from the rotation only and bisymmetric models, as a function of that returned by the rotation only model. In all panels, the solid black line shows the 1:1 relation between parameters. Outliers from this relation are labelled.

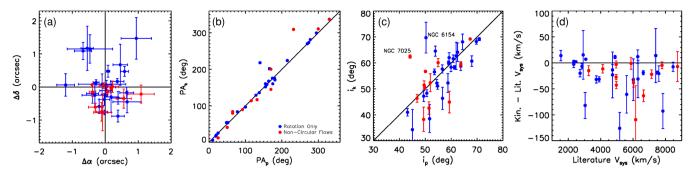
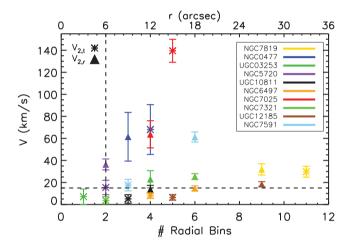


Figure 8. Comparison of optimal DISKFIT disc geometry with literature values from Table 1 for each final sample galaxy. In all panels, blue dots represent galaxies in the *Rotation Only* category including those classified as *Can't Tell*, while red dots represent galaxies in the *Non-Circular Flows* category. (a) Difference in centre position of right ascension and declination relative to photometric centre. (b) PA. The uncertainties are smaller than the symbol size for many systems. (d) Kinematic inclination ( $i_k$ ) compared with the photometric inclination derived by the CALIFA collaboration ( $i_p$ ). (d) Difference between  $V_{sys}$  returned from the rotation only and bisymmetric models, as a function of literature values. In all panels, the solid black line shows the 1:1 relation between parameters.



**Figure 9.** Mean value of  $V_{2,t}$  (stars) and  $V_{2,r}$  (triangles) as a function of the number of independent radial bins (bottom) or arcsec from the centre (top) over which the flow was detected, in final sample galaxies where the bisymmetric model was judged to be optimal (column (3) = 'm2' in Table 2). The error bars are the standard deviation on the mean. At least one component of each galaxy lies above and to the right of the horizontal and vertical black dashed lines at  $V \sim 15 \, \mathrm{km \, s^{-1}}$  and two radial bins: we adopt these values as the detectability threshold for bisymmetric flows in the final sample.

reveal galaxies in which bar-like flows are driving galaxy evolution despite the lack of a clear photometric bar signature.

Our analysis of the 37/100 CALIFA DR1 galaxies suitable for kinematic modelling hints at the richness of the information that can be gleaned from a systematic search for non-circular flows in nearby galaxies, but the relatively small final sample size precludes a detailed statistical interpretation of our results. That is set to change with the full CALIFA sample of  $\sim\!600$  galaxies that will be available in the near future: scaling the results presented here, we expect that  $\sim\!200$  CALIFA galaxies will ultimately afford detailed kinematic analyses. A joint photometric and kinematic decomposition of the SDSS images for each of these galaxies would enable quantitative comparisons between the bars detected in galaxy images and the non-circular flows found in their velocity fields, affording a three-dimensional examination of nearby barred systems. This work is underway.

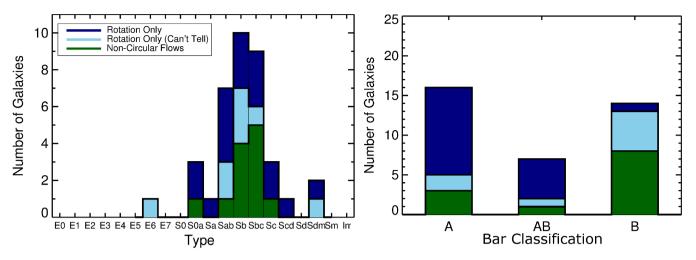
## 6 SUMMARY

We have used DISKFIT to model the H  $\alpha$  velocity fields of gasrich, intermediate-inclination CALIFA DR1 disc galaxies in a direct search for bar-like flows. We apply rotation only, bisymmetric flows, and (in some cases) radial flow and warped disc models to 49/100 galaxies with photometric inclinations  $40^{\circ} < i_p < 70^{\circ}$  and a visible velocity field gradient, and find acceptable models for a final sample of 37/100 systems. For each galaxy in the final sample, we use a  $\chi^2$  test to search for statistically significant non-circular flows as well as examine residual plots to determine the optimal kinematic model.

We find good agreement between the disc geometry returned by DISKFIT for different models of the same galaxy, as well as between the optimal model values and the photometric disc geometries and systemic velocities from the literature. Of the 29/37 final sample systems with sufficient H  $\alpha$  near the galaxy centre to afford a search for non-circular flows, we deem that 17/29 (58.6 $_{-9.4}^{+8.3}$  per cent) are best described by the rotation only model while 12/29 (41.4 $_{-8.3}^{+9.4}$  per cent) contain statistically significant non-circular flows. Of these latter galaxies we find that the bisymmetric model is optimal for 10/12 (83.3 $_{-15.5}^{+5.9}$  per cent) systems, and favour radial flows and a warped disc for the remaining two galaxies, respectively. At least one bisymmetric flow component in each of the 10 galaxies exceeds 15 km s<sup>-1</sup> over at least two independent radial bins ( $\sim$ 2.25 kpc at the characteristic final sample distance of  $\sim$ 77 Mpc): we adopt this pair of values as the detectability threshold for DISKFIT in the final sample.

Accounting for the low sensitivity of the bisymmetric model to bar-like flows aligned near the major or minor axis of the disc and comparing our optimal kinematic models to the photometric bar classifications of the sample galaxies, we conclude that the non-circular flows that we detect in 11/12 (91.7 $^{+2.8}_{-14.9}$  per cent) galaxies stem from bars, while the remaining system likely harbours an inner warp or oval disc. We find that photometrically barred CALIFA DR1 galaxies have an average non-circular flow ( $V_{2,t}$  and  $V_{2,r}$ ) amplitude of  $V_2 = 16 \pm 1$  km s<sup>-1</sup> over a radial extent of 4.5 kpc. On the other hand, the absence of non-circular flows in galaxies with intermediate (AB) bar classifications implies that these flows fall below our detection threshold for intermediate bar angles. It is evident from these relations that bisymmetric flows are nearly ubiquitous in strongly barred galaxies, as one would expect.

There are four galaxies in the final sample where our kinematic classification differs from that obtained photometrically: we find that the barred galaxy UGC 5359 is best described by a rotation



**Figure 10.** Optimal kinematic model for final sample galaxies as a function of morphological type (left) and bar classification (right). The dark blue colour represents the *Rotation Only* models, light blue are the galaxies classified as *Can't Tell*, dark green are cases of *Non-Circular Flows*: bisymmetric, radial and warp models combined.

only model, and detect bar-like non-circular flows in the unbarred systems NGC 7819, UGC 9476 and NGC 7025. We find it plausible that DISKFIT missed the putative bar-like flows in UGC 5359 due to geometric effects, and that the photometric classification of UGC 9476 is incorrect. It is also plausible that interactions in the group in which NGC 7819 resides have caused the non-circular flows that we detect; however, NGC 7025 is isolated. We therefore conclude that in 2/23 (8.7 $_{-2.0}^{+9.6}$  per cent) galaxies – or  $\sim$ 10 per cent of the time – the photometric classification of CALIFA DR1 galaxies belies a different kinematic classification.

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#### REFERENCES

Abazajian K. et al., 2003, AJ, 126, 2081

Abazajian K. et al., 2009, ApJS, 182, 543

Adelman-McCarthy J. K. et al., 2008, ApJS, 175, 297

Aguerri J. A. L., Mendez-Abreu J., Corsini E. M., 2009, A&A, 495, 491

Aguerri J. A. L. et al., 2015, A&A, 576, 102

Athanassoula E., 1992, MNRAS, 259, 345

Athanassoula E., Machado R. E. G., Rodionov S. A., 2013, MNRAS, 429, 1949

Barazza F. D., Jogee S., Marinova I., 2008, ApJ, 675, 1194

Barrera-Ballesteros J. K. et al., 2014, A&A, 568, A70

Bershady M. A., Verheijen M. A. W., Swaters R. A., Andersen D. R., Westfall K. B., Martinsson T., 2010, ApJ, 716, 198

Blanc G. A. et al., 2013, AJ, 145, 138

Briggs F. H., 1990, ApJ, 352, 15

Bryant J. J. et al., 2015, MNRAS, 447, 2857

Bundy K. et al., 2015, ApJ, 798, 7

Cameron E., 2011, PASA, 28, 128

Cappellari M. et al., 2011, MNRAS, 413, 813

Croom S. M. et al., 2012, MNRAS, 413, 813

Davoust E., Considere S., 1995, A&AS, 110, 19

de Blok W. J. G., Walter F., Brinks E., Trachternach C., Oh S.-H., Kennicutt R. C., Jr, 2008, AJ, 136, 2648

de Vaucouleurs G., de Vaucouleurs A., Corwin J. H. G., Buta R. J., Paturel G., Fouque P., 1991, Third Reference Catalogue of Bright Galaxies, Version 3.9. Springer, New York, NY

de Zeeuw P. T. et al., 2002, MNRAS, 329, 513

dell'Antonio I. P., Bothun G. D., Geller M. J., 1996, AJ, 112, 1759

Epinat B. et al., 2008a, MNRAS, 388, 500

Epinat B., Amram P., Marcelin M., 2008b, MNRAS, 390, 466

Erwin P., Debattista V. P., 2013, MNRAS, 431, 3060

Eskridge P. B. et al., 2000, AJ, 119, 536

Falco E. E. et al., 1999, PASP, 111, 438

Freudling W., Haynes M. P., Giovanelli R., 1992, ApJS, 79, 157

Friedli D., Martinet L., 1993, A&A, 277, 27

García-Lorenzo B. et al., 2014, A&A, 573, A59

García-Ruiz I., Sancisi R., Kuijken K., 2002, A&A, 394, 769

Giovanelli R., Haynes M. P., 1993, AJ, 105, 1271

Haynes M. P., Giovanelli R., Herter T., Vogt N. P., Freudling W., Maia M. A. G., Salzer J. J., Wegner G., 1997, AJ, 113, 1197

Hernandez O., Carignan C., Amram P., Chemin L., Daigle O., 2005, MNRAS, 360, 1201

Huchra J. P., Geller M. J., Corwin H. G., Jr, 1995, ApJS, 99, 391

Husemann B. et al., 2013, A&A, 549, A87

Karachentseva V. E., 1973, Astrofiz. Issledovaniia Izvestiya Spetsial'noj Astrofizicheskoj Obs., 8, 3

Kehrig C. et al., 2012, A&A, 540, A11

Kelz A. et al., 2006, PASP, 118, 129

Kent B. R. et al., 2008, AJ, 136, 713

Kormendy J., 2013, in Falcón-Barroso J., Knapen J. H., eds, Secular Evolution in Disk Galaxies. Cambridge Univ. Press, Cambridge, p. 1

Kormendy J., Bender R., 2012, ApJS, 198, 2

Kormendy J., Kennicutt R. C., 2004, ARA&A, 42, 603

Kuzio de Naray R., Arsenault C. A., Spekkens K., Sellwood J. A., McDonald M., Simon J. D., Teuben P., 2012, MNRAS, 427, 2523

Laurikainen E., Salo H., Athanassoula E., Bosma A., Herrera-Endoqui M., 2014, MNRAS, 444, L80

Lu N. Y., Hoffman G. L., Groff T., Roos T., Lamphier C., 1993, ApJS, 88, 383

Mahtessian A. P., 1998, Astrofizika, 41, 308

Marinova I. et al., 2009a, in Jogee S., Marinova I., Hao L., Blanc G. A., eds, ASP Conf. Ser. Vol. 419, Galaxy Evolution: Emerging Insights and Future Challenges. Astron. Soc. Pac., San Francisco, p. 138

Marinova I. et al., 2009b, ApJ, 698, 1639

Marzke R. O., Huchra J. P., Geller M. J., 1996, AJ, 112, 1803

Masters K. L. et al., 2011, MNRAS, 411, 2026

Mendez-Abreu J., Debattista V. P., Corsini E. M., Aguerri J. A. L., 2014, A&A, 572, A25

Mulchaey J. S., Regan M. W., 1997, ApJ, 482, L135

Nishiura S., Shimada M., Ohyama Y., Murayama T., Taniguchi Y., 2000, AJ, 120, 1691

Nordgren T. E., Chengalur J. N., Salpeter E. E., Terzian Y., 1997, AJ, 114, 77

O'Neil K., 2004, AJ, 128, 2080

Ramella M., Geller M. J., Huchra J. P., Thorstensen J. R., 1995, AJ, 109, 1458

Reese A. S., Williams T. B., Sellwood J. A., Barnes E. I., Powell B. A., 2007, AJ, 133, 2846

Regan M. W., Sheth K., Vogel S. N., 1999, ApJ, 526, 97

Rosales-Ortega F. F., Kennicutt R. C., Sánchez S. F., Díaz A. I., Pasquali A., Johnson B. D., Hao C. N., 2010, MNRAS, 405, 735 Roth M. M. et al., 2005, PASP, 117, 620

Saintonge A., Giovanelli R., Haynes M. P., Hoffman G. L., Kent B. R., Martin A. M., Stierwalt S., Brosch N., 2008, AJ, 135, 588

Sánchez S. F., 2006, Astron. Nachrichten, 327, 850

Sánchez S. F. et al., 2012, A&A, 538, A8

Schoenmakers R. H. M., Franx M., de Zeeuw P. T., 1997, MNRAS, 292, 349

Sellwood J. A., Sánchez R. Z., 2010, MNRAS, 404, 1733

Sellwood J. A., Wilkinson A., 1993, Rep. Prog. Phys., 56, 173

Sheth K., Vogel S. N., Regan M. W., Thornley M. D., Teuben P. J., 2005, ApJ, 632, 217

Sheth K., Mizusawa T., Kim T., Munoz-Mateos J., Regan M. W., de Swardt B., Gadotti D., S4G Team, 2011, BAAS, 43, 207.06

Shlosman I., Frank J., Begelman M. C., 1989, Nature, 338, 45

Shlosman I., Begelman M. C., Frank J., 1990, Nature, 345, 679

Simard L., Mendel J. T., Patton D. R., Ellison S. L., McConnachie A. W., 2011, ApJS, 196, 11

Skrutskie M. F. et al., 2006, AJ, 131, 1163

Spekkens K., Sellwood J. A., 2007, ApJ, 664, 204

Theureau G., Bottinelli L., Coudreau-Durand N., Gouguenheim L., Hallet N., Loulergue M., Paturel G., Teerikorpi P., 1998, A&AS, 130, 333

Theureau G., Hanski M. O., Coudreau N., Hallet N., Martin J.-M., 2007, A&A 465, 71

Walcher C. J. et al., 2014, A&A, 569, A1

Wegner G., Haynes M. P., Giovanelli R., 1993, AJ, 105, 1251

Wegner G. et al., 2003, AJ, 126, 2268

Weinberg M. D., Katz N., 2002, ApJ, 580, 627

Weiner B. J., Sellwood J. A., Williams T. B., 2001, ApJ, 546, 931

Whyte L. F., Abraham R. G., Merrifield M. R., Eskridge P. B., Frogel J. A., Pogge R. W., 2002, MNRAS, 336, 1281

Wong T., Blitz L., Bosma A., 2004, ApJ, 605, 183

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